The Large Scale Structure of the Universe 4: Redshift Space Distorions and New observables

Eusebio Sánchez Álvaro
CIEMAT

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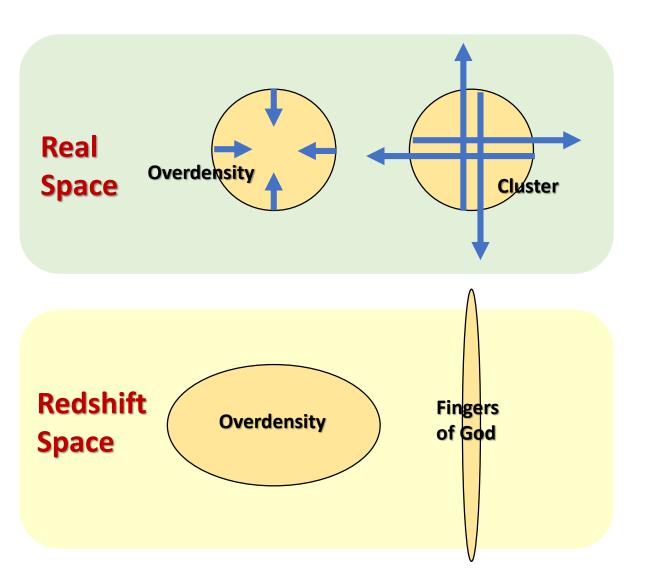
RSD, combined probes and future projects

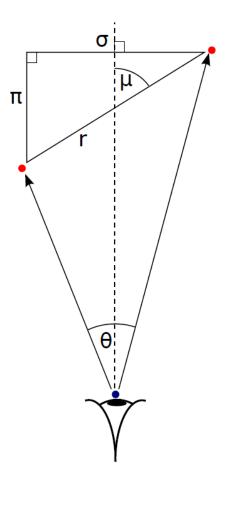
Redshift Space Distortions. Modelling and measurement Cosmology with RSD

Combined probes: cross-correlations
Brief intro to Weak Gravitational Lensing
Cosmology results from DES 3x2pt (combining probes)

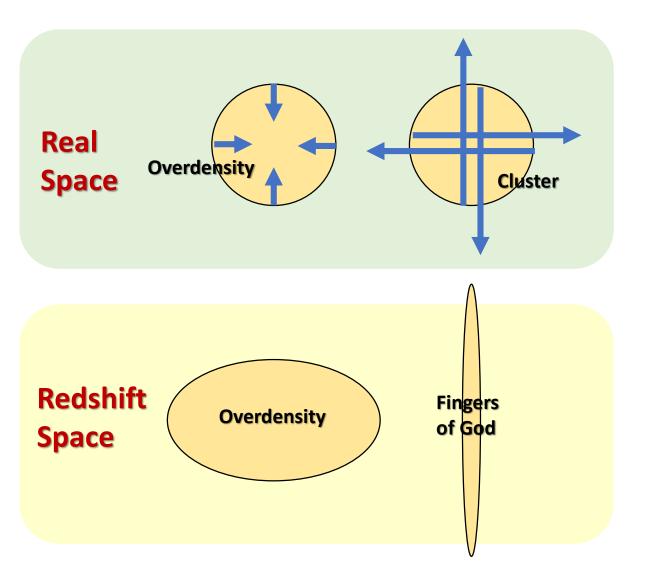
Very brief description of future experiments on LSS (DES, DESI, Euclid, LSST)

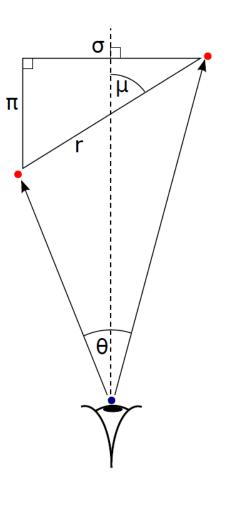
The spatial distribution of galaxies appears squashed and distorted when studied in the redshift space. But we only measure redshift, not distances. The RSD are always present

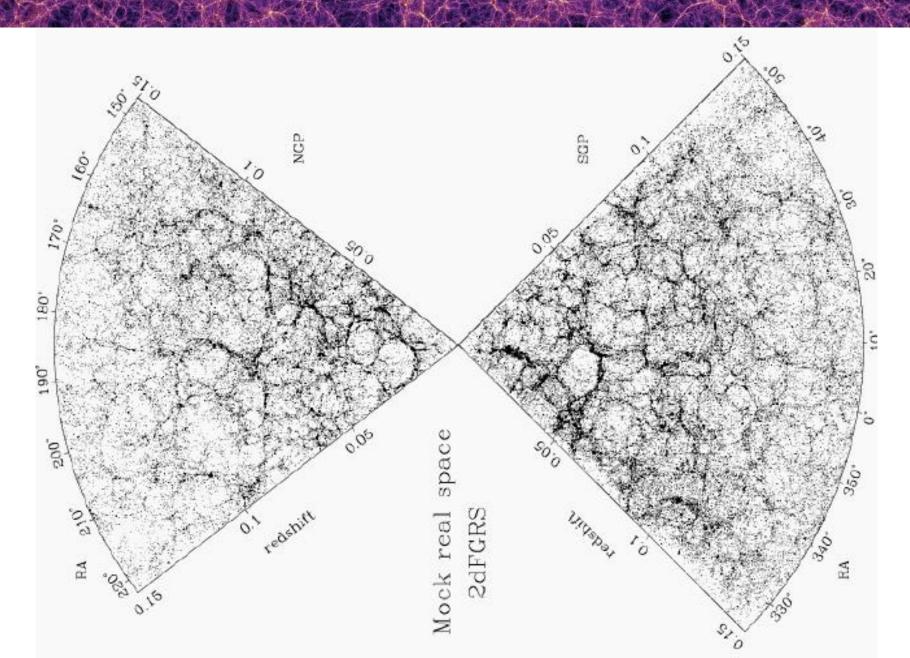


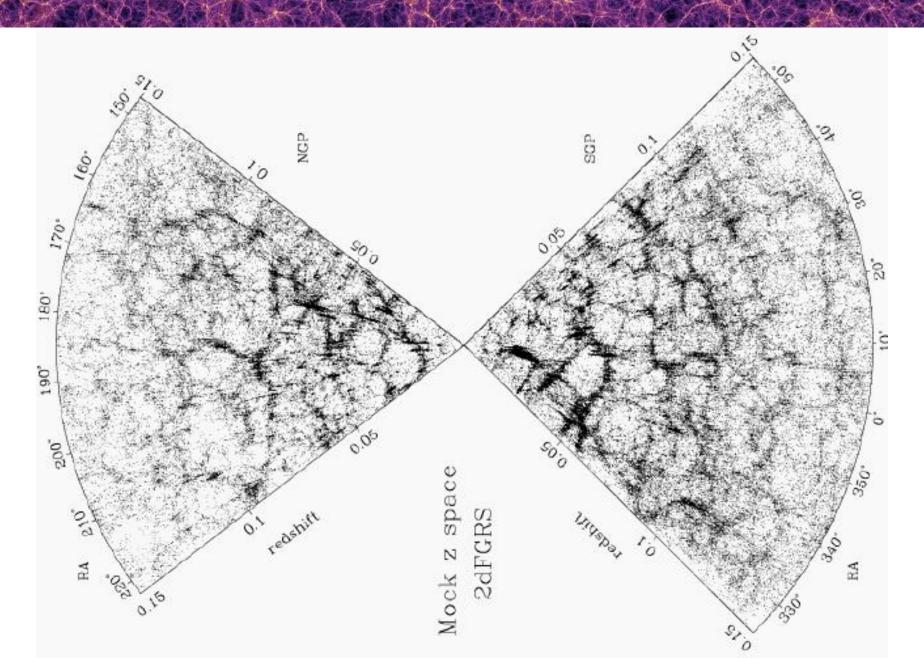


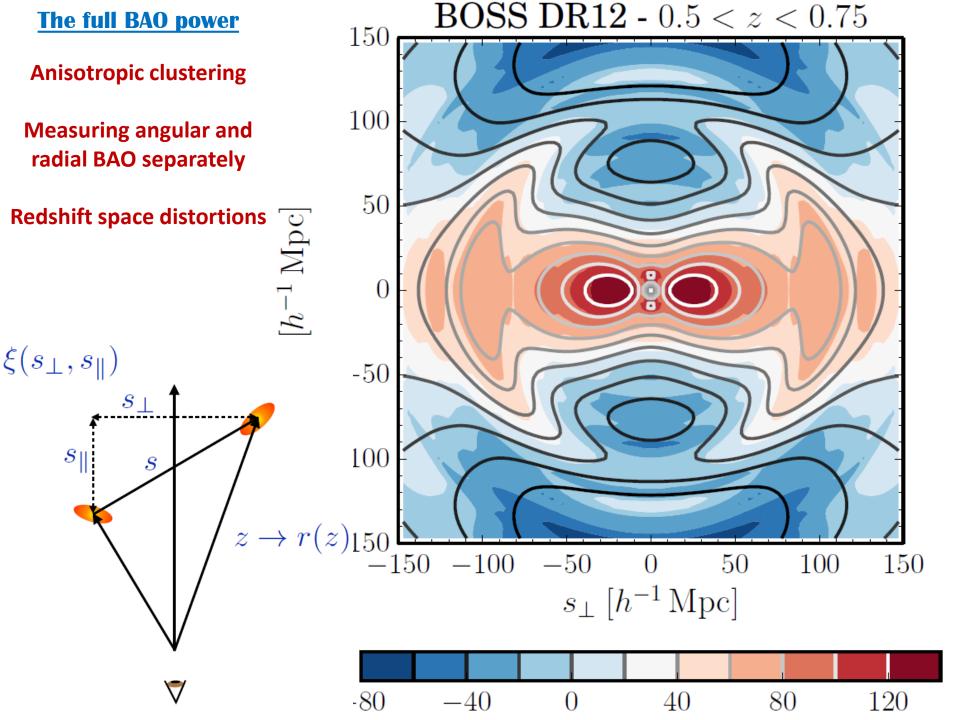
They are a consequence of peculiar velocities → Coming from structure They carry very valuable information about cosmology



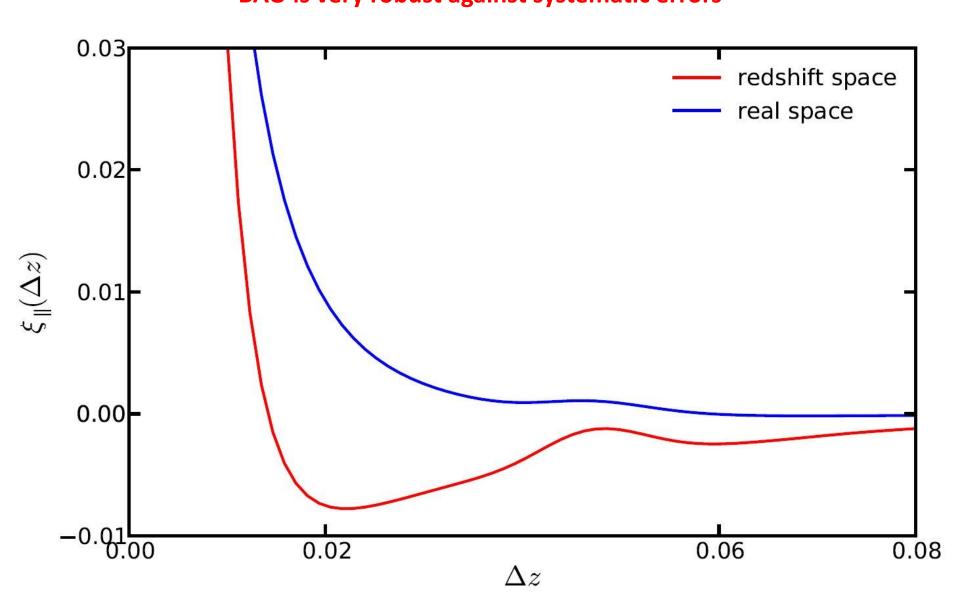






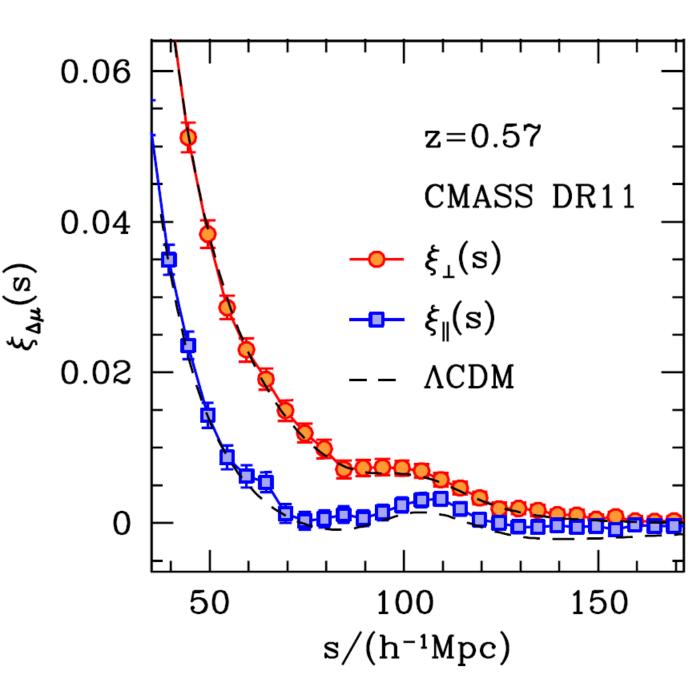


The shape of the correlation function changes dramatically when RSD are included However the BAO peak position does not change BAO is very robust against systematic errors

