

Studying heavy-ion collisions using a hybrid model



GRANT:2017/05685-2

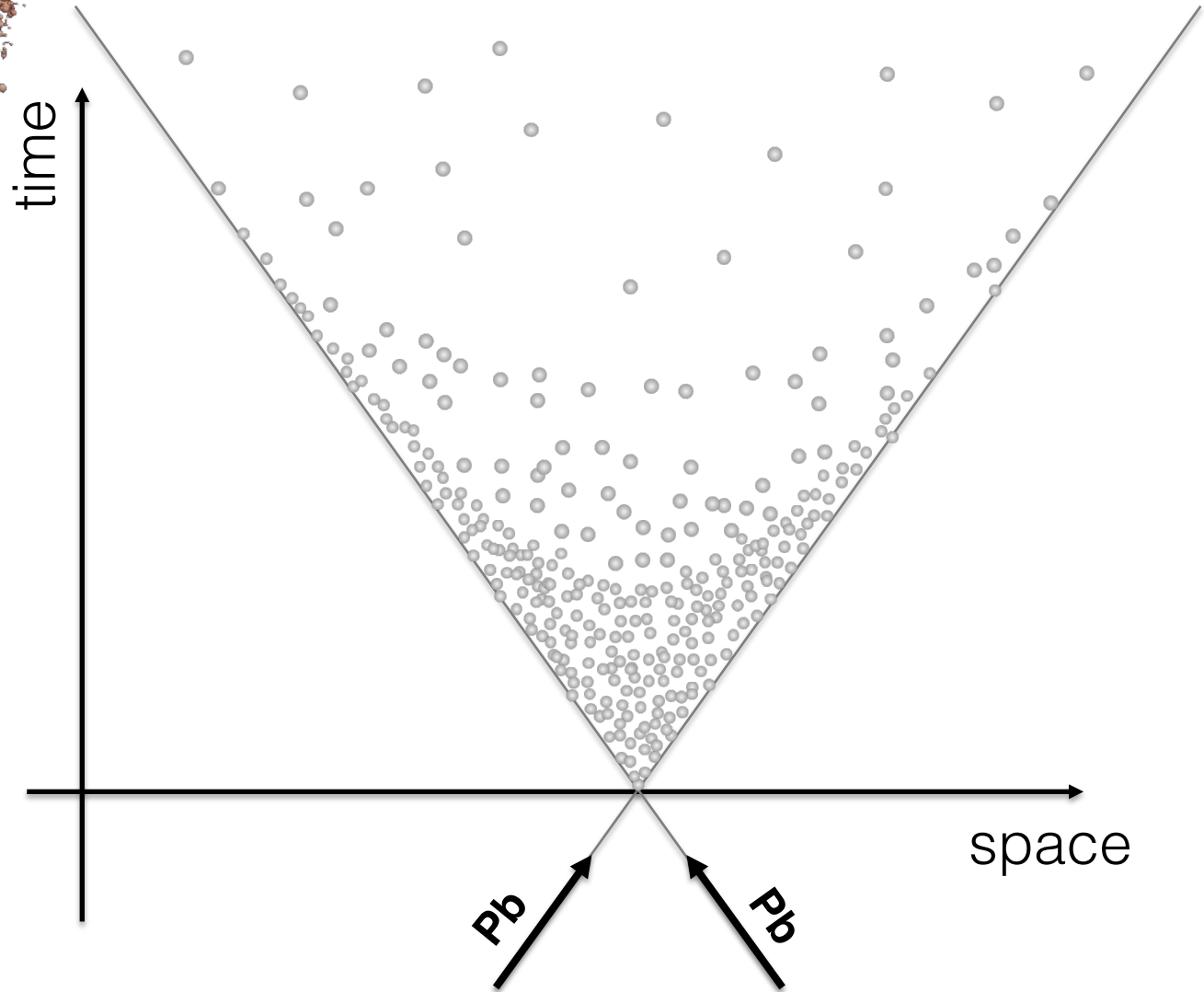
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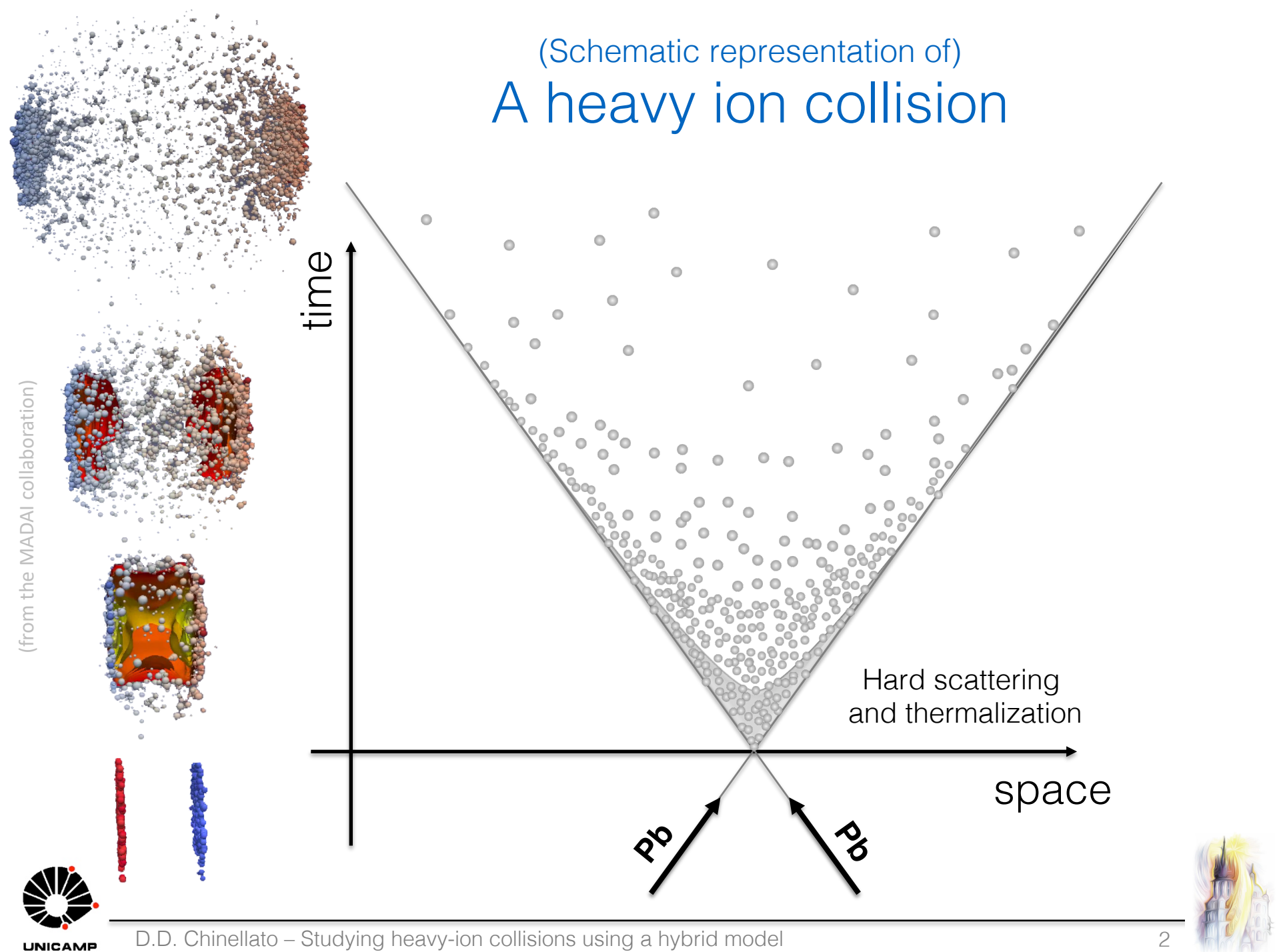
² - Universidade de São Paulo, São Paulo, Brazil

(Schematic representation of) A heavy ion collision

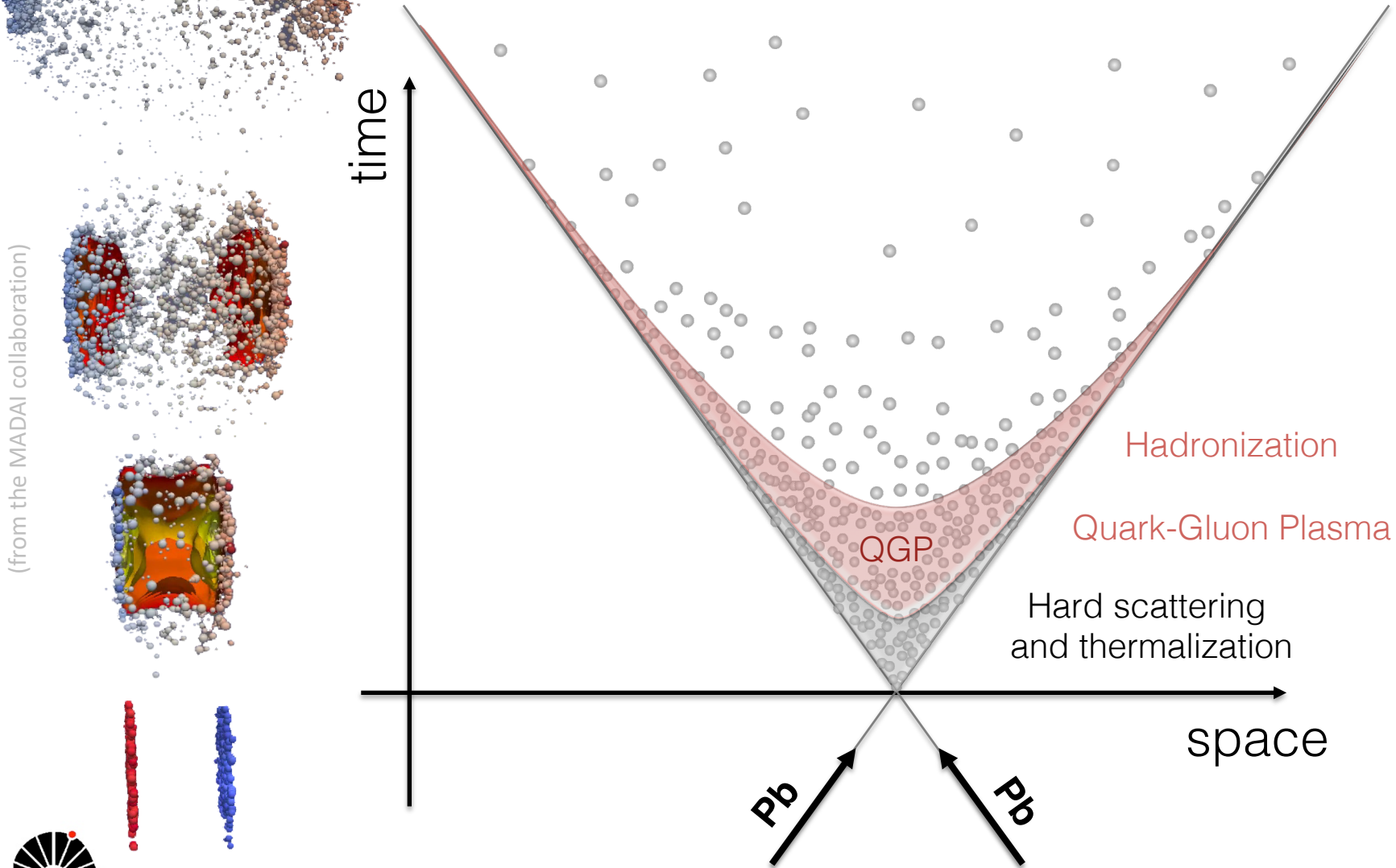
(from the MADAL collaboration)



(Schematic representation of) A heavy ion collision

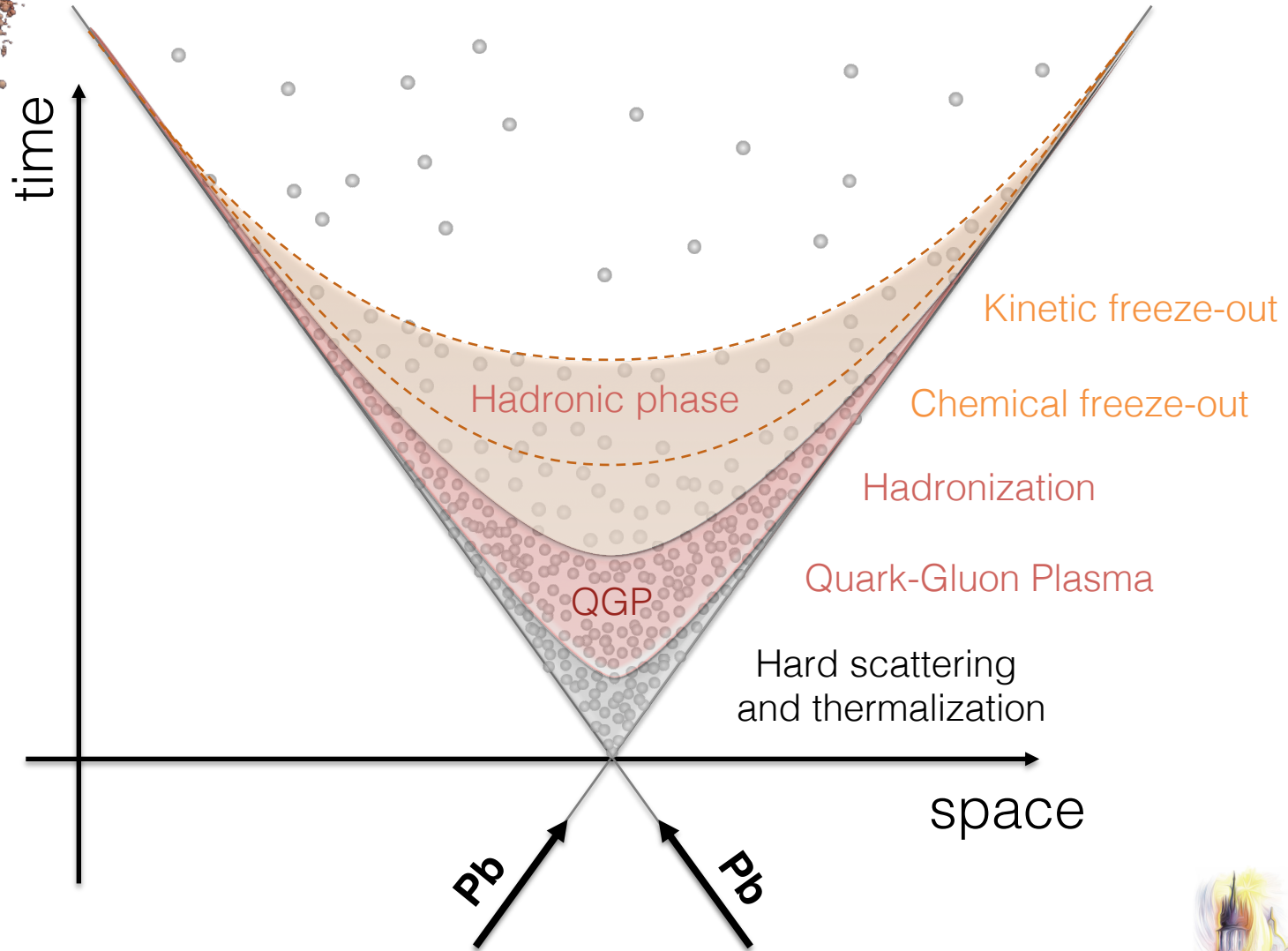


(Schematic representation of) A heavy ion collision

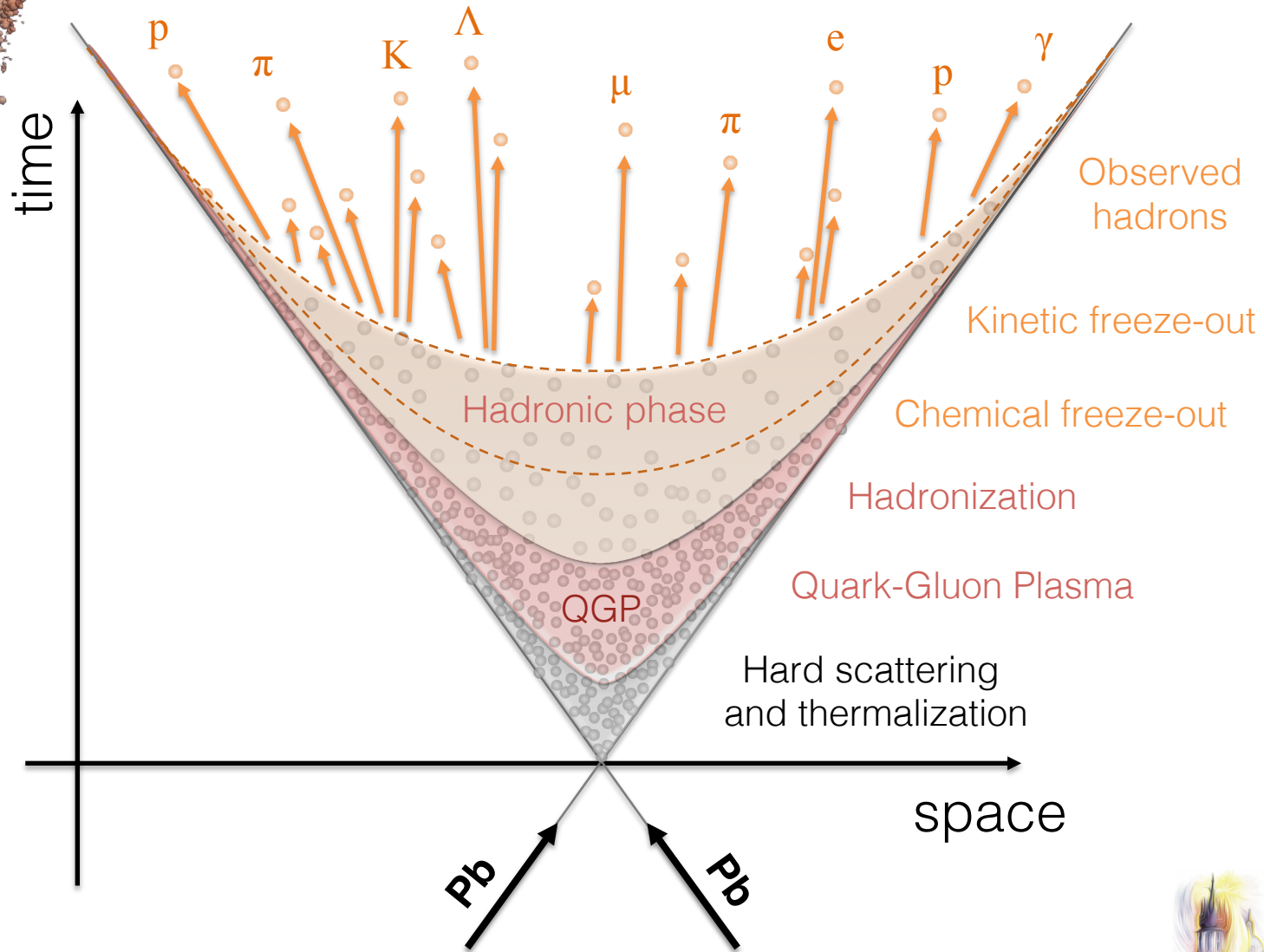


(Schematic representation of) A heavy ion collision

(from the MADAL collaboration)



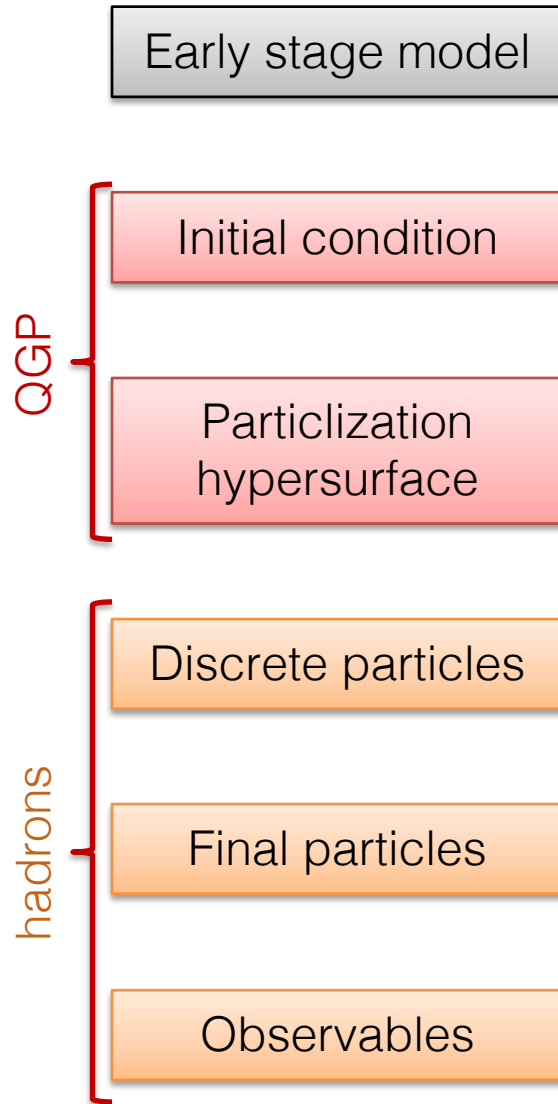
(Schematic representation of) A heavy ion collision



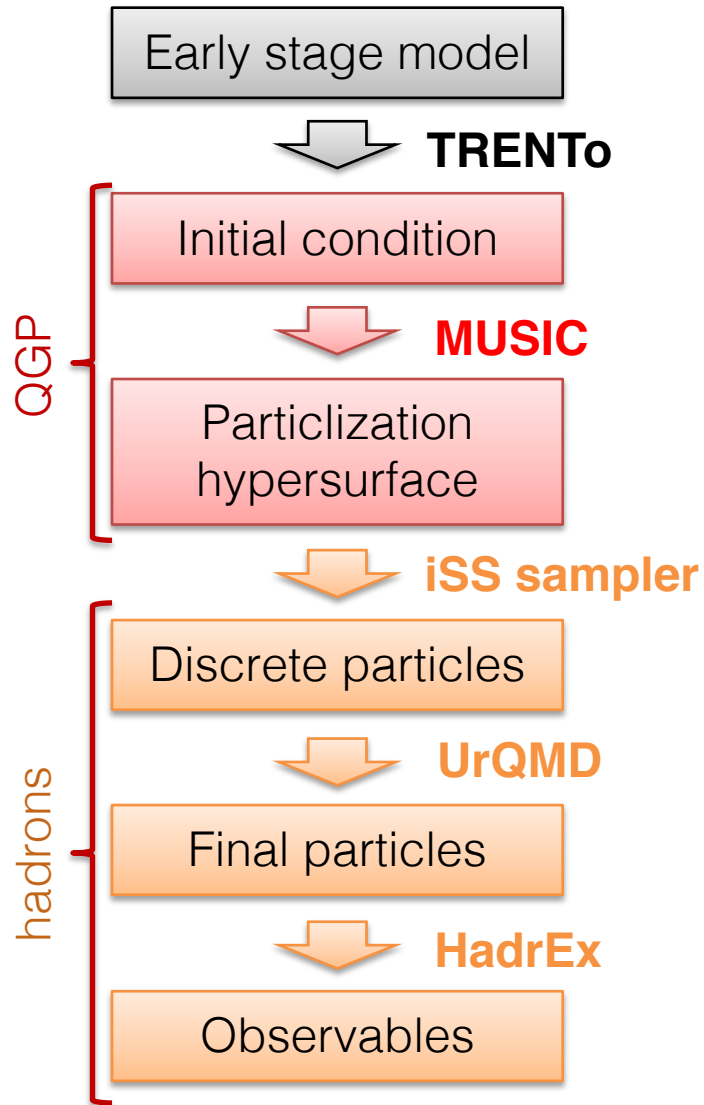
(from the MADAL collaboration)



Simulating a heavy ion collision: hybrid model



Simulating a heavy ion collision: hybrid model



- ← **TRENTo** [1]: initial condition generator
- ← **MUSIC** [2]: 3+1 hydrodynamics for the evolution of the QGP phase
- ← **iSS sampler** [3]: thermal production of hadrons from freezeout hypersurface
- ← **UrQMD** [4]: hadronic cascade simulator: scattering and resonance decays
- ← **HadrEx**: a convenient general-purpose analysis framework

[1] <http://qcd.phy.duke.edu/trento/>

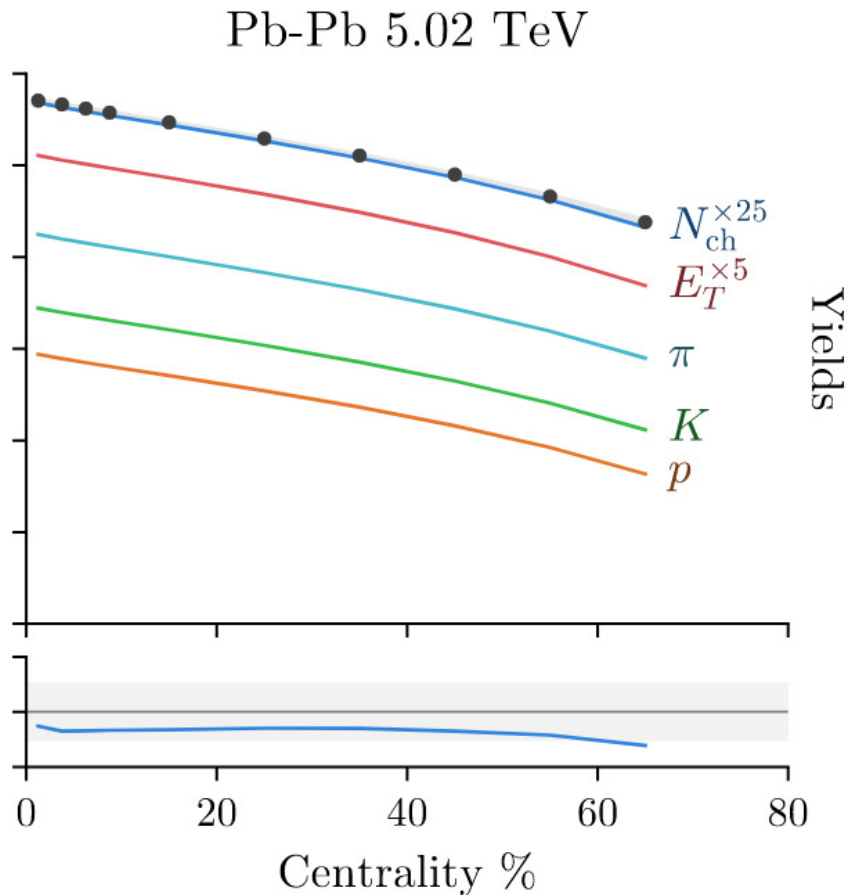
[2] <http://www.physics.mcgill.ca/music/>