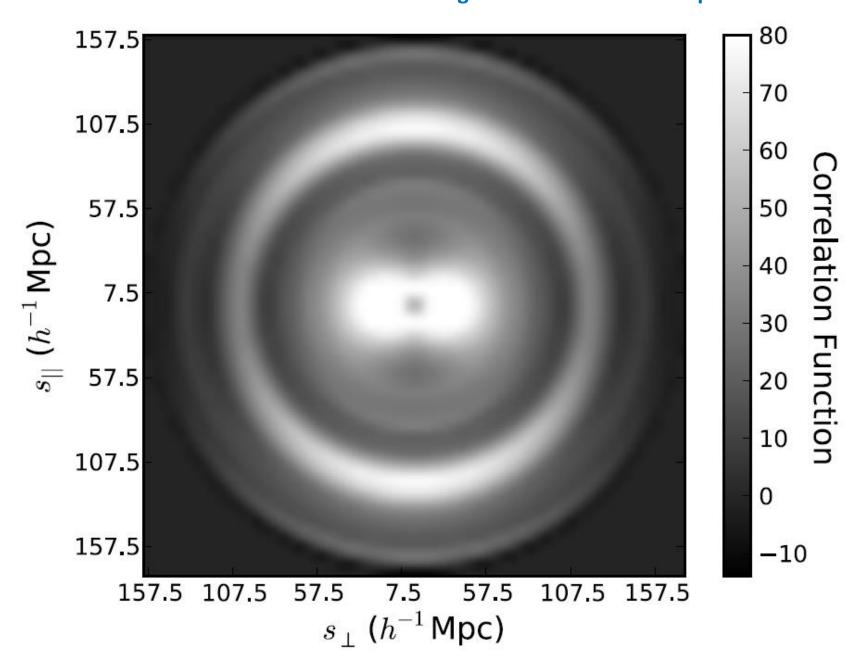




RSD are one of the cosmological probes sensitive to the growth of structure that are used today



RSD effect is concentrated in intermediate scales of the correlation function BAO is seen as an excess in a ring with radius ~110 h-1 Mpc



$$\delta_{s,\mathbf{k}} = (1 + \beta \,\mu_{\mathbf{k}}^2) \,\delta_{r,\mathbf{k}} \qquad \mu_{\mathbf{k}} \equiv \mathbf{k} \cdot \hat{\mathbf{n}}_z/k$$
$$\beta = \frac{f}{b} \approx \frac{\Omega_{\text{m0}}^{0.6}}{b} \qquad \beta = \frac{\Omega_{M}^{\gamma}}{b}$$

Hence, redshift-space distortions induce an anisotropy in the observed power spectrum, which now is a function of both k and μ_k

$$P_s(k, \mu_{\mathbf{k}}, z) = (1 + \beta(z) \,\mu_{\mathbf{k}}^2)^2 \, P_r(k, z)$$

Redshift space distortions are sensitive to the growth of structures in the Universe

Provide a good test for modified gravity theories through the determination of the growth factor and the growth index

Power spectrum is normalized using the variance of Galaxy distribution smoothed on a scale of 8h⁻¹ Mpc or

$$\sigma_8(z) = \sigma_{8,0} D(z)$$

What we really measure from RSD are $f\sigma_8$ and $b\sigma_8$

$$P_s(k, \mu_{\mathbf{k}}, z) = (1 + \beta(z) \,\mu_{\mathbf{k}}^2)^2 \, P_r(k, z)$$

$$\mu_{\mathbf{k}} \equiv \mathbf{k} \cdot \hat{\mathbf{n}}_z / k$$
 $\beta = \frac{\Omega_M'}{h}$

A very common way of studying RSD is by the use of the multipole expansion

$$(1 + \beta \mu_k^2)^2 = \left(1 + \frac{2}{3}\beta + \frac{1}{5}\beta^2\right)\mathcal{P}_0(\mu_k) + \left(\frac{4}{3}\beta + \frac{4}{7}\beta^2\right)\mathcal{P}_2(\mu_k) + \frac{8}{35}\beta^2\mathcal{P}_4(\mu_k)$$

Each term can be independently measured due to the different angular dependence

$$\xi(r,\mu) = \sum_{l} \xi_l(r) \mathcal{P}_l(\mu) \qquad \xi_l(r) = \frac{i^l}{2\pi^2} \int dk P(k) k^2 j_l(kr)$$

$$\xi_s(r,\mu) = b(z)^2 \left\{ \left[1 + \frac{2}{3}\beta + \frac{1}{5}\beta^2 \right] \mathcal{P}_0(\mu)\xi_0(r) + \left[\frac{4}{3}\beta + \frac{4}{7}\beta^2 \right] \mathcal{P}_2(\mu)\xi_2(r) + \frac{8}{35}\mathcal{P}_4(\mu)\xi_4(r) \right\}$$

Non-Linear Effects: Fingers of God

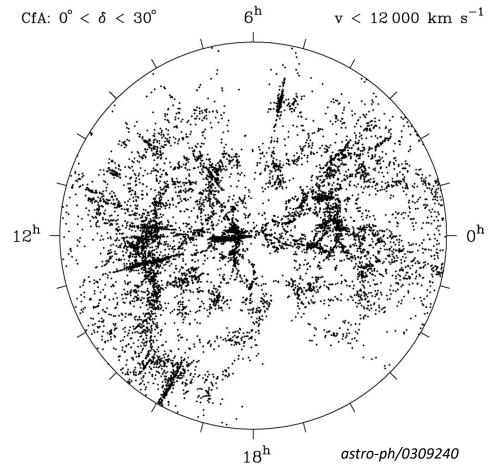
On small (non-linear) scales these velocities are large enough to compensate Hubble's law and the spheres are turned inside out and deformed in shape, forming structures that point towards the observers, commonly known as fingers of God Difficult to model. In general:

$$P_s(k,\mu_{\mathbf{k}},z) = (1+\beta(z)\,\mu_{\mathbf{k}}^2)^2 F(k,\mu_{\mathbf{k}}) \, P_r(k,z)$$

A usual $F(k, \mu)$ is

$$F(k, \mu_{\mathbf{k}}) = \frac{1}{(1 + k^2 \,\mu_{\mathbf{k}}^2 \,\Sigma_v^2)^2}$$

Streaming model



SUMMARY

- What we observe in a redshift survey is the density field in redshift space. A combination of density and velocity fields
- The 3rd dimensión of 3D maps is obtained from redshift, that is a combination of Hubble recession and peculiar velocity
- Distortion is correlated with the density field and can be used to test its growth
- Constrain dD/dlna ~ fσ₈
- 2 regimes: Coherent infall (RSD) or random motion (FoG)

Measurements of RSD in Galaxy surveys: BOSS

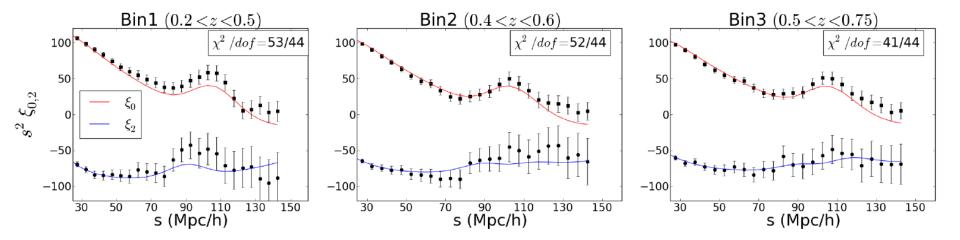
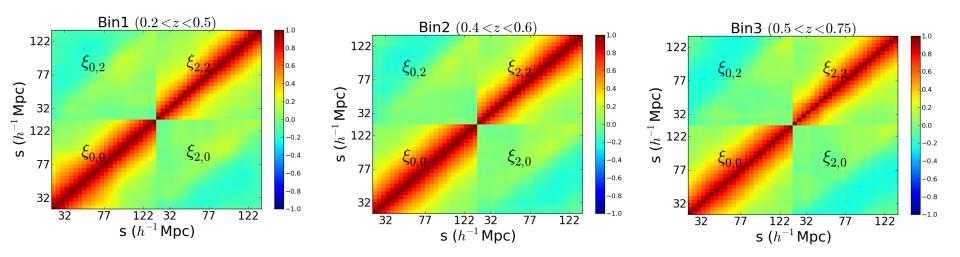


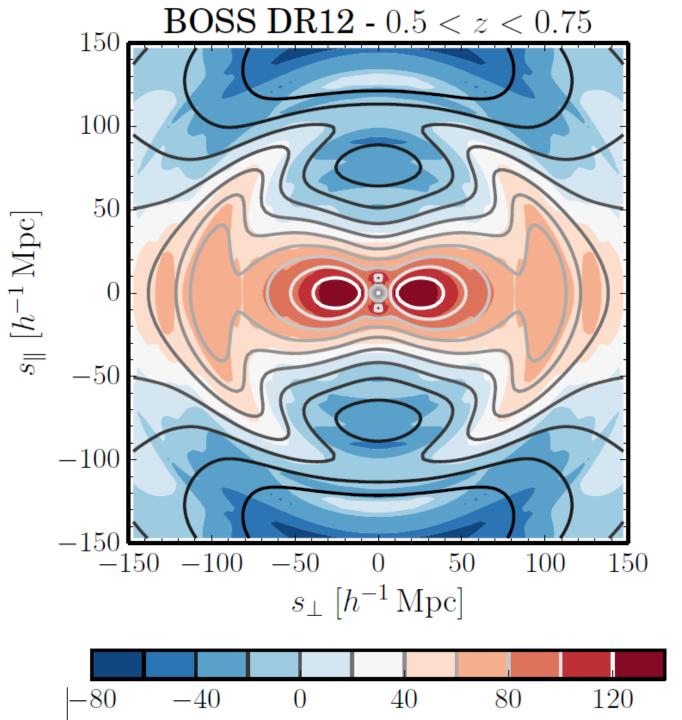
Figure 1. The black dots in the plots of this figure represent monopole (\blacksquare) and quadrupole (\bullet) for BOSS DR12 galaxy sample evaluated at different values of s. The error bars are obtained from the diagonal elements of the covariance matrices corresponding to mocks in the three redshift bins. The red and the blue lines denote the best fit models of monopole and quadrupole of the galaxy data. The analysis assumes a fitting range $25 \ h^{-1}{\rm Mpc} \le s \le 150 \ h^{-1}{\rm Mpc}$ with a bin size of $5 \ h^{-1}{\rm Mpc}$.



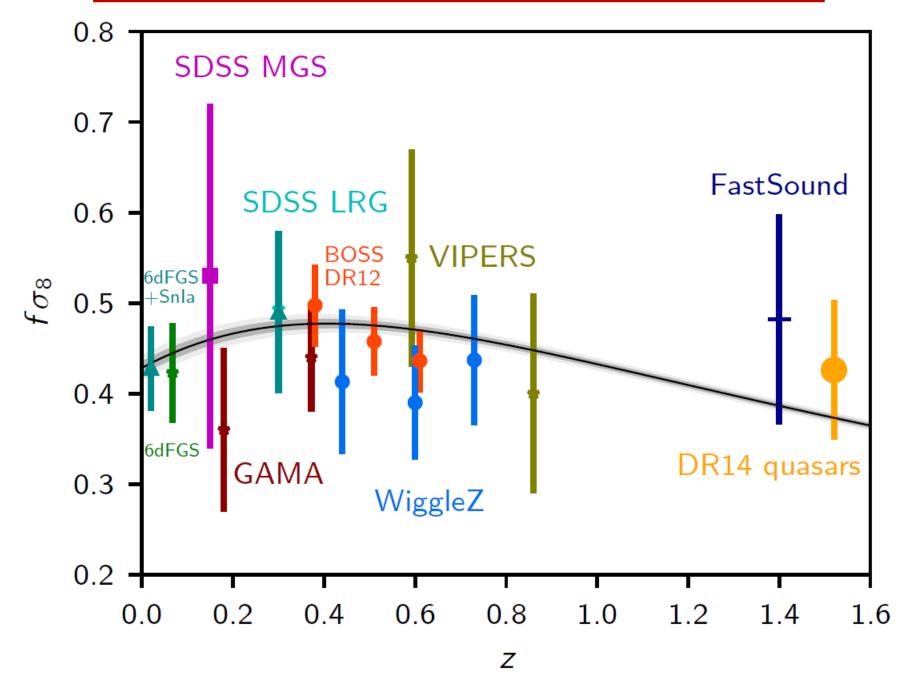
Correlation matrices obtained from MD-P mocks with $z_e = 0.38$, $z_e = 0.51$, $z_e = 0.61$.

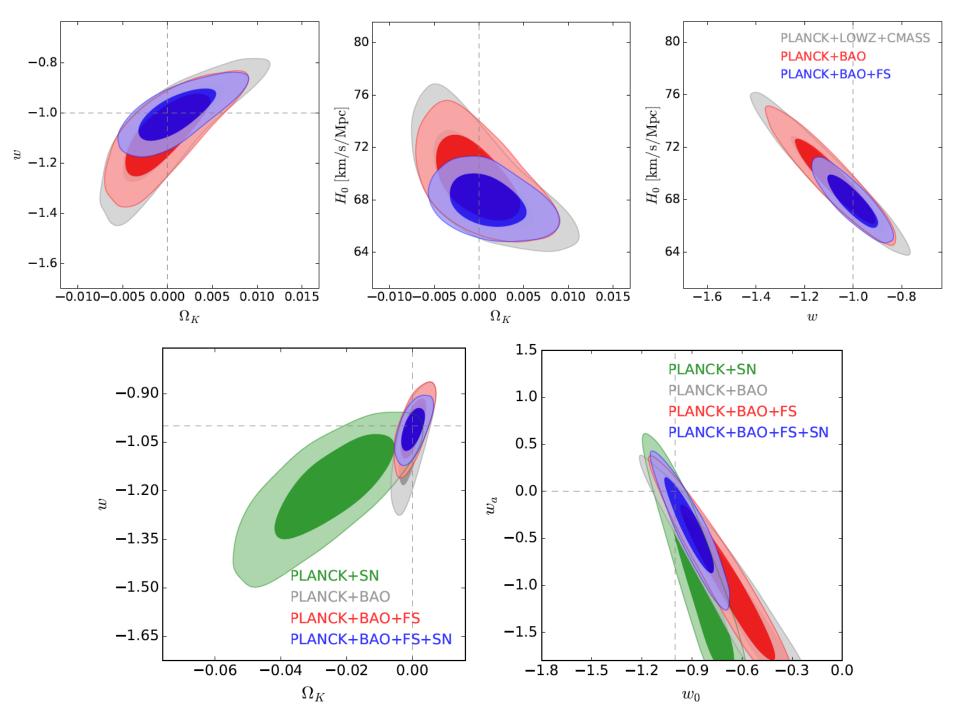
The measured prereconstruction
correlation function in
the directions
perpendicular and
parallel to the line of
sight, in the redshift
range 0.50 < z < 0.75.

The color scale shows
the data and the
contours show the
prediction of the bestfit model



Current status of Growth Factor Measurements





Beyond individual probes

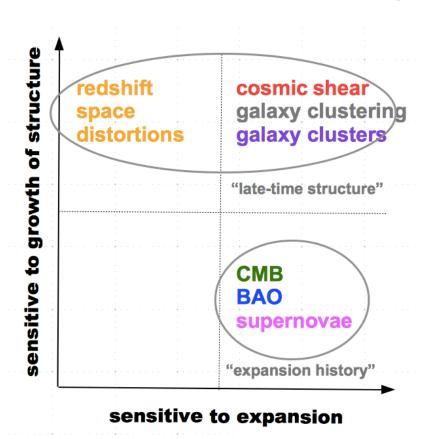
There are many observational probes for dark energy:

<u>Distance probes</u>: SN1a, BAO, CMB, weak lensing, galaxy clusters...

Growth of structure probes: CMB, RSD, weak lensing, galaxy clusters...

No single technique is sufficiently powerful to improve the current knowledge on dark energy by one order of magnitude ->

COMBINATION OF TECHNIQUES

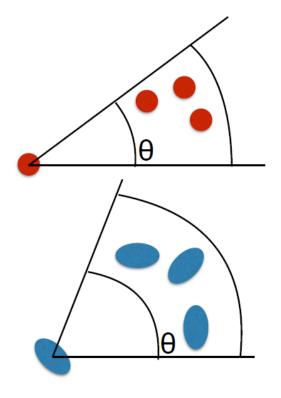


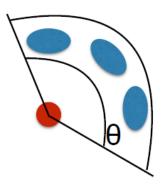
Beyond individual probes

We can measure more properties of galaxies than only their positions: colors, spectra, shape and we can correlate them

Correlations

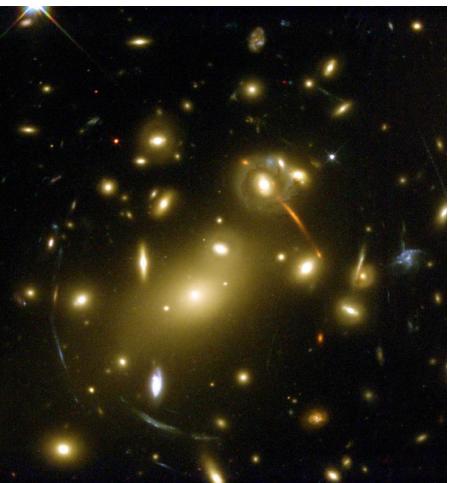
- w(θ)
 Galaxy density (position) correlation function
- $\xi_{+}(\theta)$, $\xi_{-}(\theta)$ Shear (shape) correlation functions
- γ_T(θ)
 Shear around galaxies
 (galaxy-galaxy lensing)

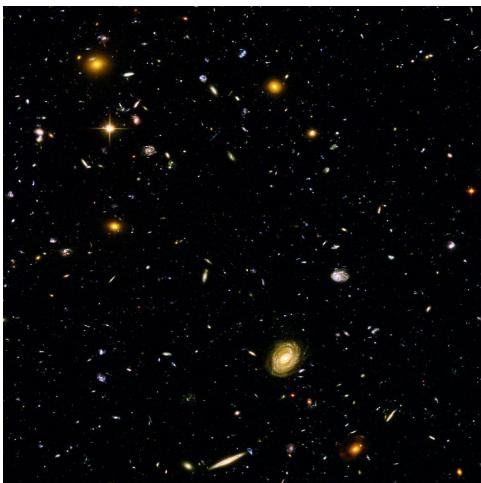




Radiation is deflected in gravitational fields → Image distortion
Since the effect comes from the gravitational field, it is sensitive to all matter/ energy, including dark matter and dark energy

STRONG LENSING WEAK LENSING





The effect depends on the lens mass and the distances between observer, lens and source:

Window to the mass (mostly dark matter) distribution in the lenses

Window to cosmological parameters:

lens

source

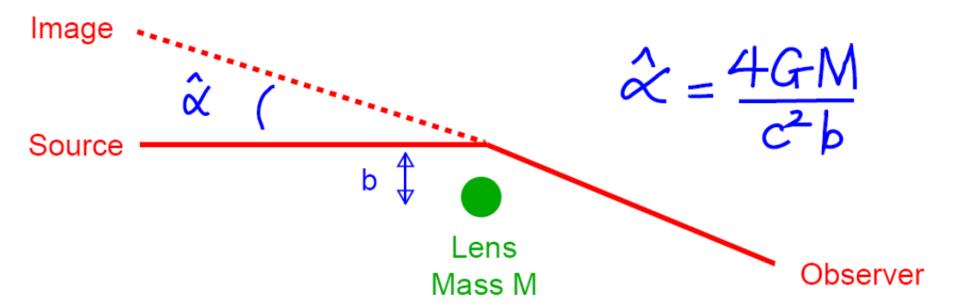
Cosmology changes distances **Dd, Ds, Dds**

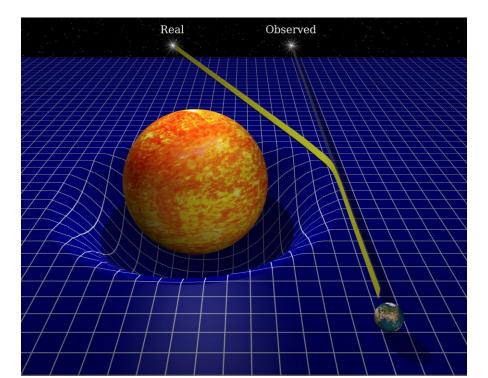
Cosmology changes the growth rate of mass structures in the universe

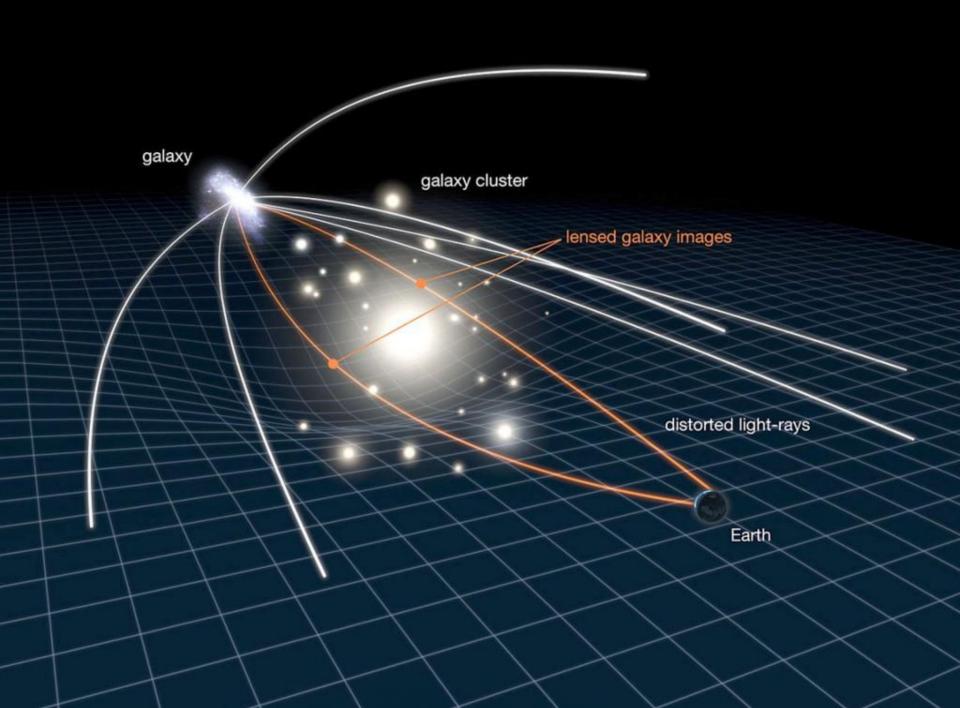
Use galaxies as tracers

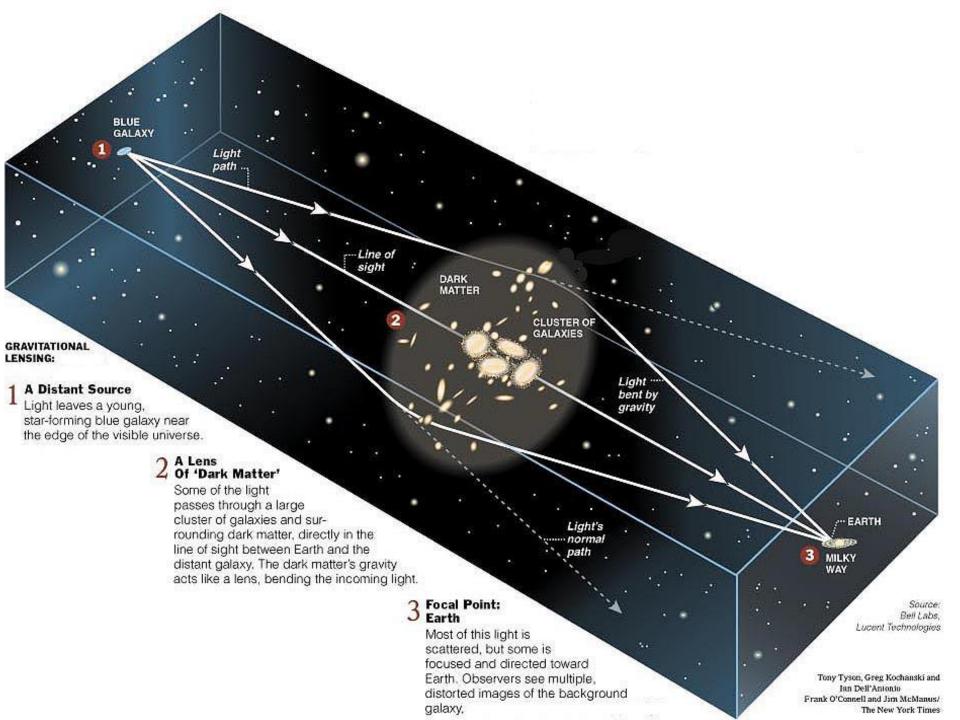
Measure the shapes of background galaxies → Galaxy shapes are distorted by intervening mass → Infer mass integrated along the line of sight

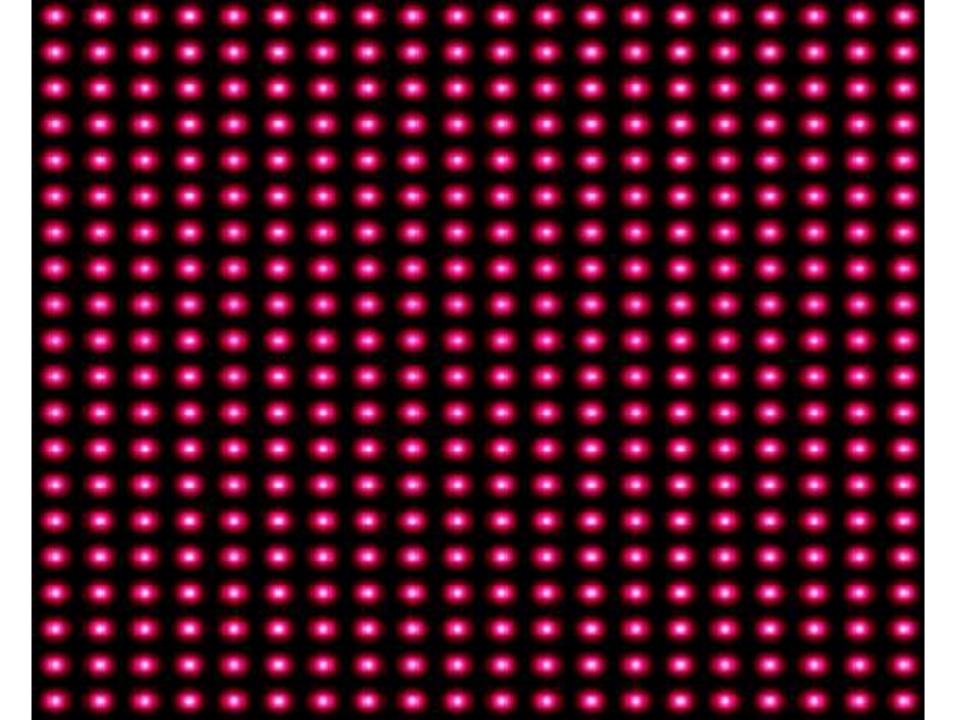






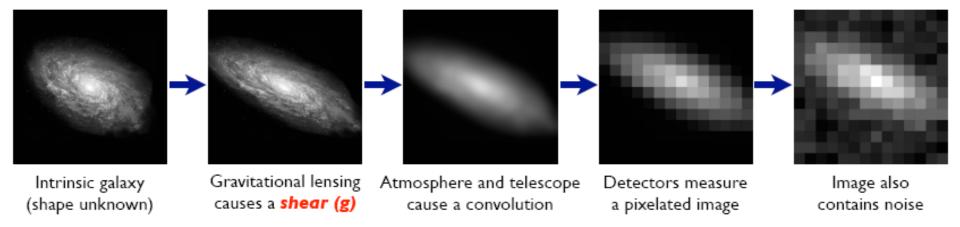






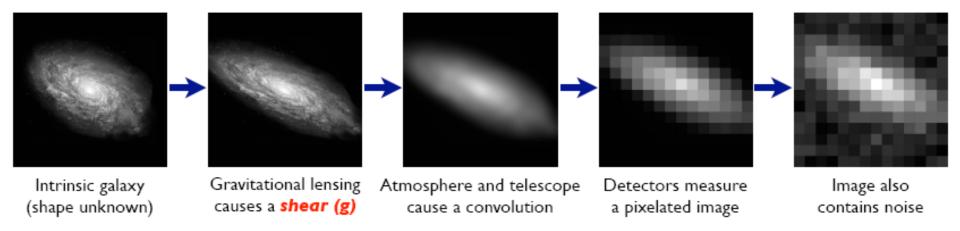
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Effect exagerated by x20