[3] <https://github.com/chunshen1987/iSS>

[4] <https://urqmd.org/>



Configuring the chain

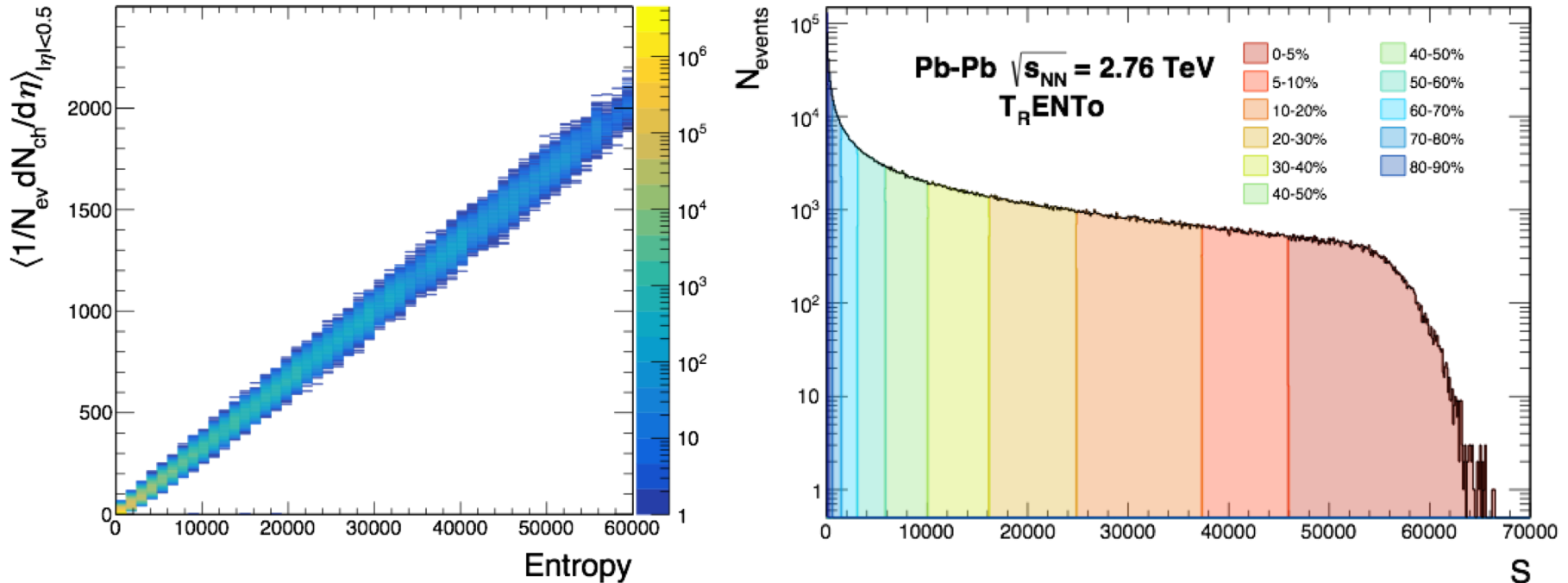


- ← TRENTo + Free Streaming + VISH2+1 + FRZOUT + UrQMD (by the Duke group [1]): obtained optimal a posteriori parameters
- We utilize these parameters but with a different overall normalization
- Minor differences in the two approaches under study

[1] Nuc.Phys.A, 967 (67-73)



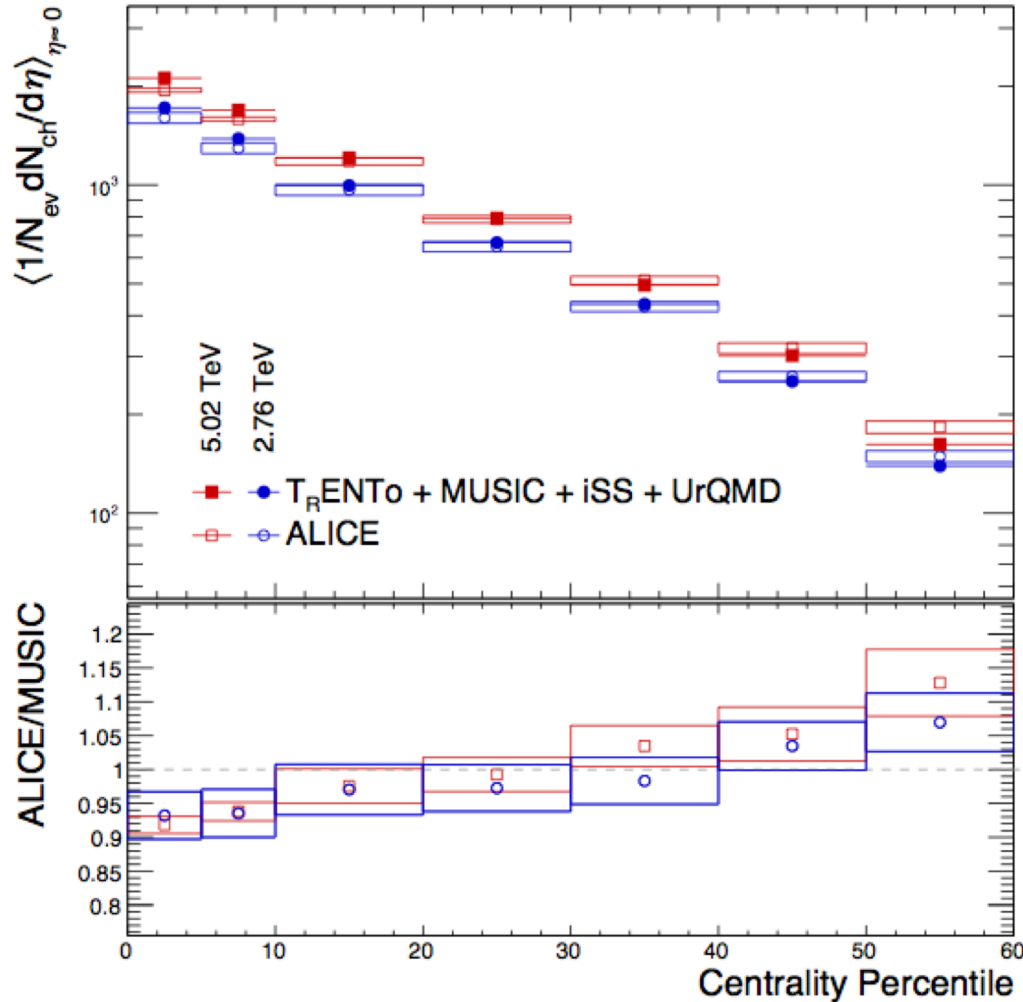
Centrality determination



- **Strongly correlated:** Initial entropy S and final charged-particle multiplicity
- Centrality calibration based on **a sample of 10^6 TRENTo initial conditions** and entropy classification



Charged-particle multiplicity density



- ← Description **acceptable within uncertainties** (~10%) within 0-60%
- Centrality dependence similar for both energies



Particle distribution in azimuth

Single particle distribution in a single event:

$$\frac{dN}{d\vec{p}} = \sum_{n=-\infty}^{+\infty} V_n(p) e^{in\varphi} \quad V_n(p) \equiv \frac{1}{2\pi \Delta p_T \Delta \eta} \sum_{j=1}^{M(p)} \exp(in\varphi_j)$$

Pair distribution:

$$\left\langle \frac{d^2 N_{pairs}}{dp_a dp_b} \right\rangle = \underbrace{\left\langle \frac{dN}{dp_a} \frac{dN}{dp_b} \right\rangle}_{\text{Leading term}} + \underbrace{\mathcal{O}(N)}_{\text{Non-flow}}$$



Studying how particle pairs are correlated: The pair correlation matrix

Fourier expansion of the pair distribution:

$$\left\langle \frac{d^2 N_{pairs}}{dp_a dp_b} \right\rangle = \sum_{n=-\infty}^{+\infty} V_{n\Delta}(p_a, p_b) e^{in(\varphi_a - \varphi_b)}$$

With:

$$V_{n\Delta}(p_a, p_b) = \begin{pmatrix} \langle V_n(p_1) V_n^*(p_1) \rangle & \langle V_n(p_1) V_n^*(p_2) \rangle & (\dots) \\ \langle V_n(p_2) V_n^*(p_1) \rangle & \langle V_n(p_2) V_n^*(p_2) \rangle & (\dots) \\ (\dots) & (\dots) & (\dots) \end{pmatrix}$$

and 1, 2, 3... refers to the various momentum intervals used for analysis



Principal Component Analysis

We approximate the correlation matrix:

$$V_{n\Delta}(p_a, p_b) \approx \sum_{\alpha=1}^k V_n^{(\alpha)}(p) V_n^{(\alpha)*}(p_b)$$

And diagonalize it:

$$V_{n\Delta}(p_a, p_b) = \sum_{\alpha} \lambda^{(\alpha)} \psi^{(\alpha)}(p_a) \psi^{(\alpha)*}(p_b)$$

And ordering λ from largest to smallest:

$$V_n^{(\alpha)} \equiv \sqrt{\lambda^{(\alpha)}} \psi^{(\alpha)}$$



How is this related to the usual flow coefficients?

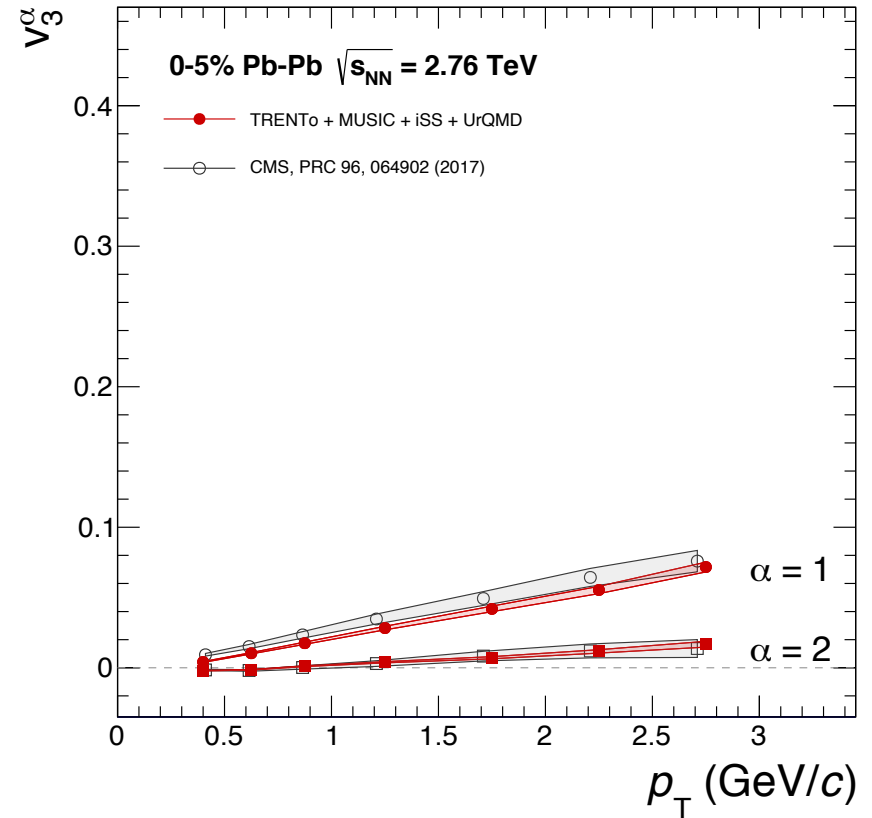
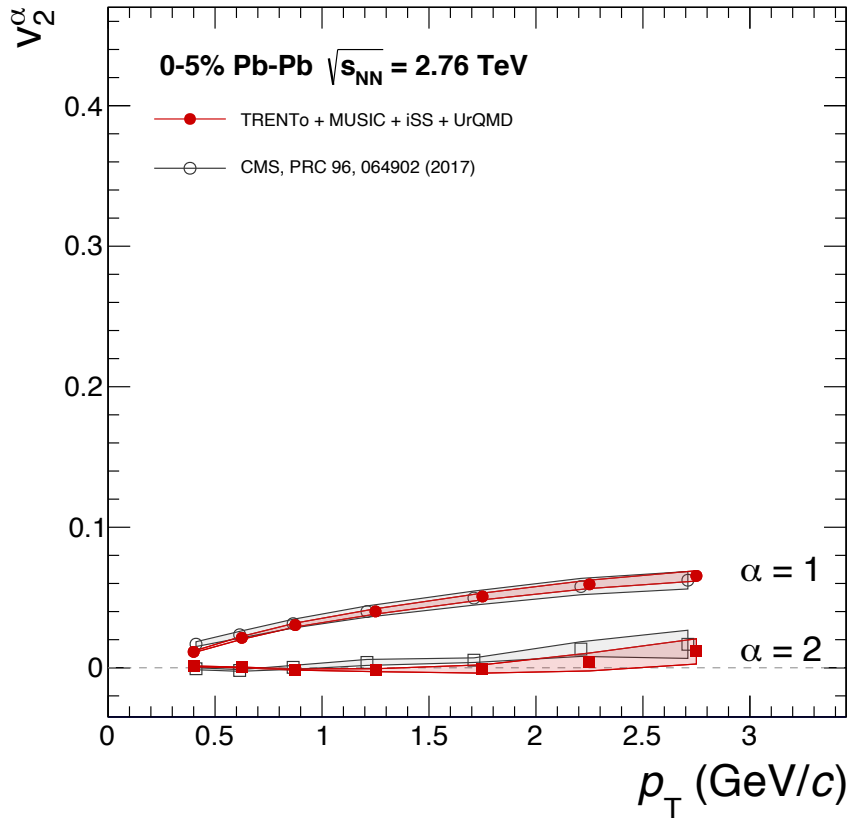
For compatibility with the usual flow picture:

$$v_n^{(\alpha)}(p) \equiv \frac{V_n^{(\alpha)}(p)}{V_0(p)}$$

- This way, the $\alpha = 1$ term will be equivalent to v_n measured via the usual two-particle correlation techniques...
- ...and the subleading ($\alpha = 2$) term quantifies factorization breaking in different momentum bins
- More information by exploiting the correlation matrix