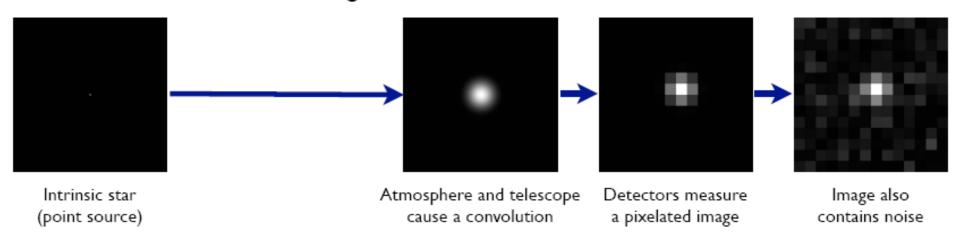


Small and difficult to measure effect, but observable

Effect exagerated by x20



Stars: Point sources to star images:



Small and difficult to measure effect, but observable

Control the measurement using known pointlike objects → stars

The light of distant galaxies is deflected while travelling through the inhomogeneous Universe. Information about mass distributions is imprinted on observed galaxy

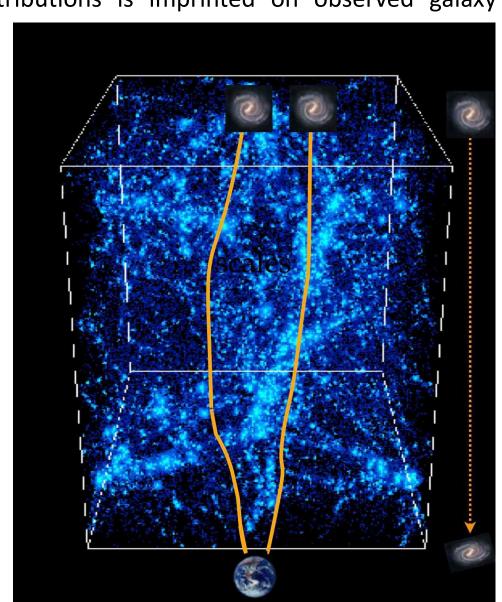
images

Sensitive to projected 2D mass distribution

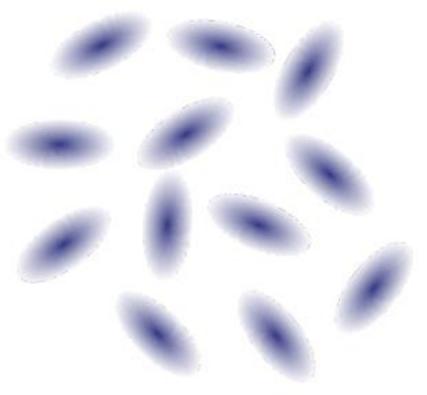
2 effects: magnification, distortions of images

few percent change of images. Need a statistical measurement and huge surveys to have enough statistics

Coherent distortions: measure correlation



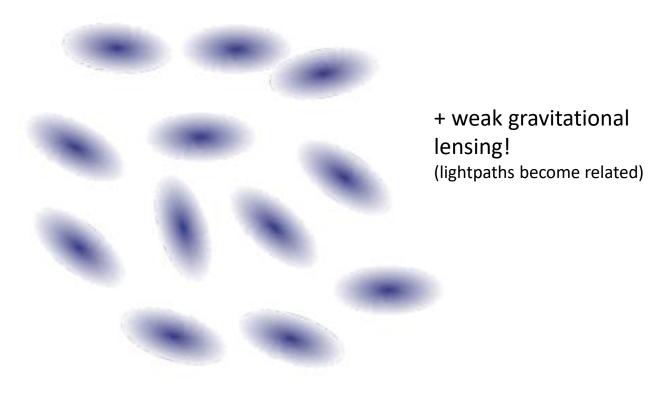
small patch on sky filled with (elliptical) galaxies (unrelated objects with different redshifts)



=> the average shape will be circular:

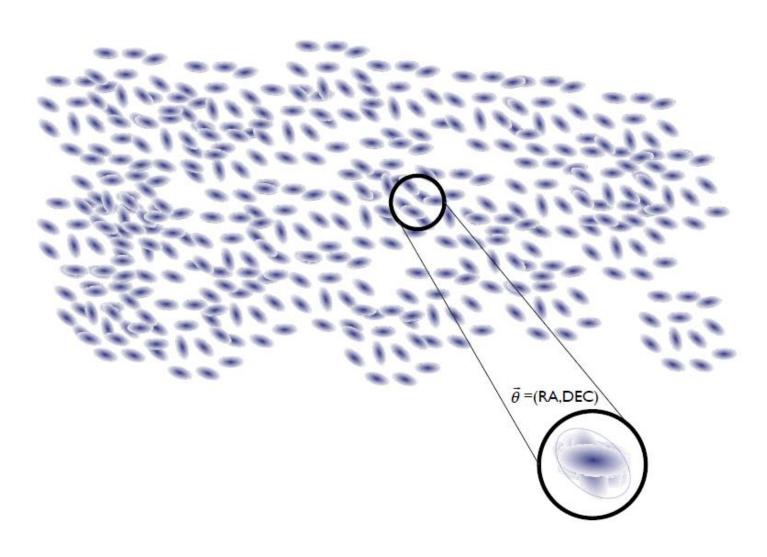


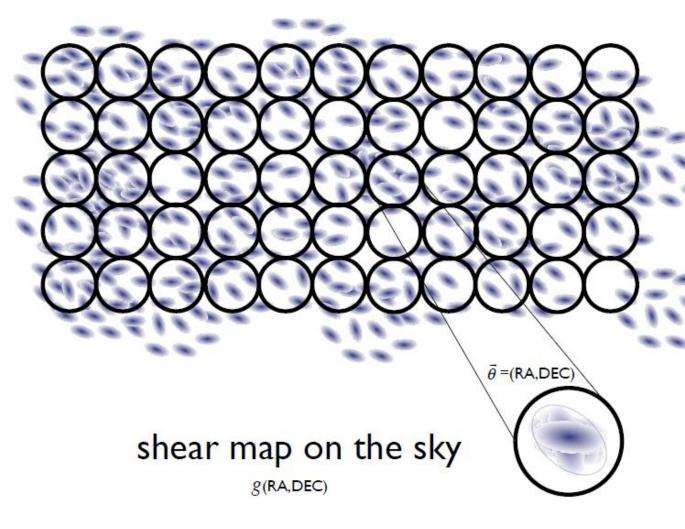
small patch on sky filled with (elliptical) galaxies (unrelated objects with different redshifts)



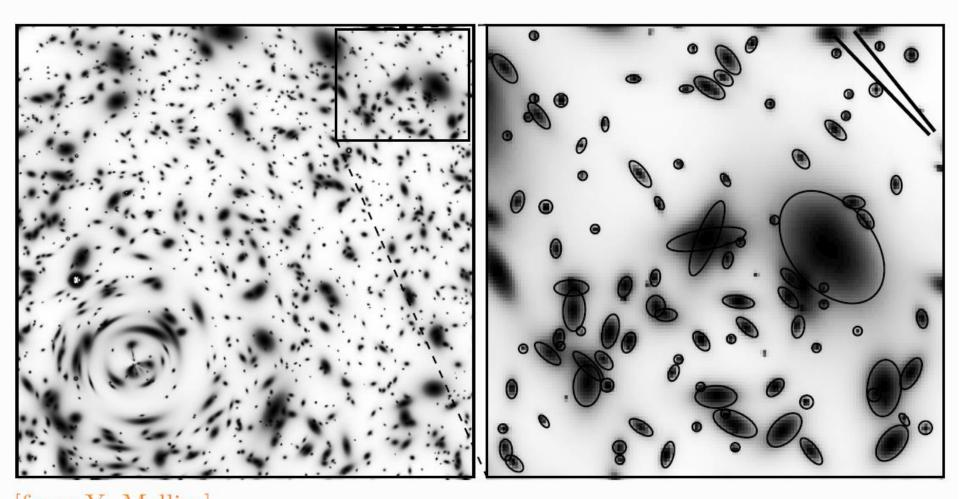
=> the average shape will be elliptical:







Ellipticity and local shear



[from Y. Mellier]
Galaxy ellipticities are an estimator of the local shear.



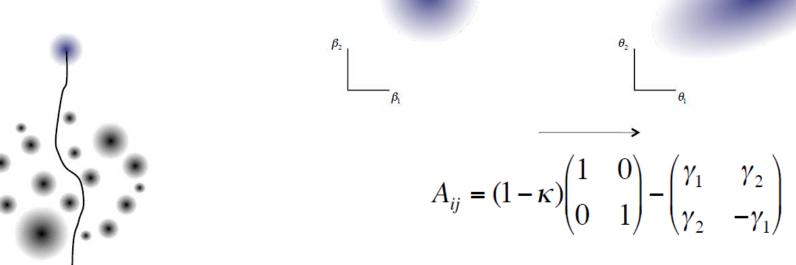


image distortion depends on...

...cosmic structure formation

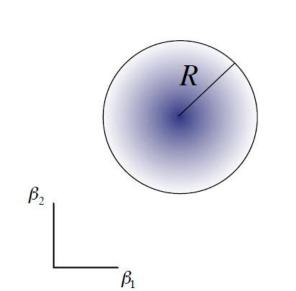
$$G(a) = \frac{5}{2} \Omega_0 \frac{\dot{a}}{a} \int_0^a \frac{1}{\dot{a}^3} da$$

...cosmic distance

$$D(z) = \frac{1}{1+z} \frac{c}{H_0} \int_0^z \frac{dz}{\left[\Omega_0 (1+z)^3 + \Omega_\Lambda\right]^{1/2}}$$

Great potential for cosmology

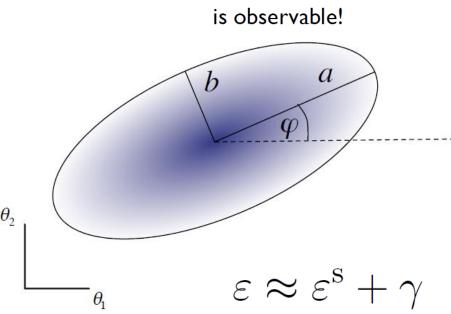
$$g = \frac{\gamma}{1 - \kappa} = \langle \varepsilon(\theta) \rangle$$



$$\gamma = |\gamma| e^{i2\varphi}$$

$$a = \frac{R}{1 - \kappa - |\gamma|}$$

$$b = \frac{R}{1 - \kappa + |\gamma|} \, \theta_2$$



circular source => measuring a, b (and φ) gives reduced shear $g=|\gamma|/(1-\kappa)$

$$A_{ij} = (1 - \kappa) \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} - \begin{pmatrix} \gamma_1 & \gamma_2 \\ \gamma_2 & -\gamma_1 \end{pmatrix}$$

If the original shape is not circular, the elipticity does not give the reduced shear

Weak lensing quantities are related:
$$\kappa(\boldsymbol{\theta}) - \kappa_0 = \frac{1}{\pi} \int \mathrm{Re} \Big[D^*(\boldsymbol{\theta} - \boldsymbol{\theta}') \gamma(\boldsymbol{\theta}') \Big] \, d^2 \boldsymbol{\theta}'$$

$$D(\boldsymbol{\theta} - \boldsymbol{\theta}') = \frac{\left((\theta_1 - \theta_1') + i(\theta_2 - \theta_2') \right)^2}{\left| \boldsymbol{\theta} - \boldsymbol{\theta}' \right|^4}$$

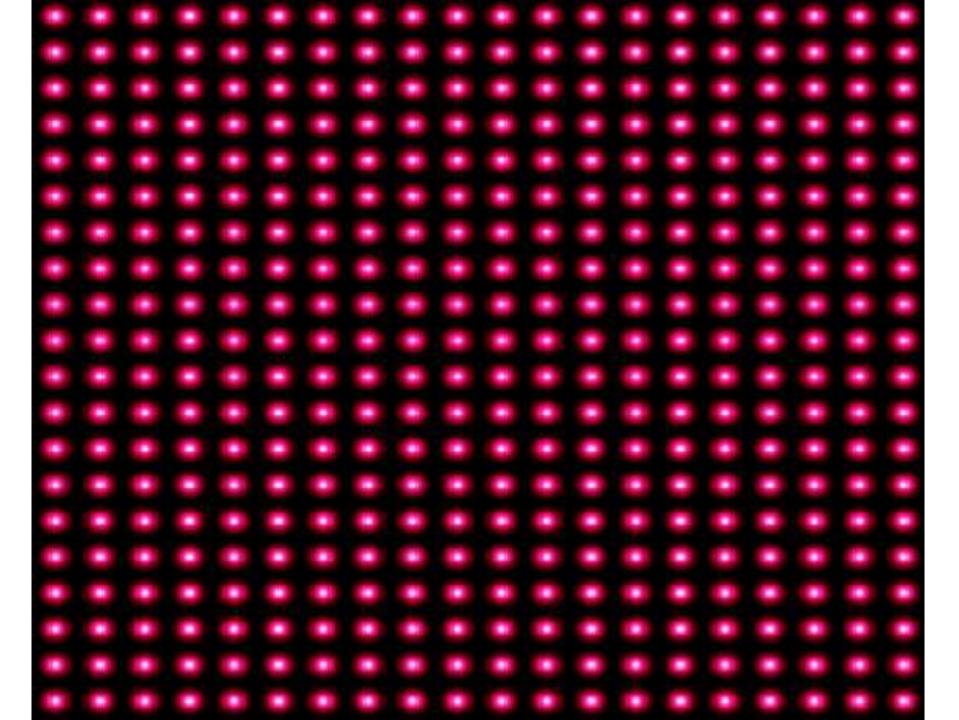
And related to cosmology:
$$\kappa(\theta) = \frac{3H_0^2\Omega_0}{2c^2} \int \frac{D_{LS}D_L}{D_S} \frac{\delta(\theta,z)}{a(z)} dz$$