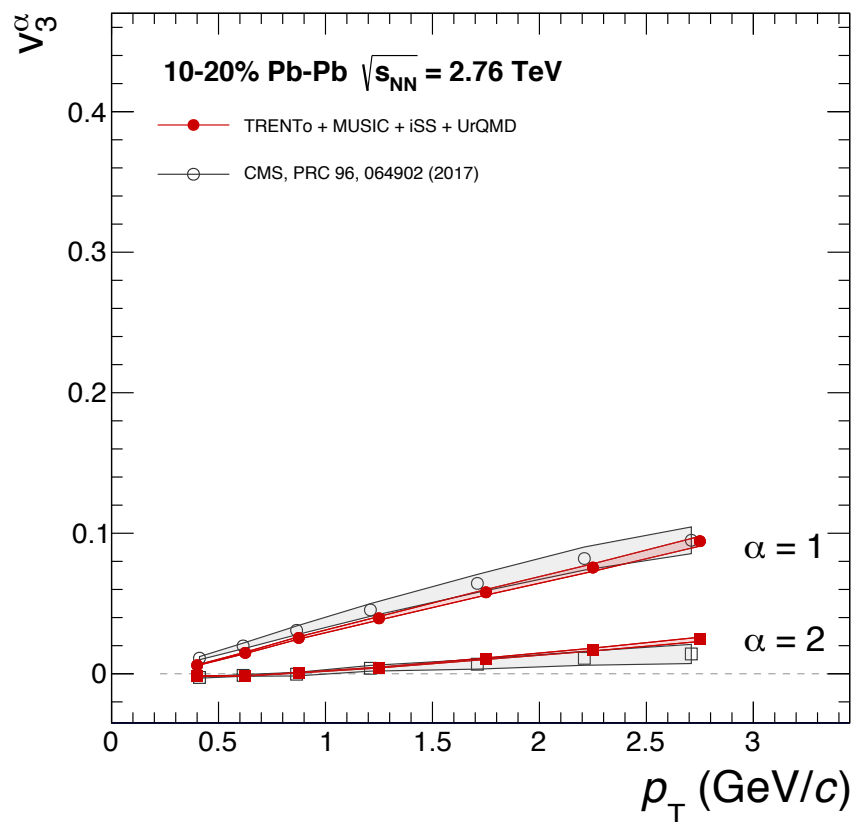
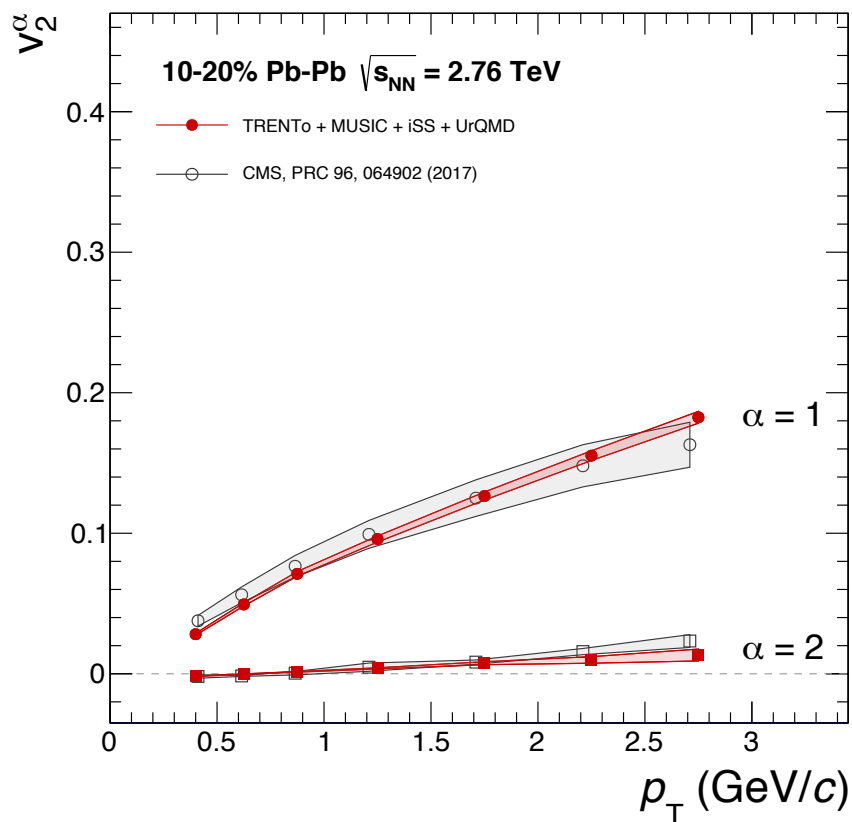
Pb-Pb 2.76 TeV: PCA as a function of p_T , 0-5%



- Model describes data within uncertainties for $\alpha = 1, 2$



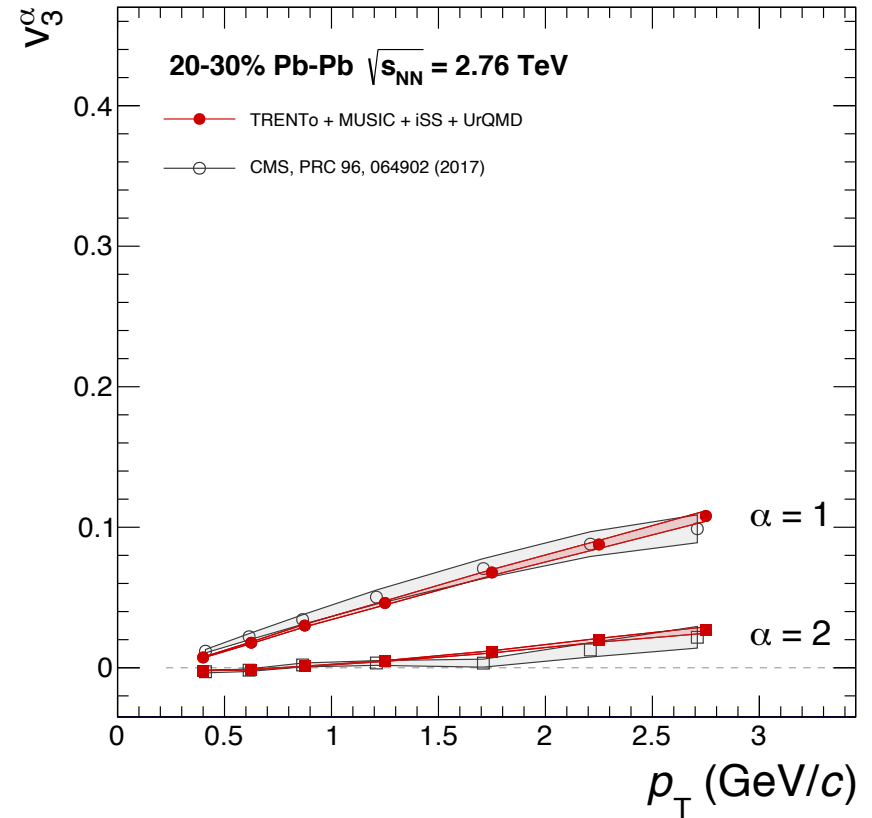
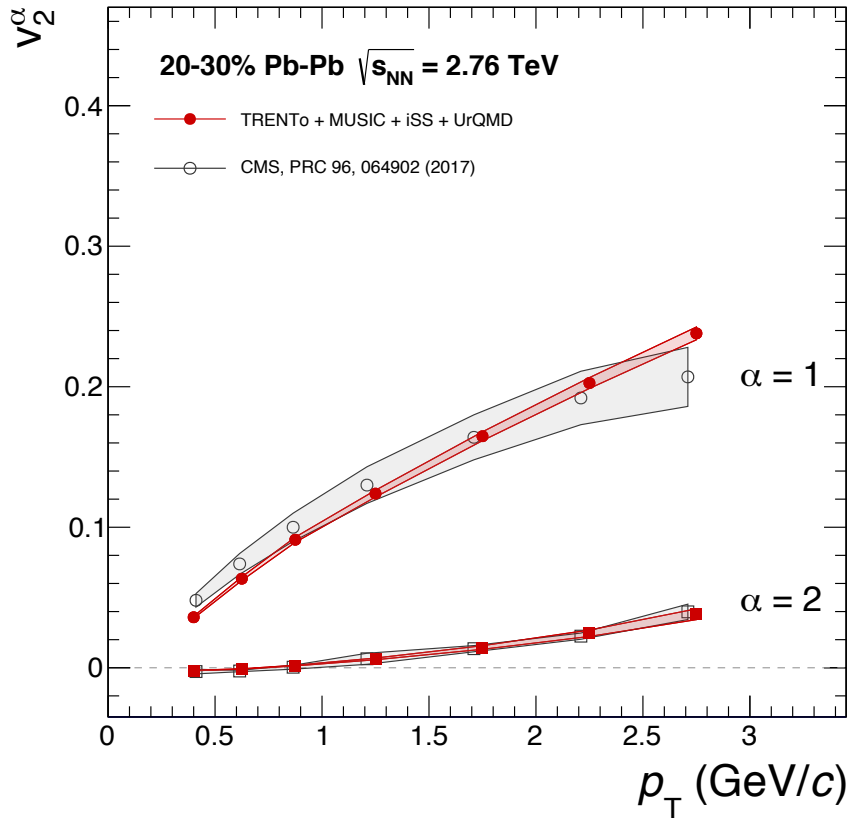
Pb-Pb 2.76 TeV: PCA as a function of p_T , 10-20%



- Model describes data within uncertainties for $\alpha = 1, 2$



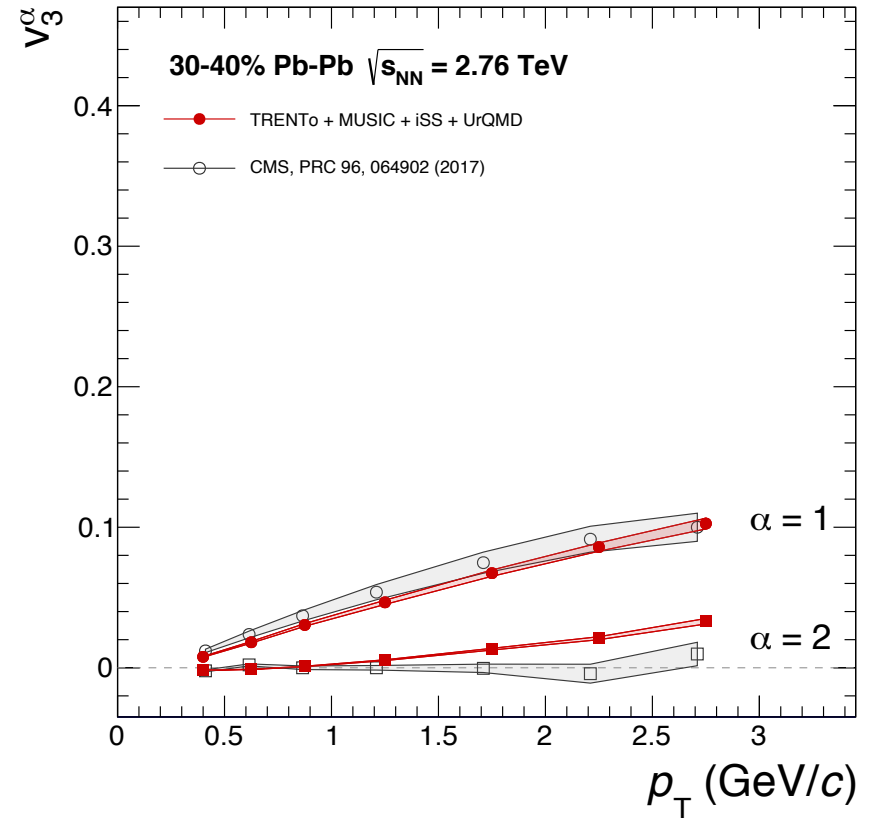
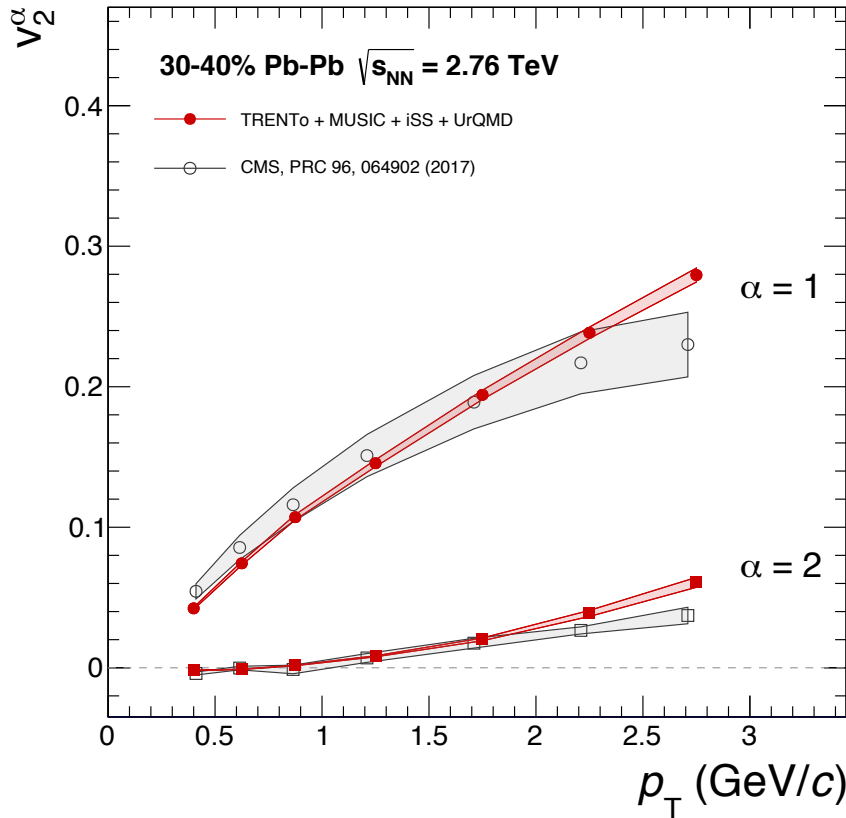
Pb-Pb 2.76 TeV: PCA as a function of p_T , 20-30%



- Model describes data within uncertainties for $\alpha = 1, 2$



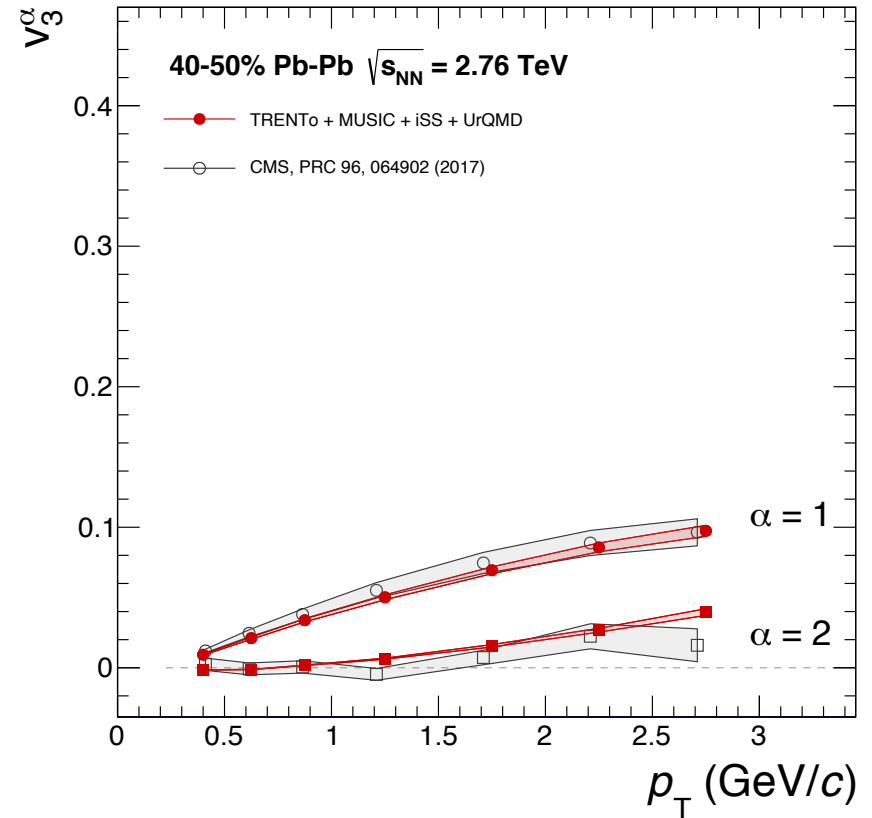
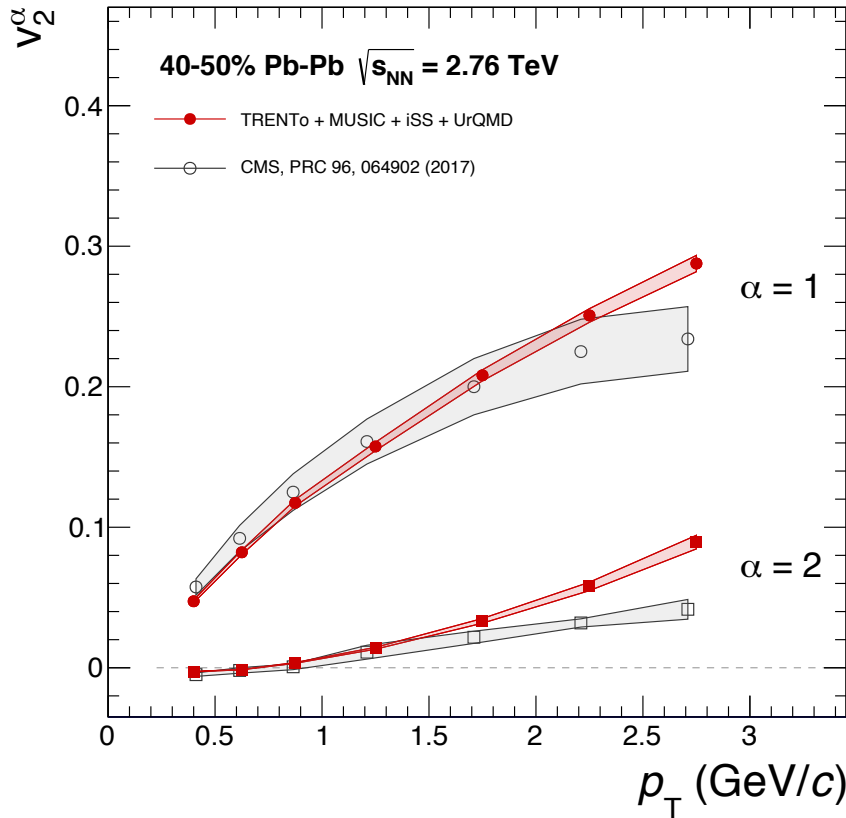
Pb-Pb 2.76 TeV: PCA as a function of p_T , 30-40%



- Model describes data within uncertainties for $\alpha = 1, 2$
- ...but deviations appear for semi-central collisions at high p_T



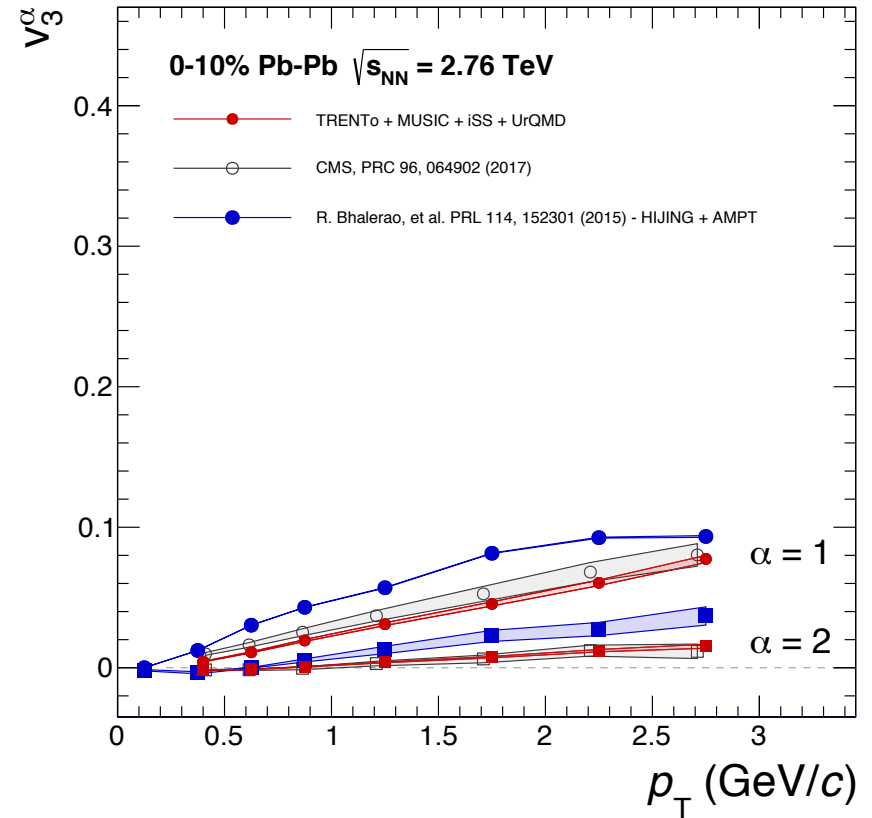
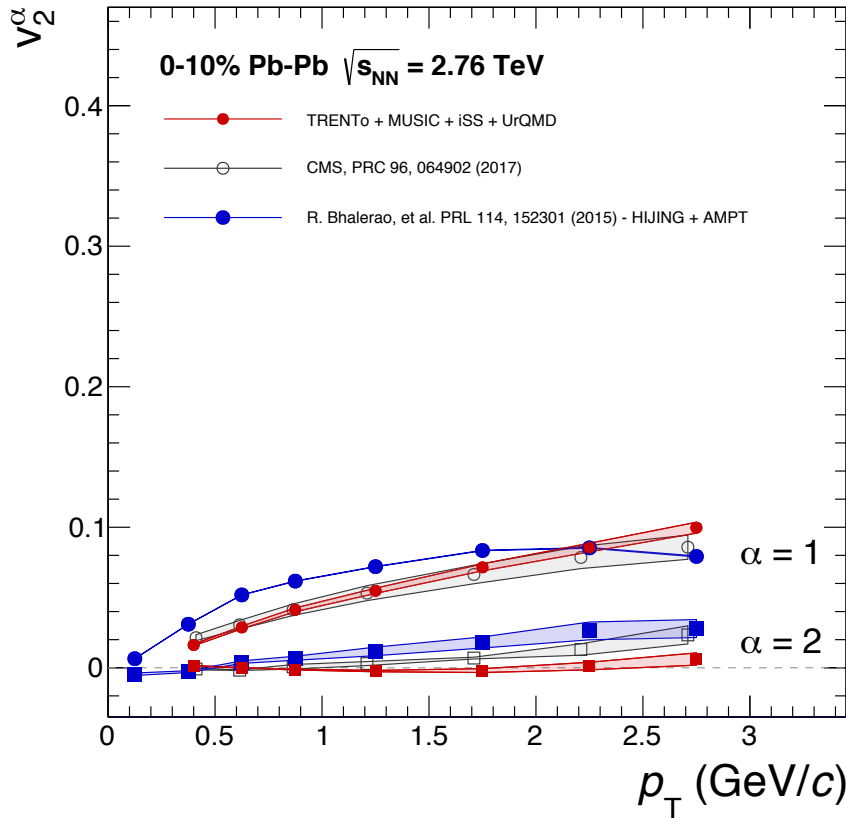
Pb-Pb 2.76 TeV: PCA as a function of p_T , 40-50%



- Model describes data within uncertainties for $\alpha = 1, 2$
- ...but deviations appear for semi-central collisions at high p_T



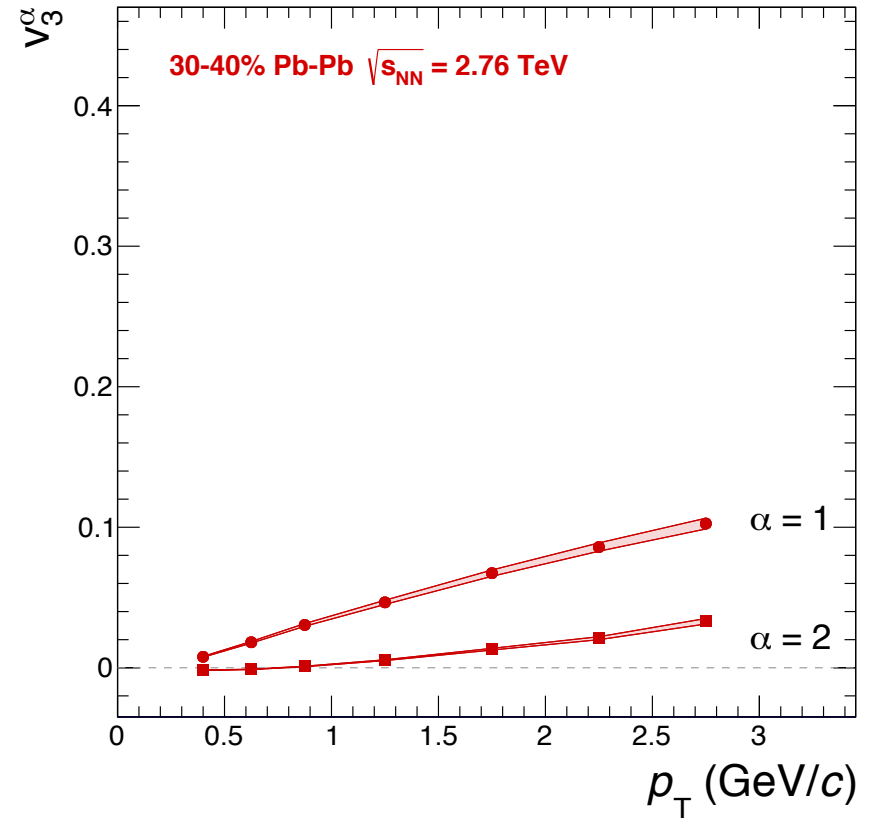
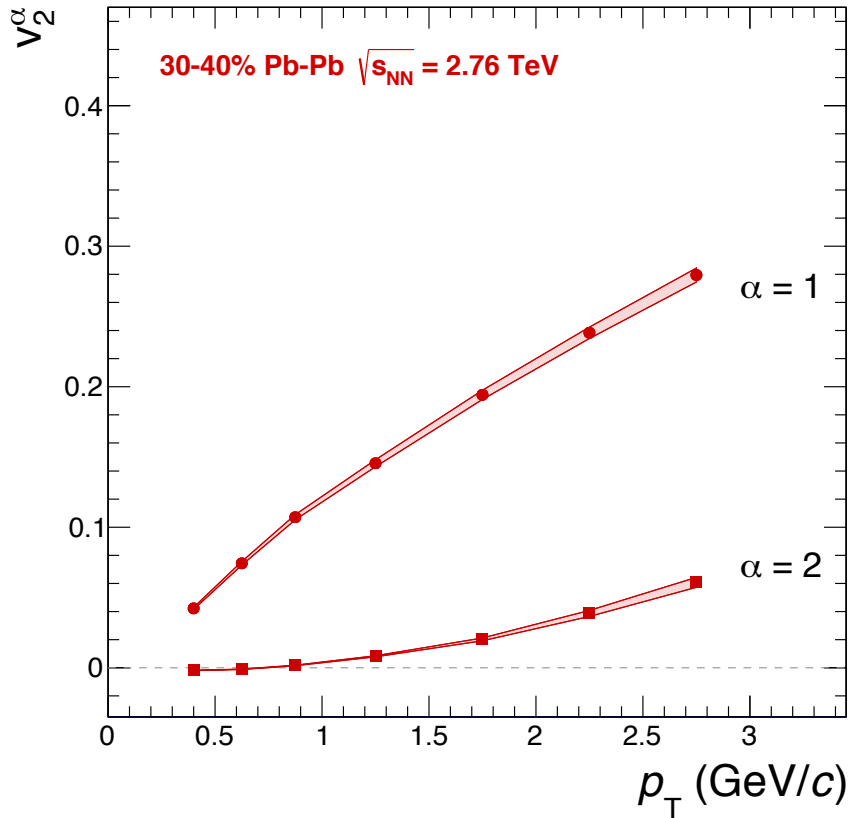
Comparison to Bhalerao et al: 0-10%



- HIJING+AMPT (Bhalerao et al, [no hydrodynamics](#)) fails to accurately predict the data