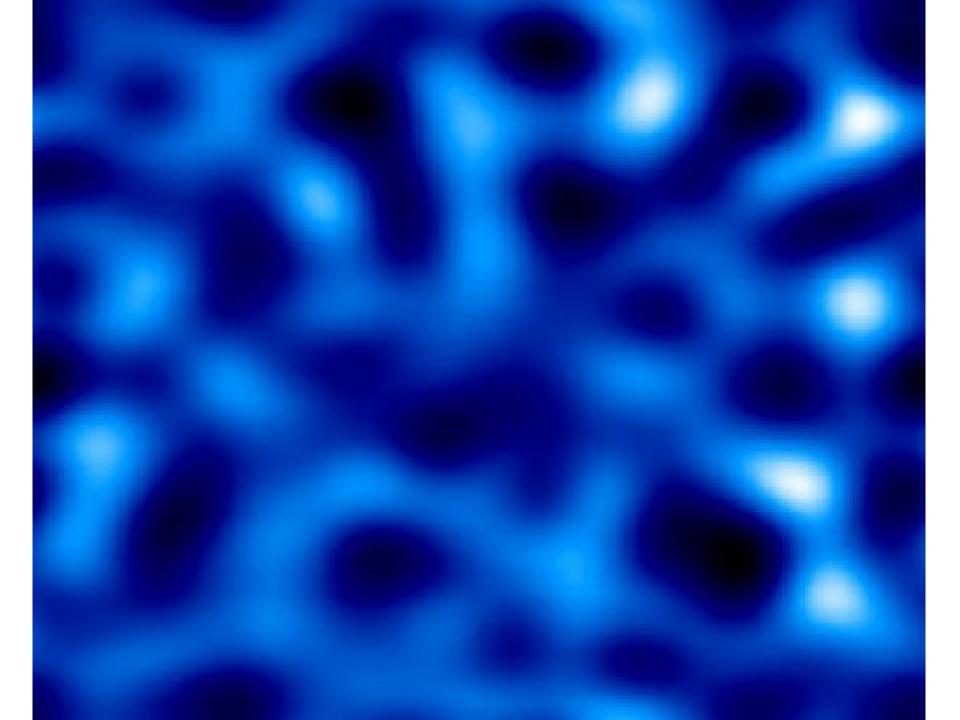
For a distribution of sources:

Geometry: Comoving distance to lens, source and scale factor

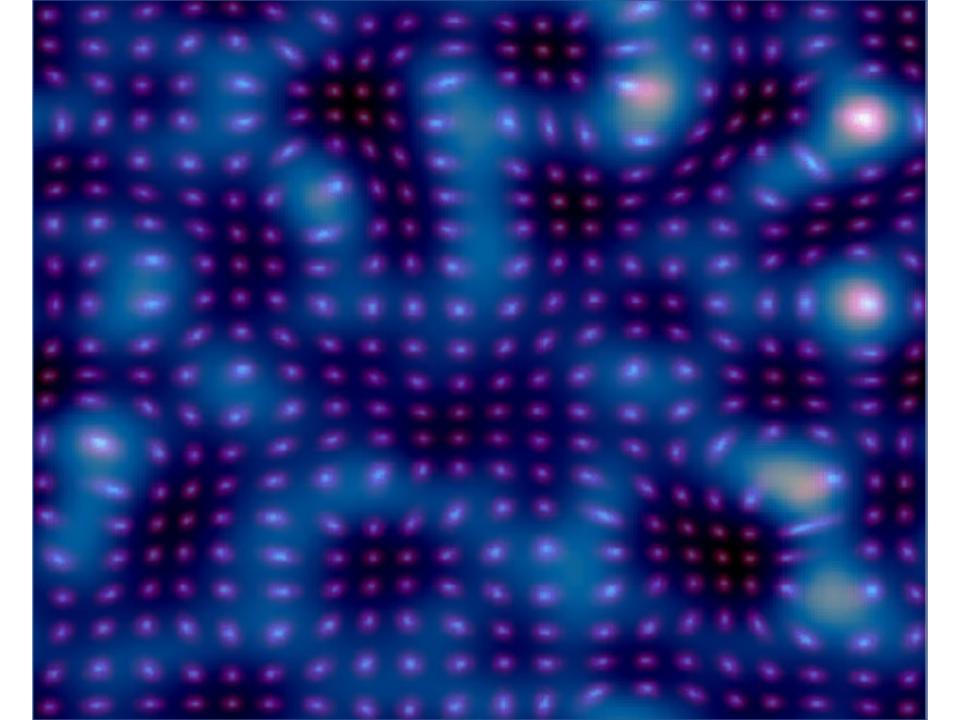
$$\kappa(\theta) = \frac{3H_0^2\Omega_0}{2c^2} \int n_s(z_s) \int \frac{D_{LS}D_L}{D_s} \frac{\delta(\theta, z)}{a(z)} dz dz_s$$

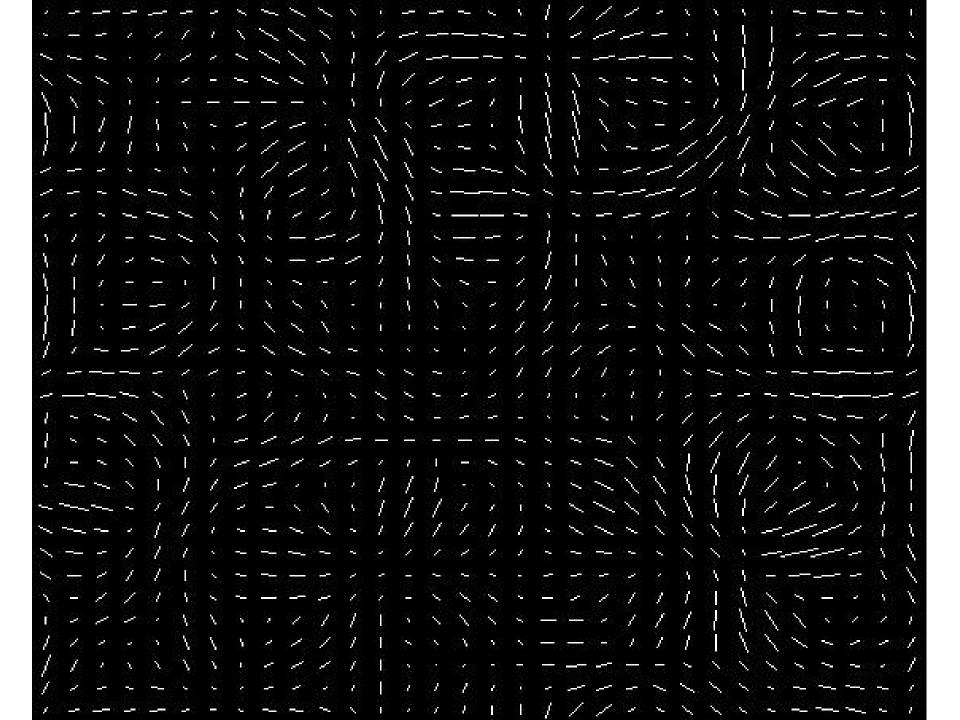
Growth of structure: Density contrast

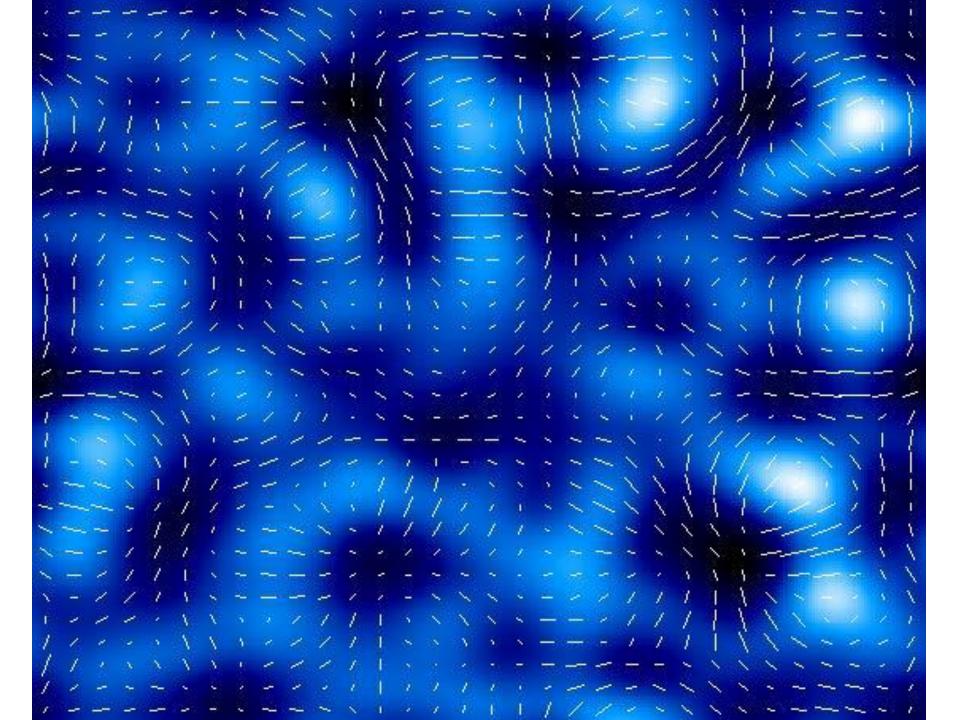


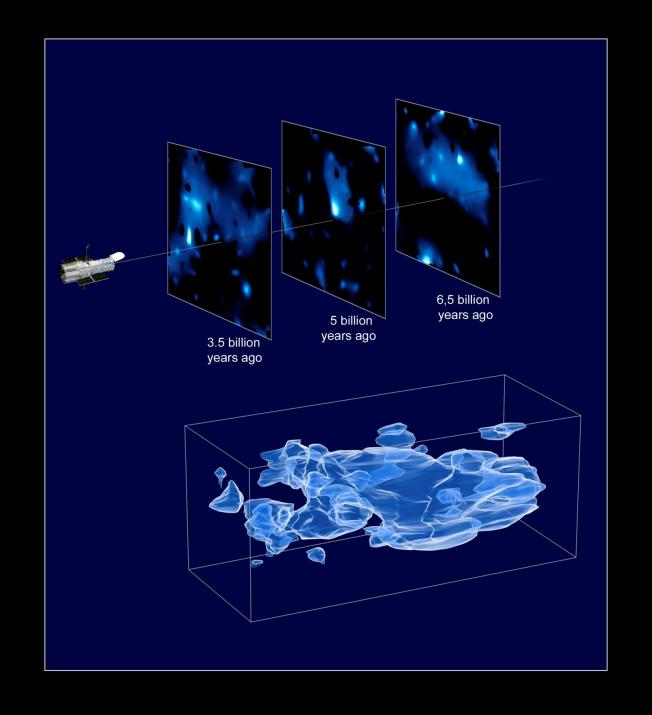


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The variance of convergence is related to the variance of the density contrast

Power spectrum of convergence and matter

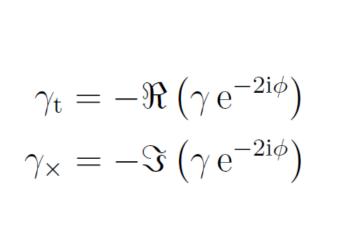
$$\langle \hat{\kappa}(\boldsymbol{\ell}) \hat{\kappa}^*(\boldsymbol{\ell}') \rangle = (2\pi)^2 \delta_{\mathrm{D}}(\boldsymbol{\ell} - \boldsymbol{\ell}') P_{\kappa}(\boldsymbol{\ell})$$
$$\langle \hat{\delta}(\boldsymbol{k}) \hat{\delta}^*(\boldsymbol{k}') \rangle = (2\pi)^3 \delta_{\mathrm{D}}(\boldsymbol{k} - \boldsymbol{k}') P_{\delta}(k)$$

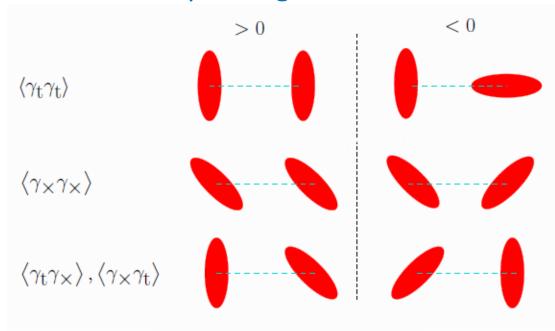
Related between them and related to cosmology (Limber's equation)

$$P_{\kappa}(\ell) = \int d\chi \, G^{2}(\chi) P_{\delta} \left(k = \frac{\ell}{\chi} \right)$$

In the small angle approximation and assuming that the power spectrum varies slowly

Cosmic shear: Correlations of shears at two points give us 4 functions





Robustness test: The cross correlations must be null $\rightarrow \langle \gamma_t \gamma_\times \rangle = \langle \gamma_\times \gamma_t \rangle = 0$ If they are not, this is a clear sign of a systematic error in your analysis.