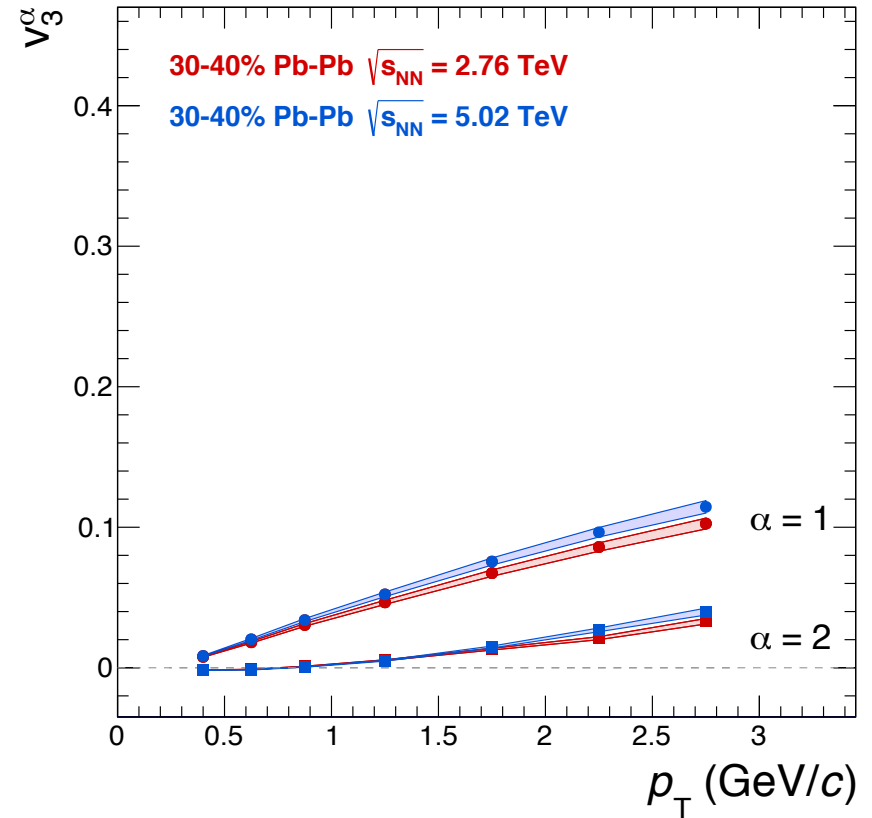
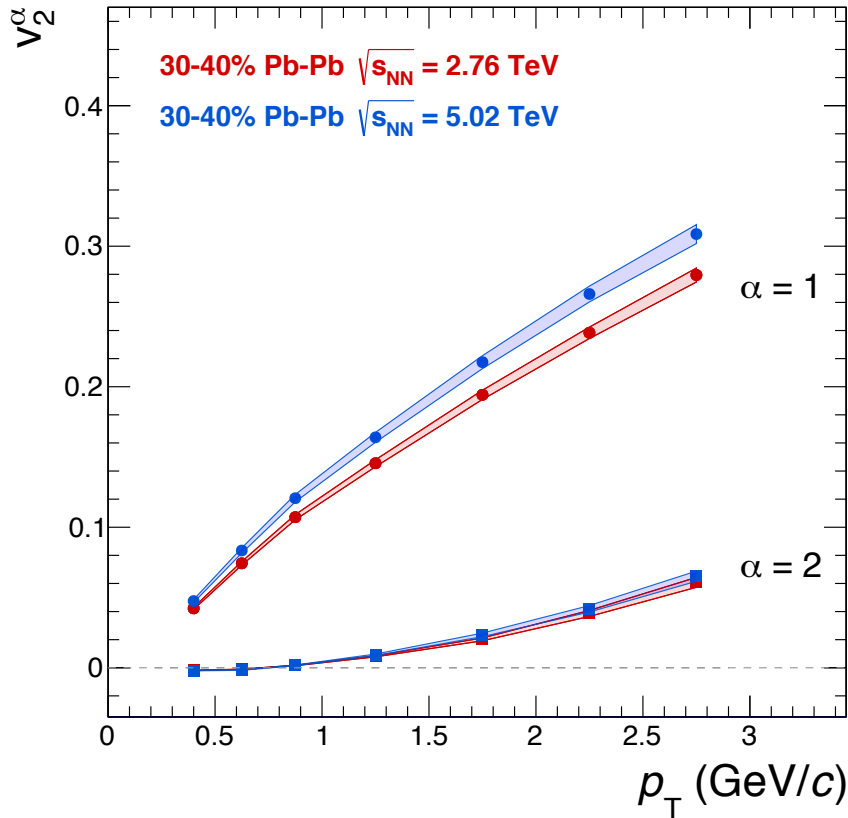
The energy dependence of PCA results



- Do results **change significantly with energy?**



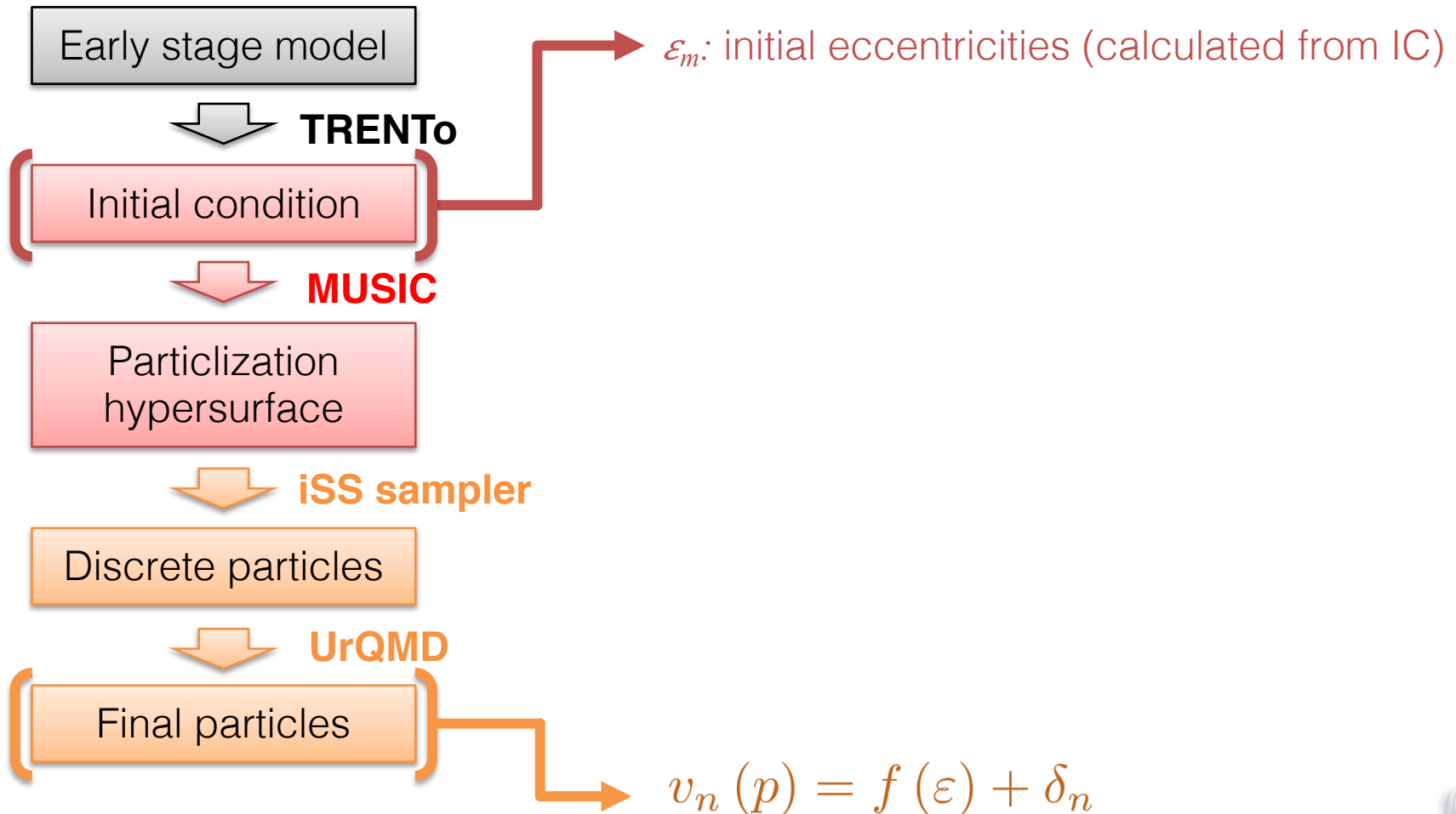
The energy dependence of PCA results



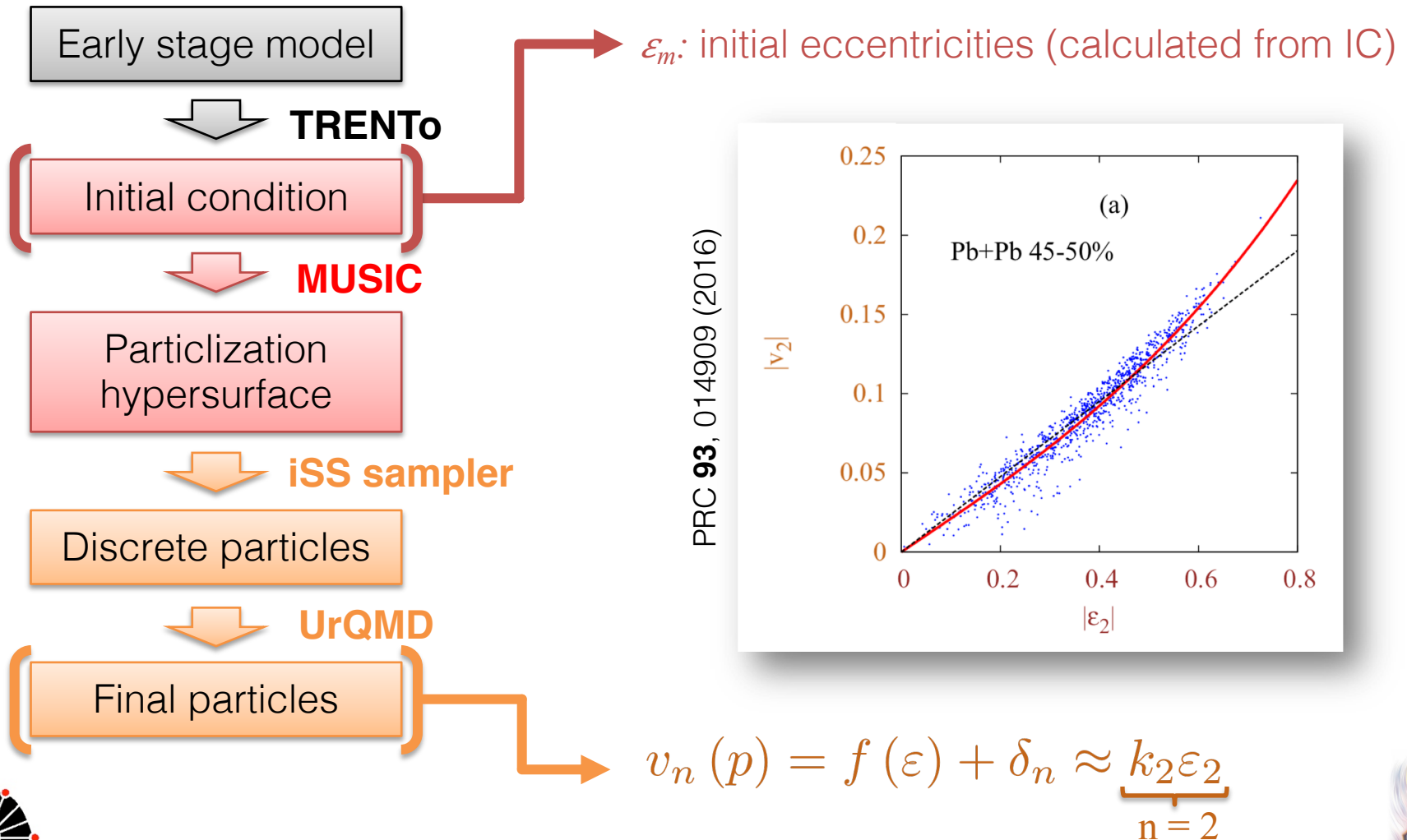
- Do results **change significantly with energy**?
- Weak **energy dependence**: $v_n^{(\alpha)}$ at most 10% larger



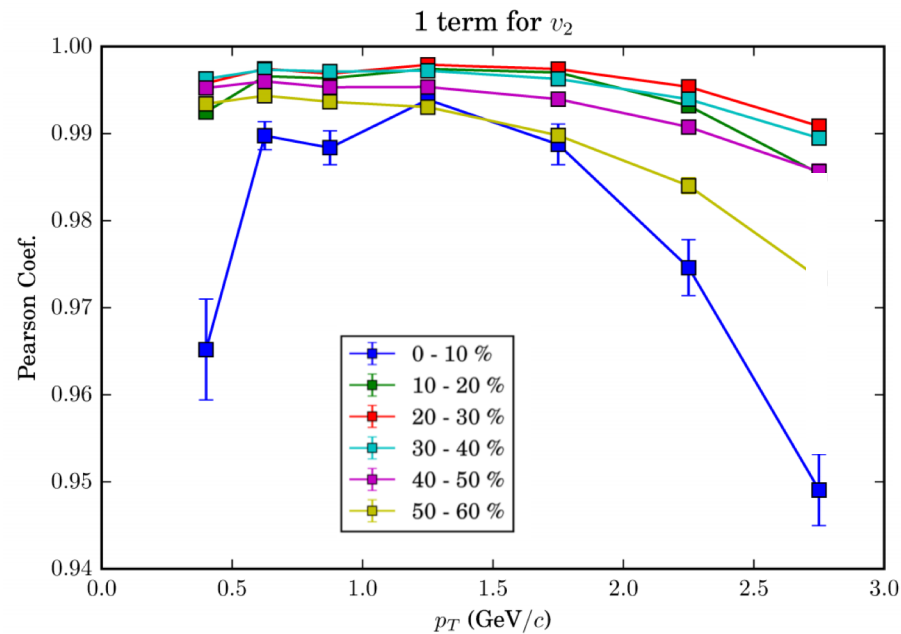
Work in progress: Studying hydrodynamic response



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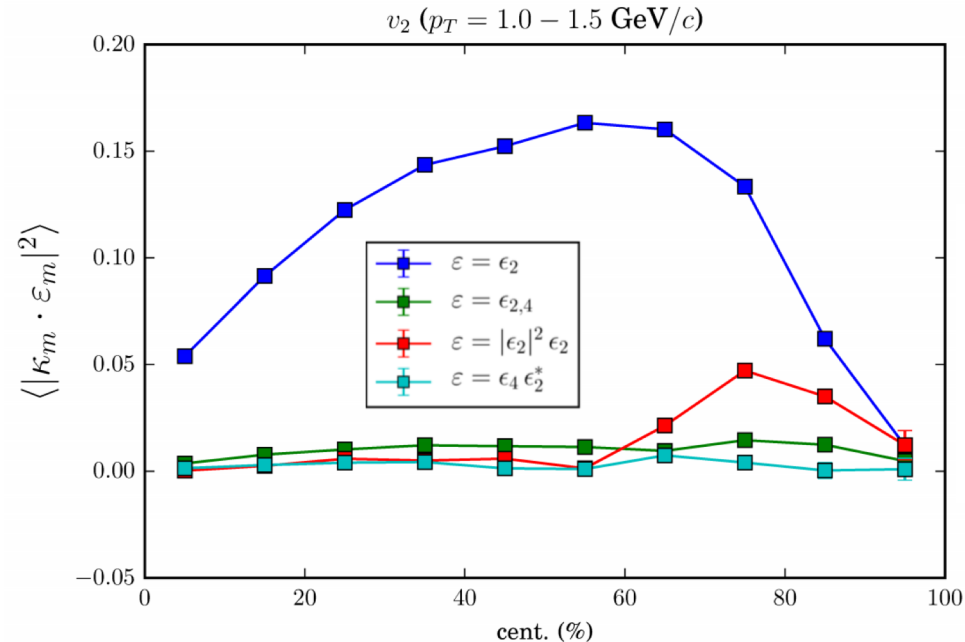
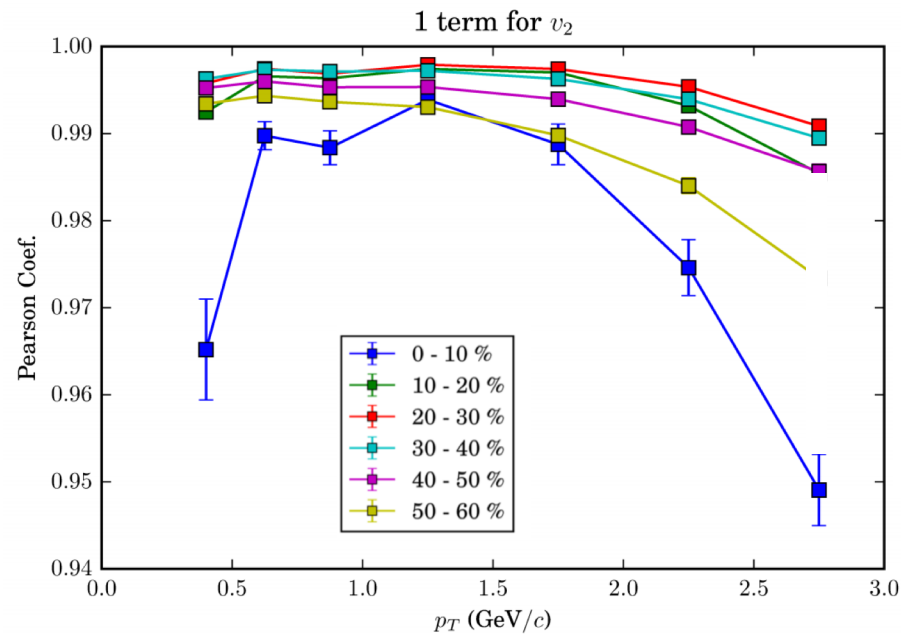
Work in progress: Studying hydrodynamic response: a first look



- **Very successful description:** initial and final flow well correlated across large momentum range



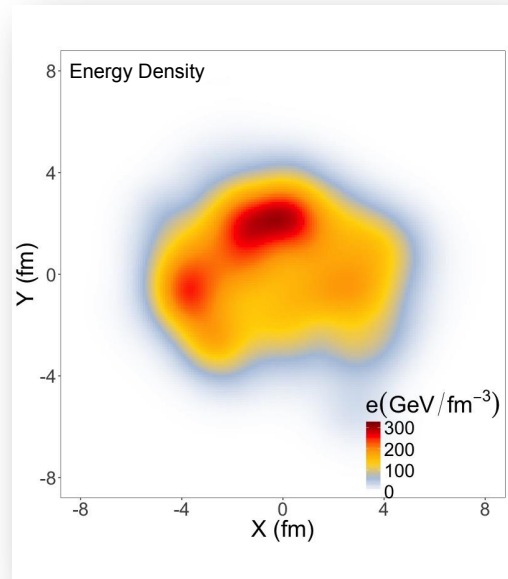
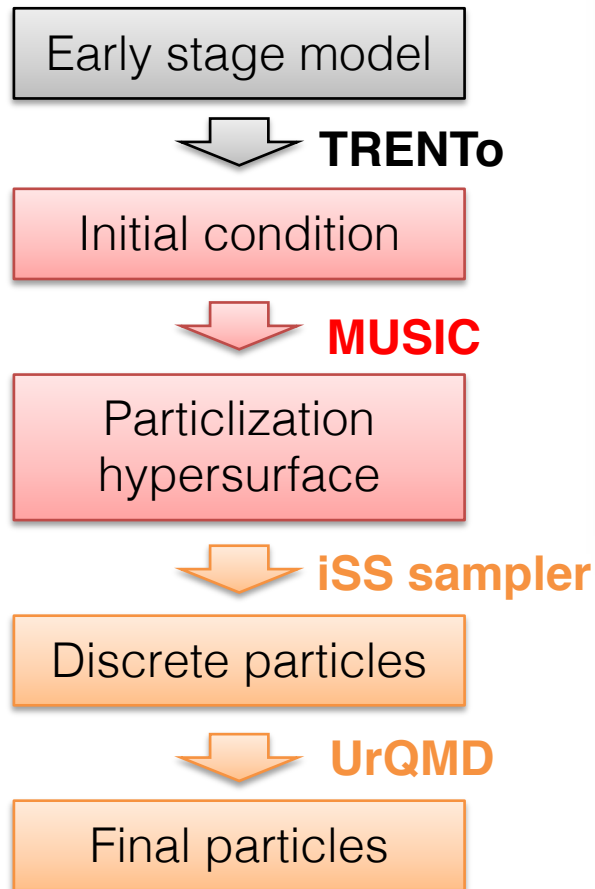
Work in progress: Studying hydrodynamic response: a first look



- **Very successful description:** initial and final flow well correlated across large momentum range
- Where do **higher order corrections** matter? Peripheral events
 - p_T -differential study pending



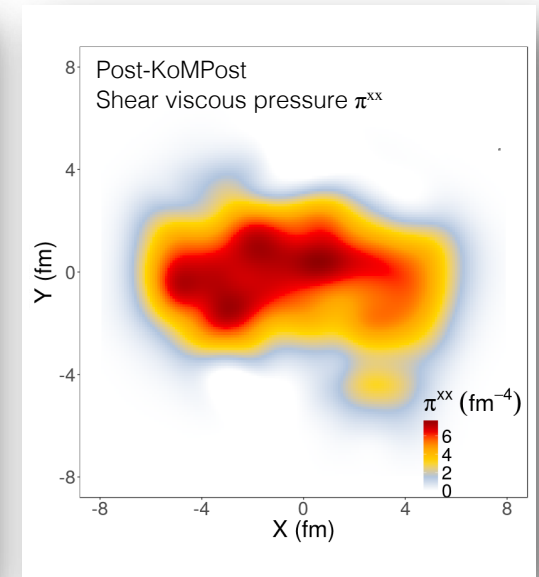
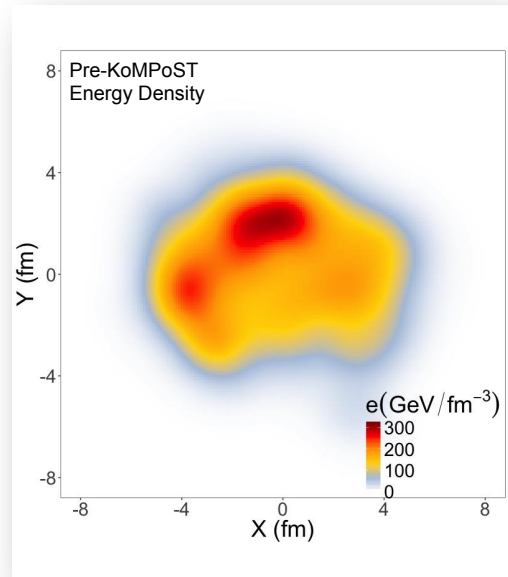
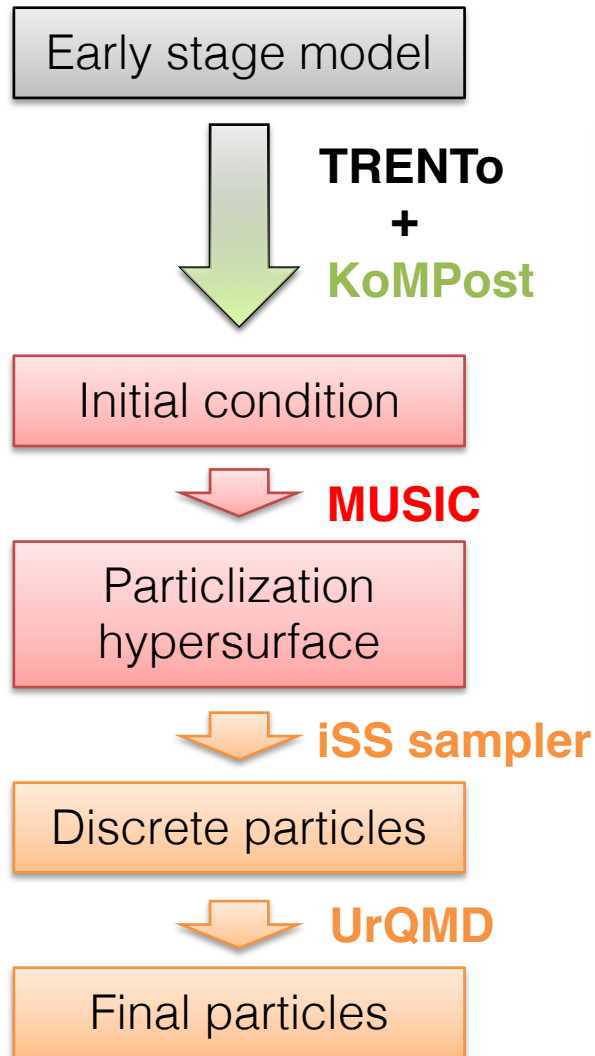
A more realistic IC: TRENTo + KoMPost



- Standard initial conditions: **only energy terms of energy-momentum tensor** populated → unrealistic



A more realistic IC: TRENTo + KoMPost

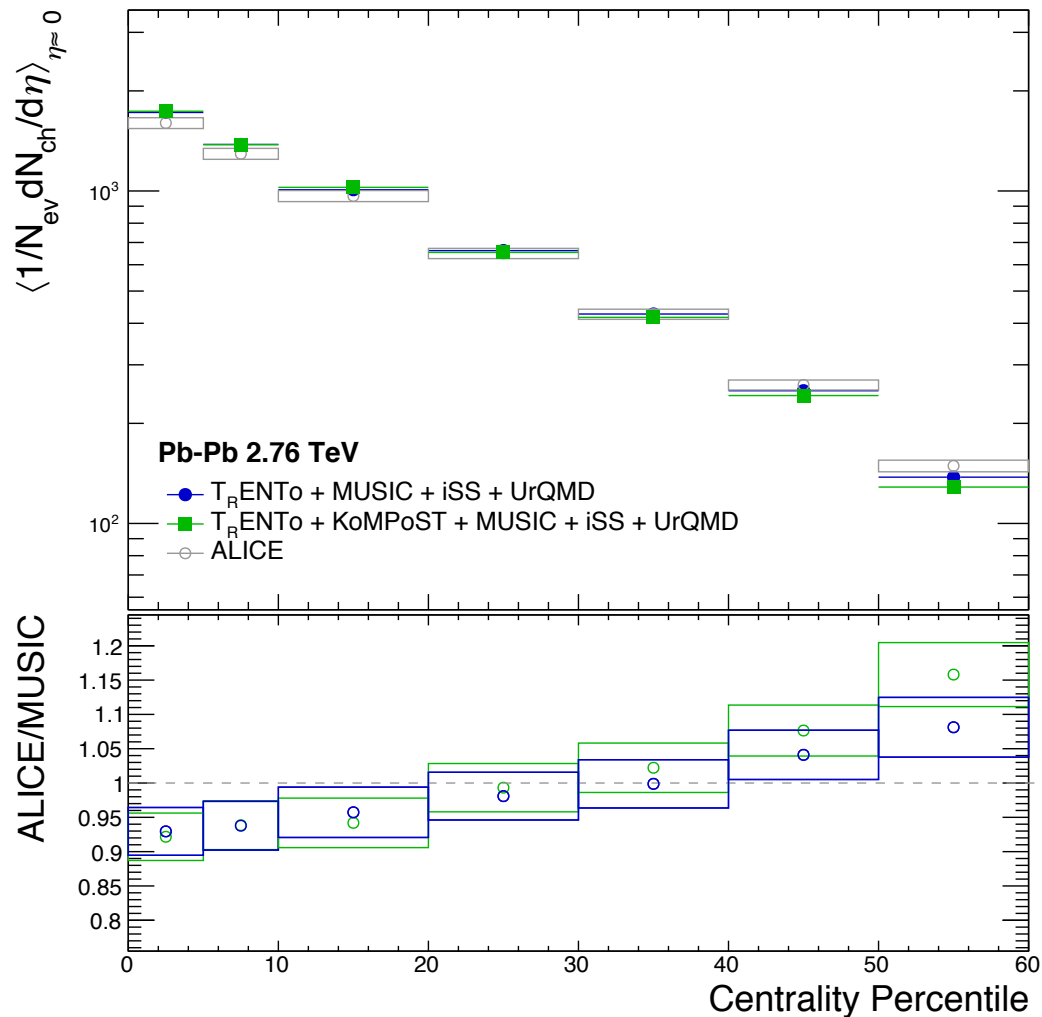


- Standard initial conditions: **only energy terms of energy-momentum tensor** populated \rightarrow unrealistic
- **Pre-equilibrium dynamics** can be simulated with kinetic theory: KoMPost [1]