Finally the 2 correlation functions that are used for cosmic shear are

defined as:

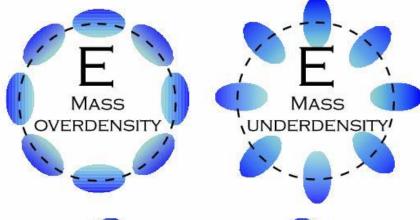
$$\xi_{+}(\vartheta) = \langle \gamma_{t} \gamma_{t} \rangle (\vartheta) + \langle \gamma_{\times} \gamma_{\times} \rangle (\vartheta)$$

$$\xi_{-}(\vartheta) = \langle \gamma_{t} \gamma_{t} \rangle (\vartheta) - \langle \gamma_{\times} \gamma_{\times} \rangle (\vartheta)$$

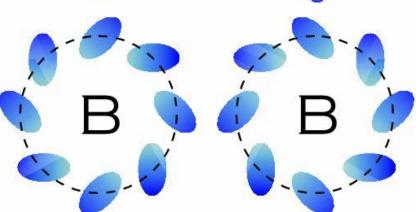
The cosmic shear correlation functions are related to cosmological parameters

$$\xi_{+}(\theta) = \frac{1}{2\pi} \int_{0}^{\infty} d\ell \, \ell J_{0}(\ell \theta) P_{\kappa}(\ell)$$

$$\xi_{-}(\theta) = \frac{1}{2\pi} \int_{0}^{\infty} d\ell \, \ell J_{4}(\ell \theta) P_{\kappa}(\ell),$$

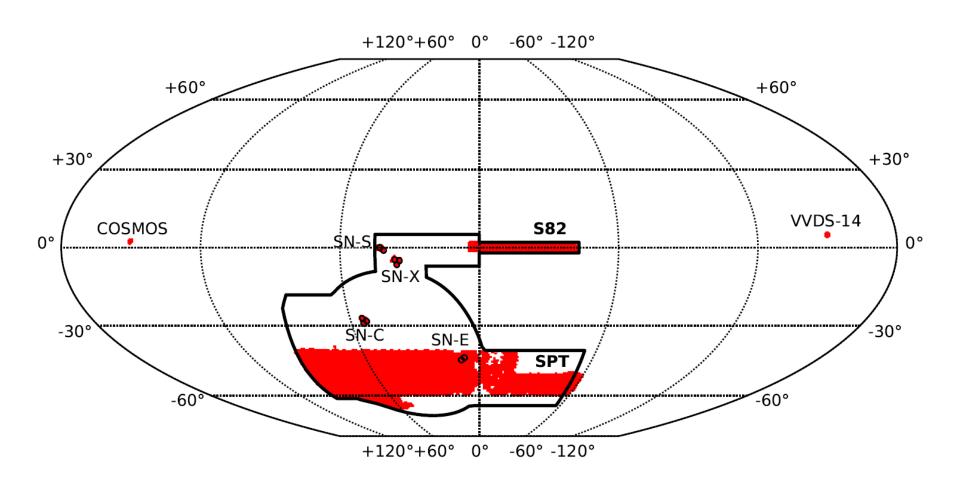


Tangential pattern is due to mass overdensity Radial pattern is due to underdensities



No other patterns are posible for the shear field. A so-called B-mode is not generated

Example: Cosmology from clustering AND weak lensing from DES Y1 Data



The Dark Energy Survey



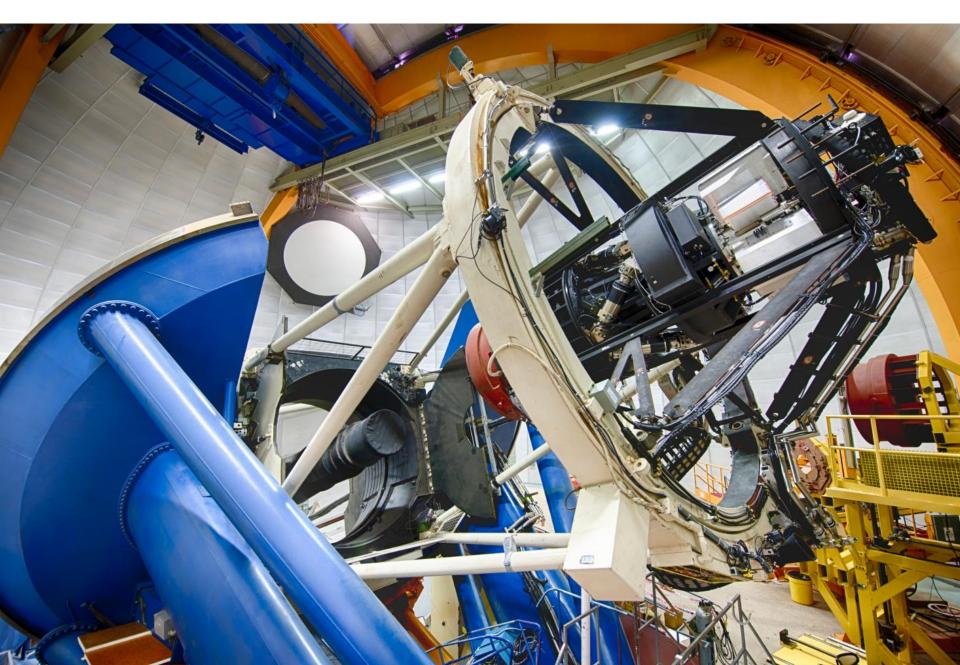
Optical/IR imaging survey with the Blanco 4m telescope at Cerro Tololo Inter-American Observatory(CTIO) in Chile

5000 sq-deg (1/8 of the sky) in grizY bands (2500 sq-deg overlapping with SPT survey) + 30 sq-deg time-domain griz (SNe)

Up to $i_{AB} \sim 24$ th magnitude at 10 σ (z \sim 1.5)

570 Mpx camera with 3 sq-deg FoV, DECam

Installed on Blanco since 2012



NGC 1365

NGC 1365 (the Great Barred Spiral Galaxy) is a barred spiral galaxy about 56 million lightyears away in the constellation Fornax. (DECam, DES Collaboration)

NGC 1566

NGC 1566 (the Spanish Dancer) is a spiral galaxy in the constellation Dorado. (DECam, DES Collaboration)



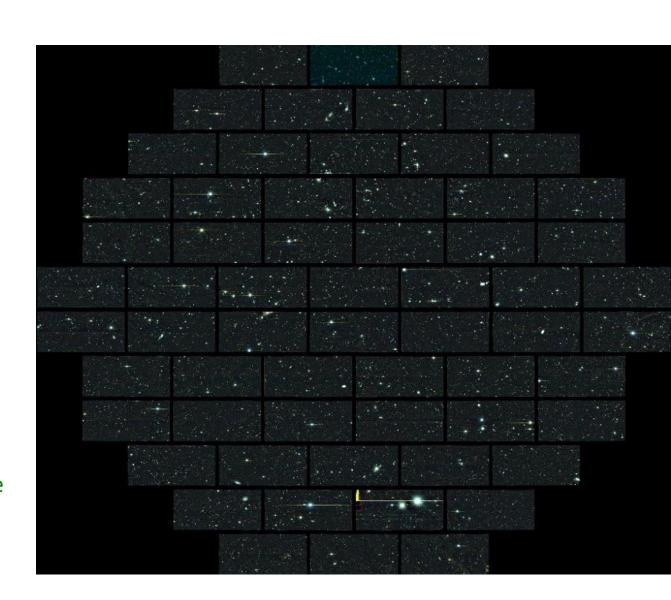
DECam

74 CCD chips (570 Mpx/image) (62 2kx4k image, 8 2kx2k alignment/focus, 4 2kx2k guiding)

Red Sensitive CCDs QE>50% @ 1000 nm 250 microns thick

3 sq-deg FoV Excellent image quality 0.27''/pixel

Low noise electronics (<15 e @ 250 kpx/s)



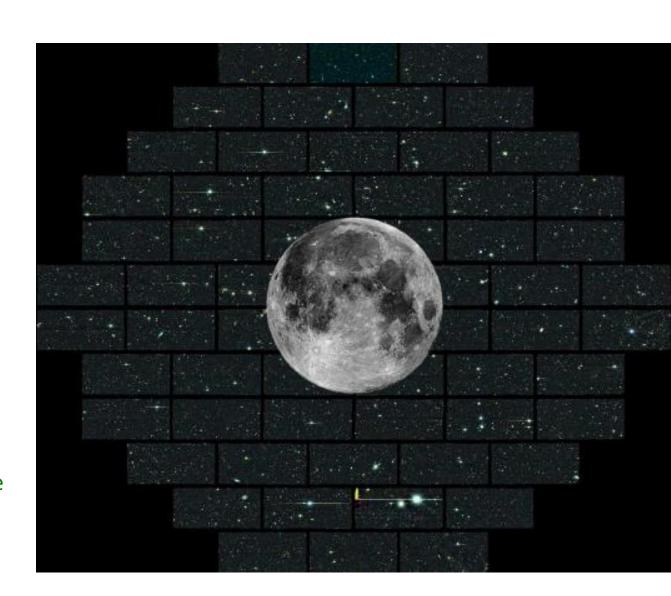
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DES Science Summary

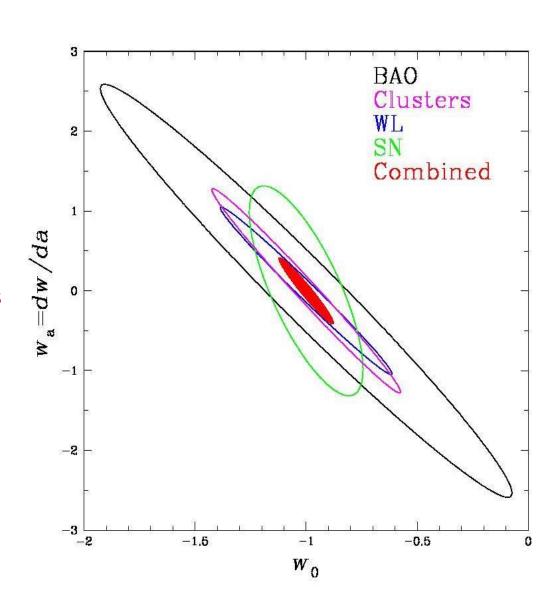
4 Probes of Dark Energy

Galaxy Clusters (dist & struct)
Tens of thousands of clusters to z~1
Synergy with SPT, VHS

Weak Lensing (dist & struct)
Shape and magnification measurements
of 200 million galaxies

Baryon Acoustic Oscillations (dist) 300 million galaxies to z~1.4

Supernovae (dist) 3500 well-sampled Sne Ia to z~1



DES Science summary

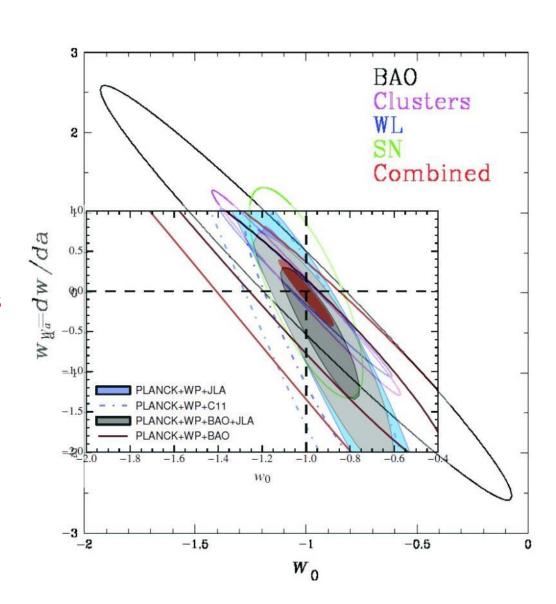
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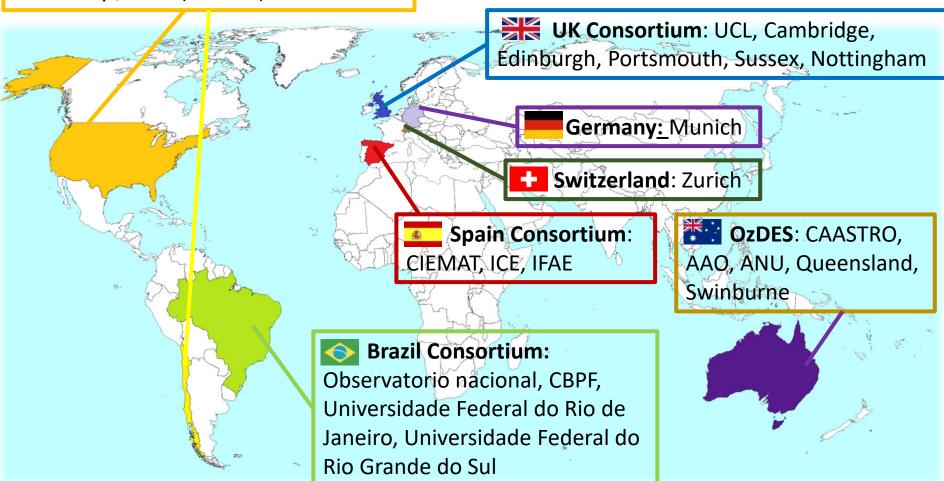


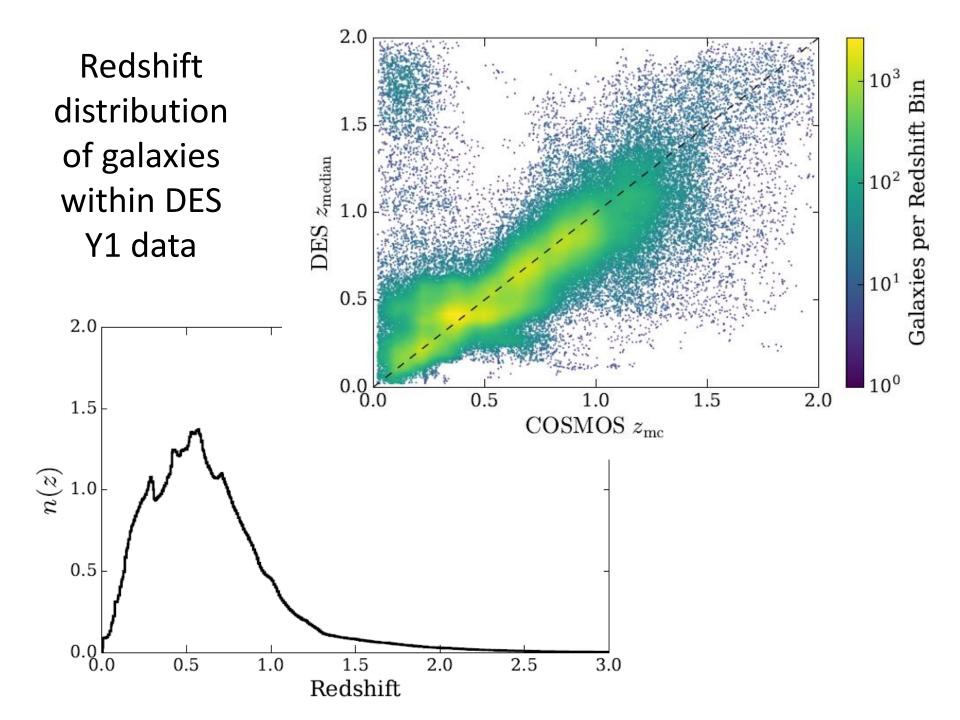
USA:_Fermilab, UIUC/NCSA,
University of Chicago, LBNL, NOAO,
University of Michigan, University of
pennsylvania, Argonne National
Laboratory, Ohio State University, Santa
Cruz/SLAC Consortium, Texas A&M
University, CTIO (in Chile)

DES Collaboration

~500 scientists from
25 institutions in 7 countries
darkenergysurvey.org
Facebook.com/darkenergysurvey



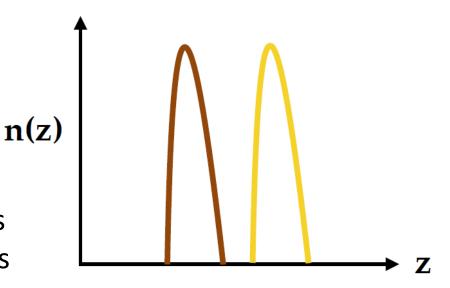


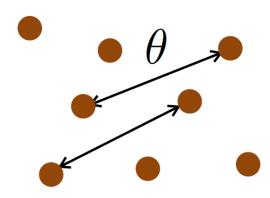


2 samples of galaxies: "lens" and "sources"

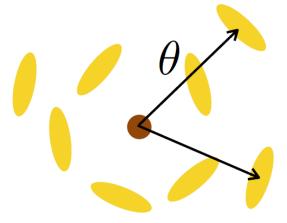
Combine the auto and cross-correlation of

- 1. positions of the lens galaxies
- 2. **shapes** of the source galaxies

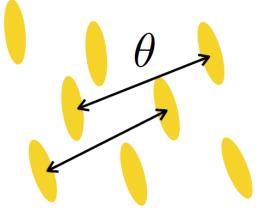




Galaxy clustering



Galaxy-galaxy lensing

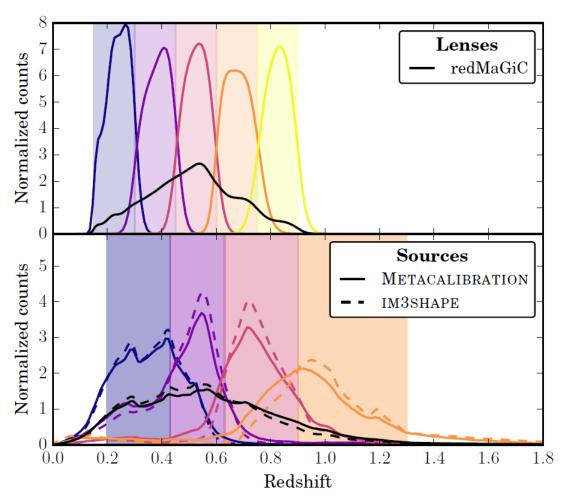


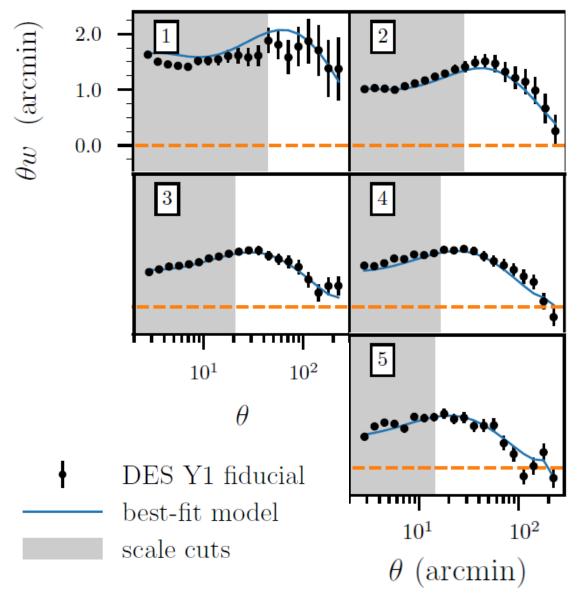
Cosmic shear

This is a very demanding measurement:

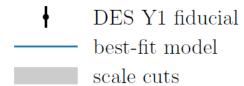
- Manage a large dataset
- Compute correlation functions (3 types)
- These measurements are not independent

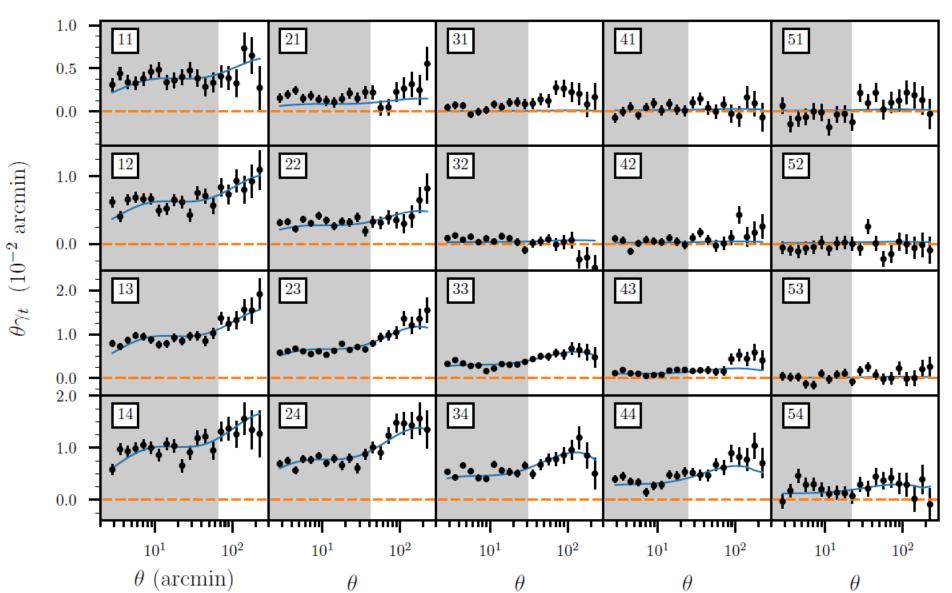
 Compute and verify the covariance matrix

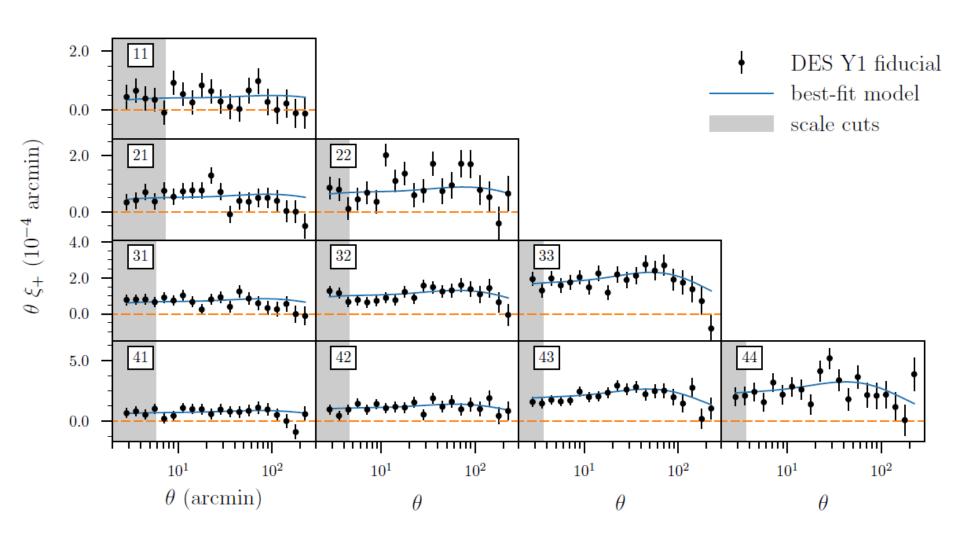


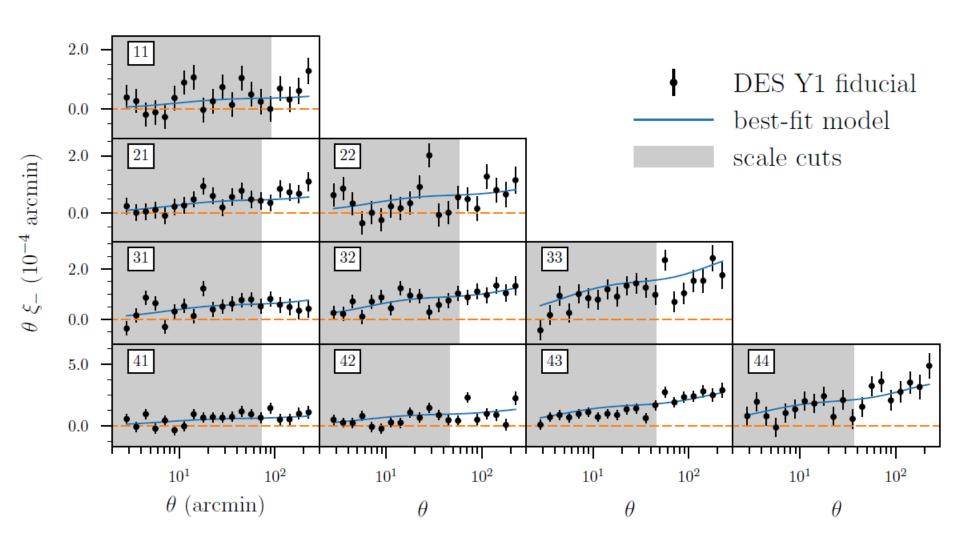


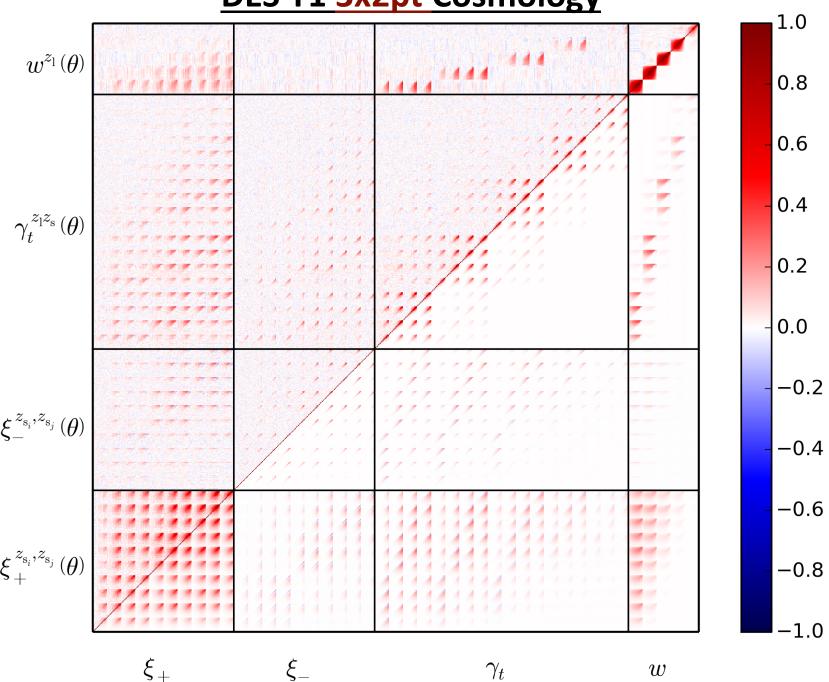
Lens density correlation functions for each redshift bin











$$w^{i}(\theta) = (b^{i})^{2} \int \frac{dl \, l}{2\pi} J_{0}(l\theta) \int d\chi$$
$$\times \frac{\left[n_{1}^{i}(z(\chi))\right]^{2}}{\chi^{2} H(z)} P_{NL} \left(\frac{l+1/2}{\chi}, z(\chi)\right)$$

Galaxy Clustering Correlation position- position

$$\gamma_{t}^{ij}(\theta) = b^{i}(1+m^{j}) \int \frac{dl \, l}{2\pi} J_{2}(l\theta) \int d\chi n_{l}^{i}(z(\chi))$$
$$\times \frac{q_{s}^{j}(\chi)}{H(z)\chi^{2}} P_{NL}\left(\frac{l+1/2}{\chi}, z(\chi)\right)$$

Galaxy-Glaxy Lensing Correlation position-shape

$$q_s^i(\chi) = \frac{3\Omega_m H_0^2}{2} \frac{\chi}{a(\chi)} \int_{\chi}^{\chi(z=\infty)} d\chi' n_s^i(z(\chi')) \frac{dz}{d\chi'} \frac{\chi' - \chi}{\chi'}$$
(IV.3)

$$\xi_{+/-}^{ij}(\theta) = (1 + m^{i})(1 + m^{j}) \int \frac{dl \, l}{2\pi} J_{0/4}(l\theta) \int d\chi$$
$$\times \frac{q_{s}^{i}(\chi)q_{s}^{j}(\chi)}{\chi^{2}} P_{\rm NL}\left(\frac{l + 1/2}{\chi}, z(\chi)\right)$$

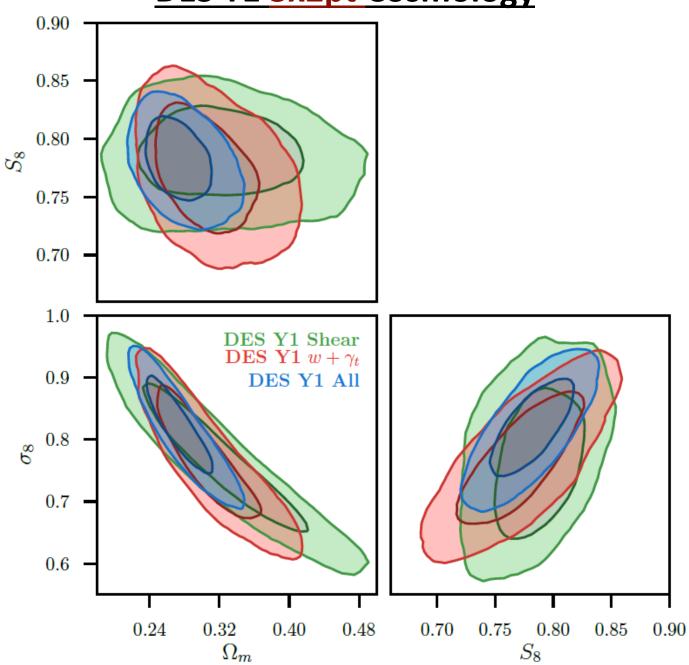
Cosmic Shear Correlation shape-shape

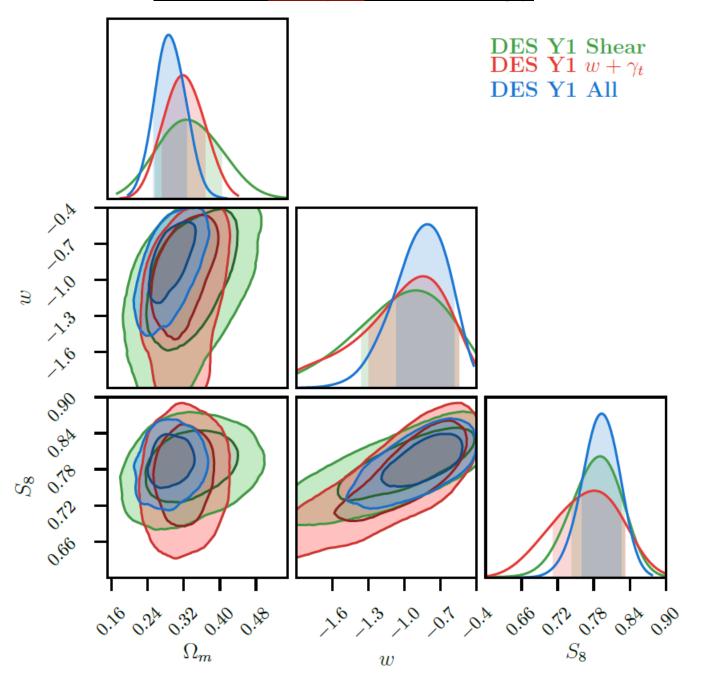
How to decide if ΛCDM (or any other theory) describes the data: The Likelihood function

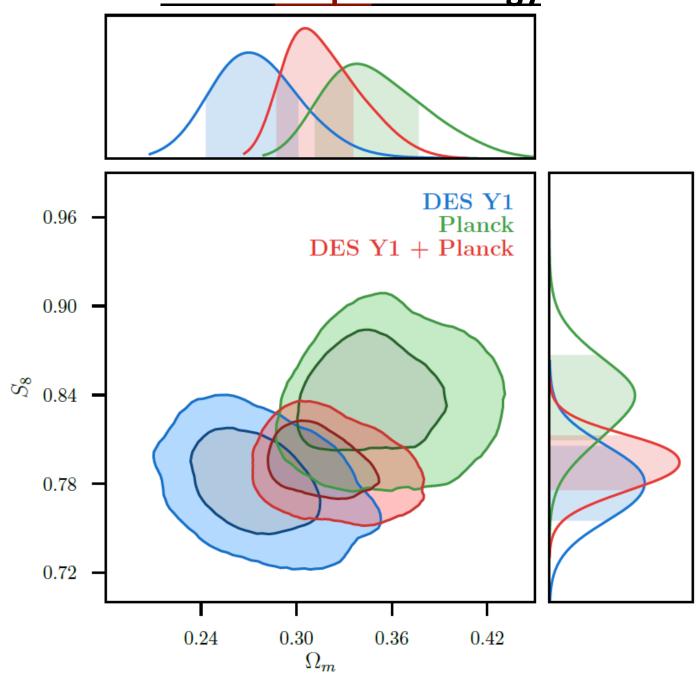
$$\ln \mathcal{L}(\vec{p}) = -\frac{1}{2} \sum_{ij} [D_i - T_i(\vec{p})] C^{-1}_{ij} [D_j - T_j(\vec{p})]$$

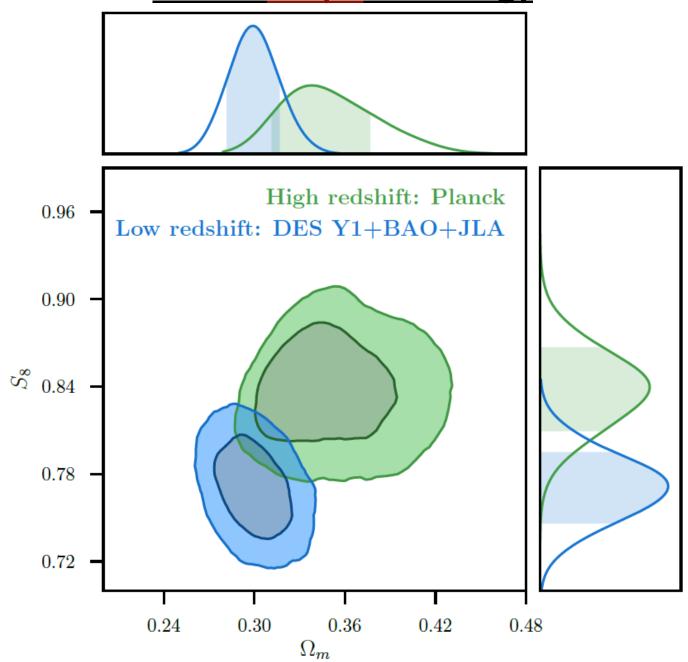
Derived Parameters: S8 to minimize correlations between original parameters

$$S_8 \equiv \sigma_8 \left(\frac{\Omega_m}{0.3}\right)^{0.5}$$

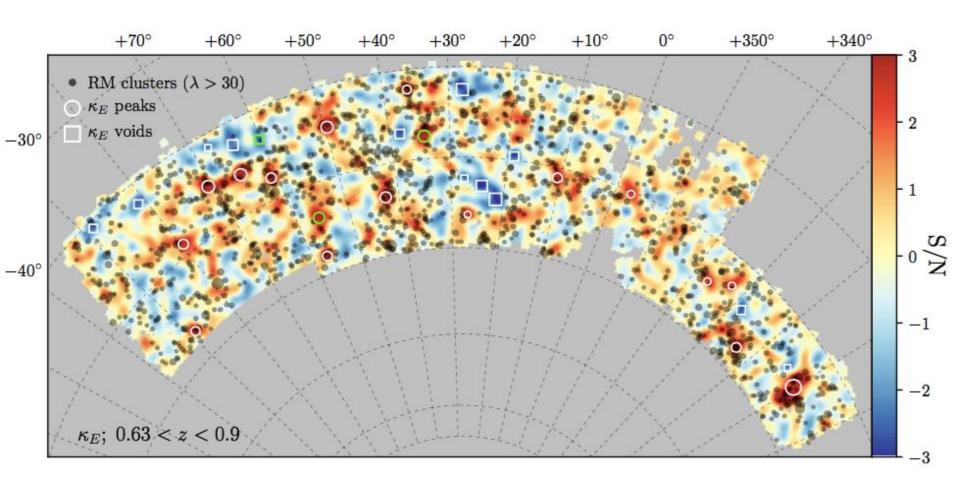






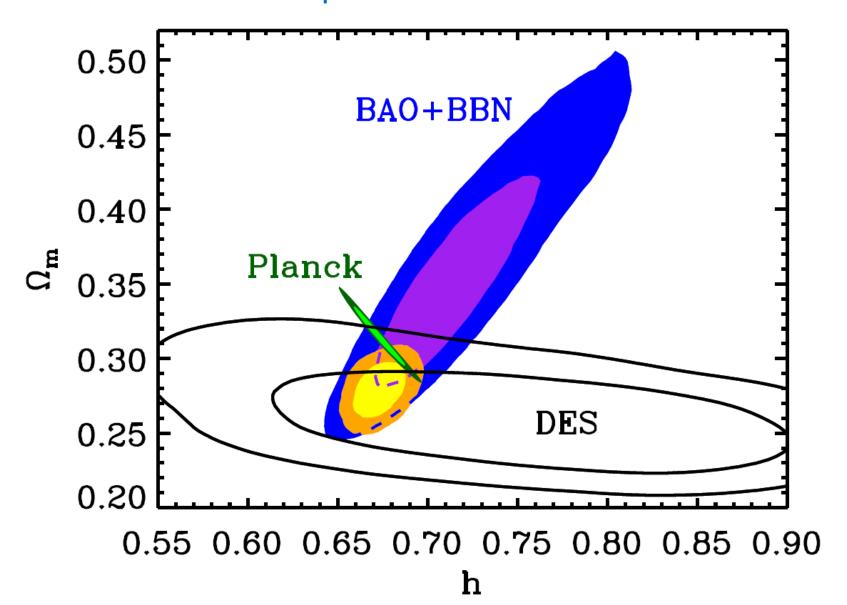


Using the weak gravitational lensing it is posible to build a map of matter (all, including the dark matter) in the Universe



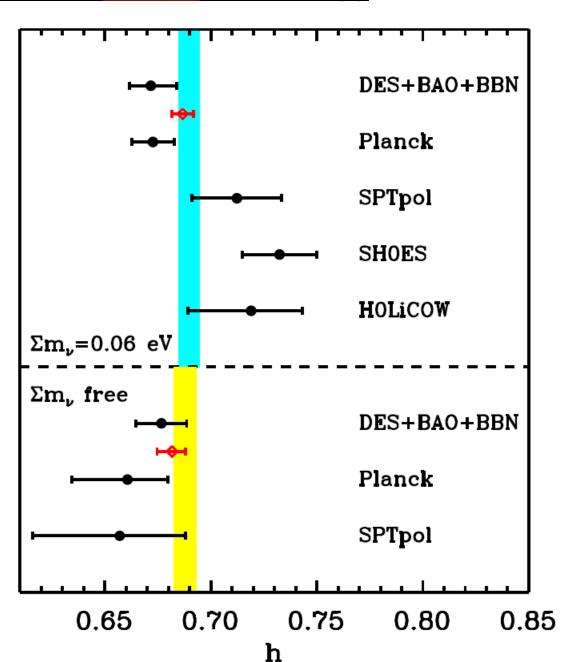
Other Results; Hubble parameter measurement combining BAO, BBN and DES 3x2pt.

Independent determination



No significant tensión found in the measurements

... yet?



Future Projects: DESI



DESI (Dark Energy Spectroscopic Instrument)



A new corrector for the Mayall telescope at Kitt Peak (8 deg² FOV)

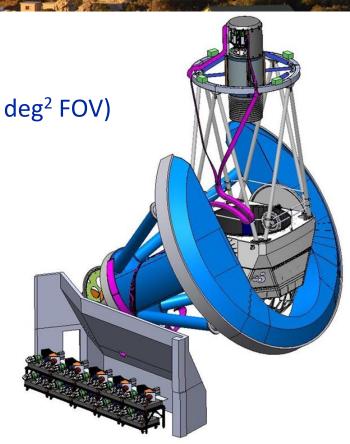
A new top ring, barrel and hexapod

A focal plane with 5000 robots fiber positioner

10 espectrographs, following the BOSS design

Instrument control and data proccess systems

DESI will start the data taking in 2019



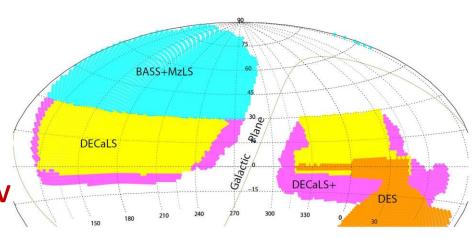
Future Projects: DESI

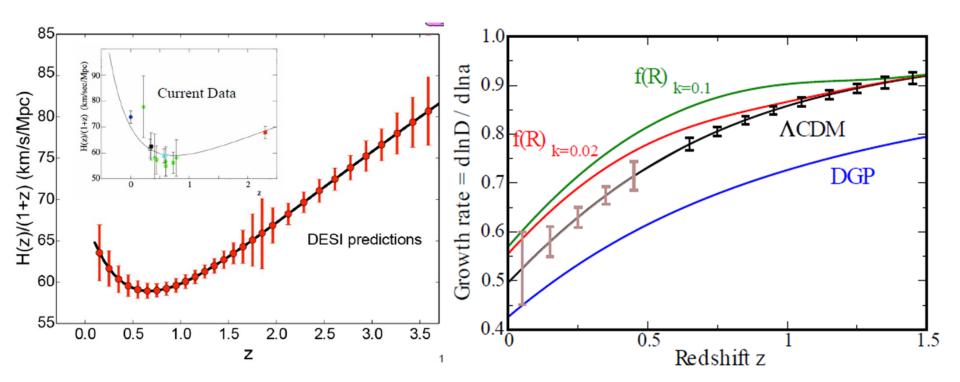
Scientific potential

Distances with BAO better than 0.3%

Growth factor better than 1% → GR test

Sum of neutrino masses better than 20 meV





Future Projects: Euclid & LSST



FoM ~ 1500 , -4000 (all)

Main probes: WL & Galaxie clustering (BAO,RSD) (spectro))

European lead project / ESA

Participation of NASA

~ 1000 members

Space telescope / 1.2 m mirror

Launch: Q4 2020

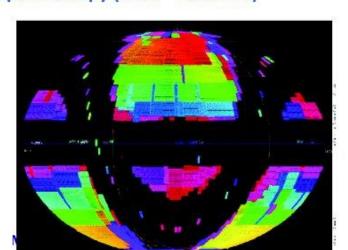
Mission length: 6 years

1 exposure depth: 24 mag

Survey Area: 15 000 sq deg (.36 sky)

Filters: 1 Visible(550-900nm)+ 3 IR (920-2000 nm) + NIR

spectroscopy (1100 - 2000 nm)





FoM > 800

Main probes: WL, CL, SN, BAO (photo)...

US lead project / NSF-DOE

Participation of France/In2P3

~ 450 Core members + 450 to come

Ground Telescope / 6.5 m effective mirror

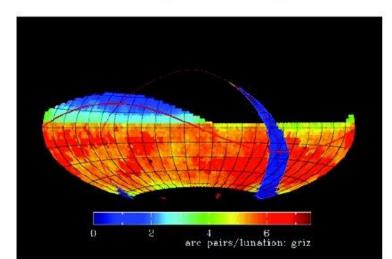
1st light: 2021

Observation length: 10 years

1 exposure depth: 24 mag (i)

Survey Area: 20 000 sq dg (.48 sky)

Filters: 6 filters (320-1070 nm)



Conclusions

Cosmology is in a golden era

All current data are consistent with Λ CDM: ~70% cosmological constant, ~25% of dark matter (of unknown nature) and ~5% of ordinary matter

Some open problems that affect the whole picture of physics: dark energy, dark matter, inflation, baryogenesis \rightarrow Require new physics

Probing the expansión history of the Universe and the growth of structure with much better precisión can provide a strong boost to the current knowledge

A number of large projects are under way or planned for the future, and hopefully, will bring significant progress

Dark matter, dark energy, baryogenesis and inflation are very important questions both for cosmology and for particle physics, since the unveiling of their physical nature can bring us to a revolution in our understanding of the cosmos