[1] <https://arxiv.org/abs/1805.00961>



Work in progress: The KoMPost pre-equilibrium model

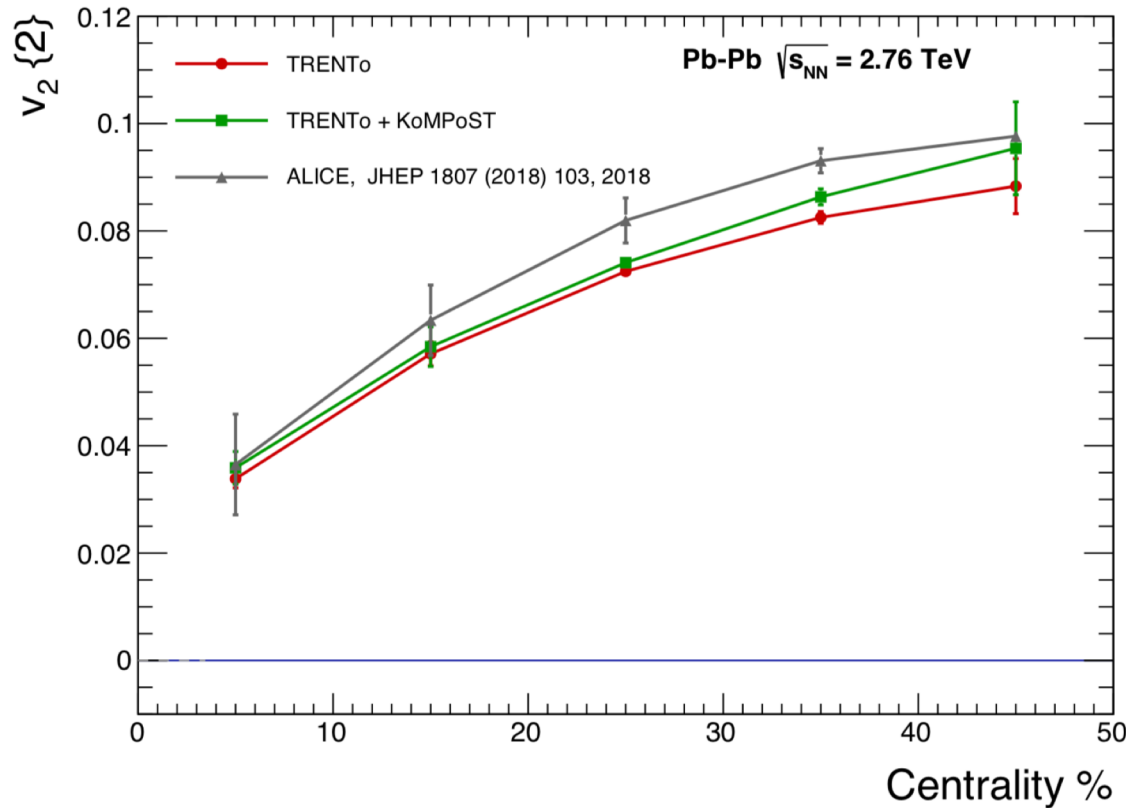


← No dramatic effect on multiplicities in central collisions

- Slight worsening in peripheral events?



Work in progress: KoMPost: first results



- Slight increase in integrated flow with pre-equilibrium dynamics?
- Possibly due to energy-momentum tensor being populated by additional terms



Summary and outlook

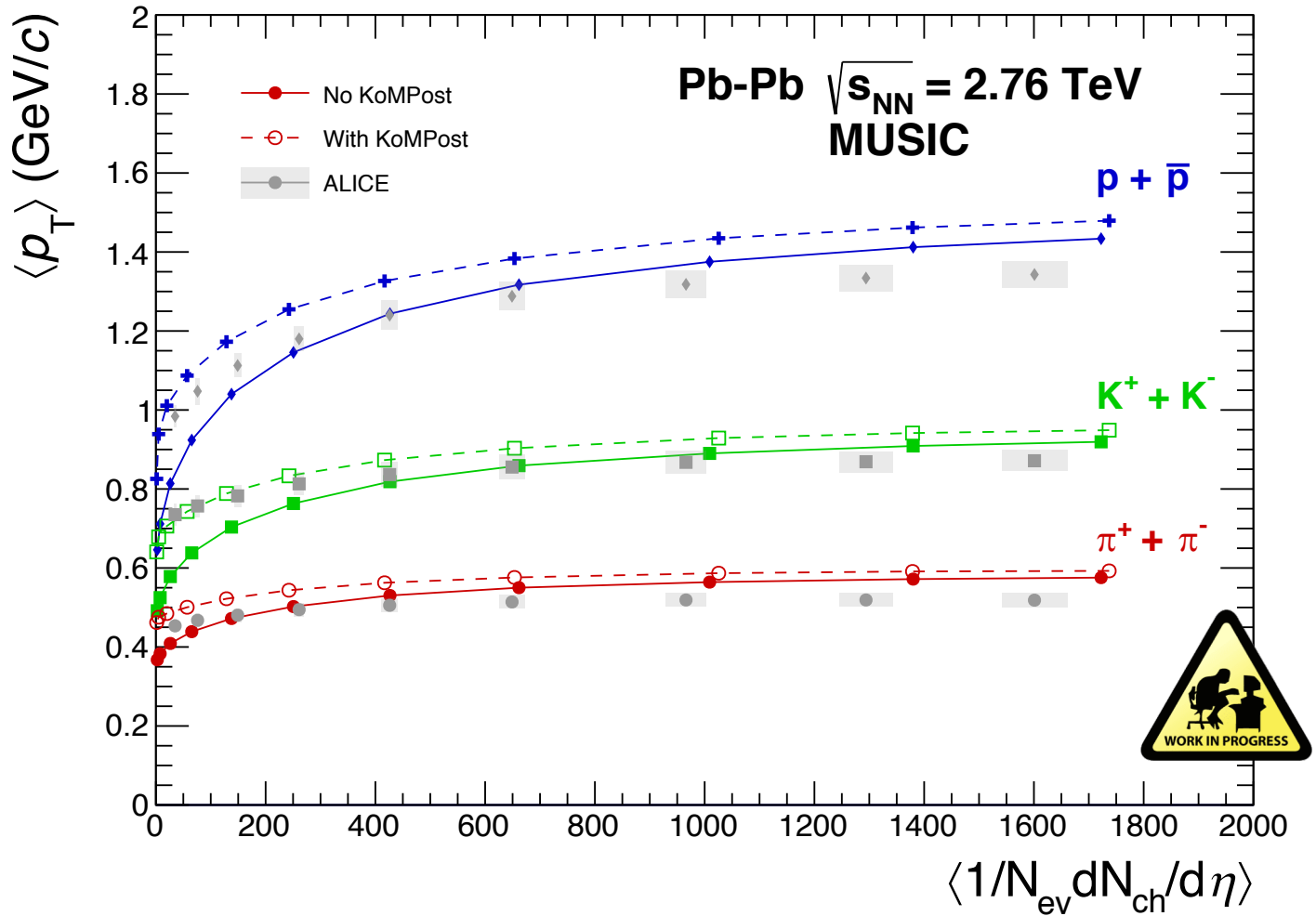
- Our [hybrid model](#) describes CMS data for the PCA of flow well in central Pb-Pb events at 2.76 TeV
- We predict [a small \(\$\sim 10\%\$ \) increase](#) in the PCA results [for 5.02 TeV](#)
- A lot of work being done:
 - Hydrodynamic response, effect of pre-equilibrium dynamics and rescattering (UrQMD), ...
 - Extension to RHIC BES-II energies and to small systems



Backup

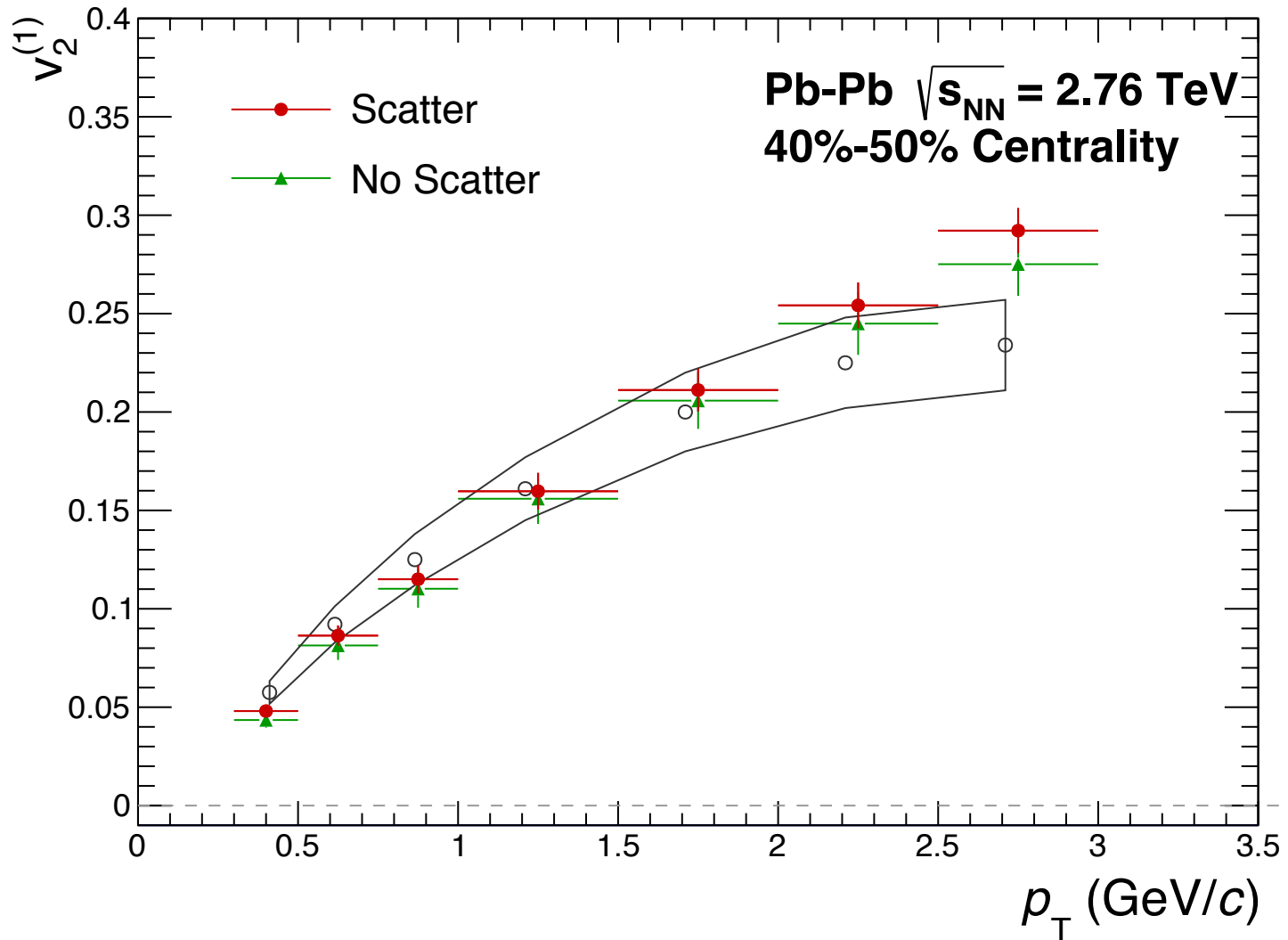


Average momentum



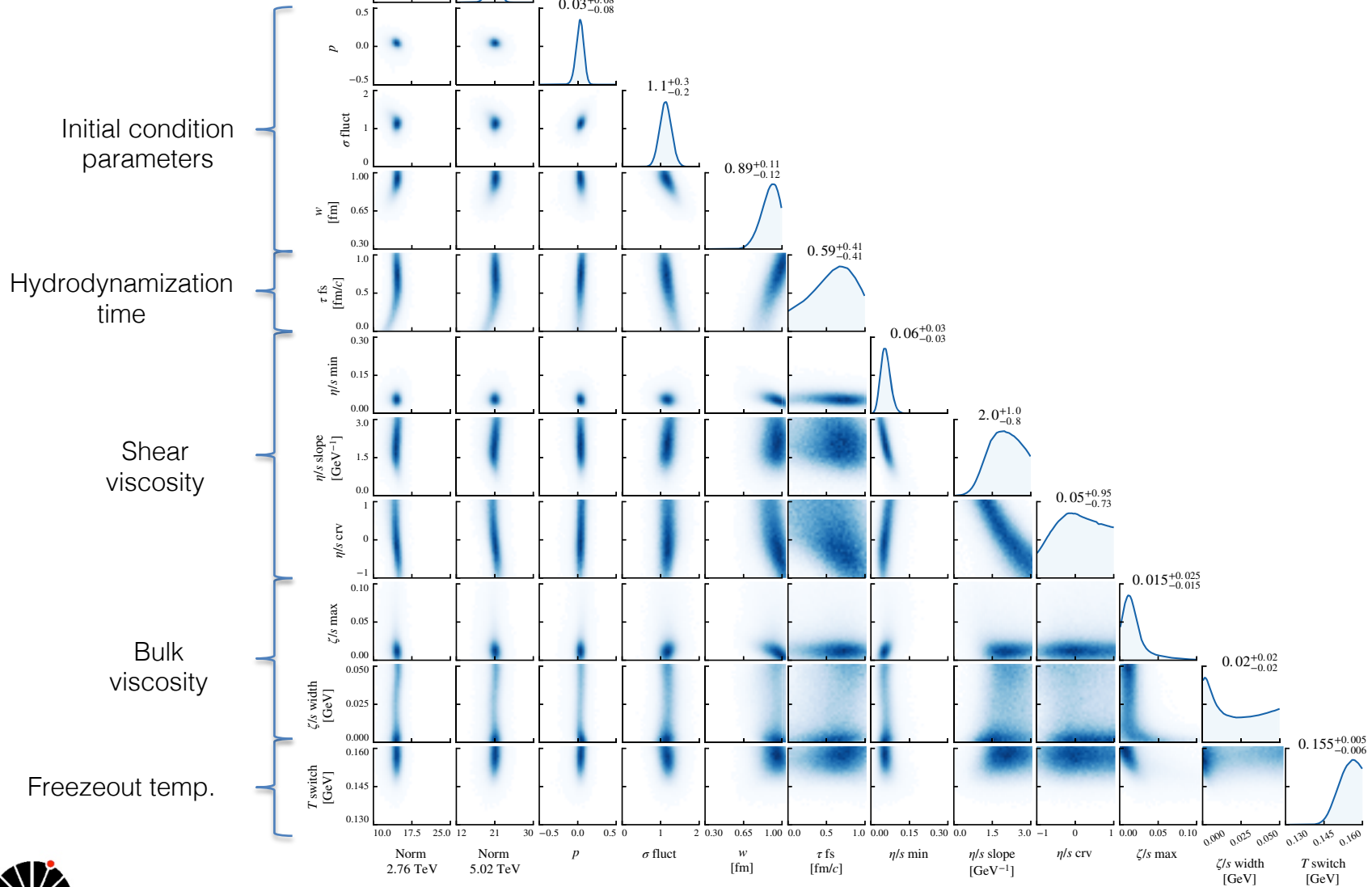
A very first look at...

Effects of rescattering



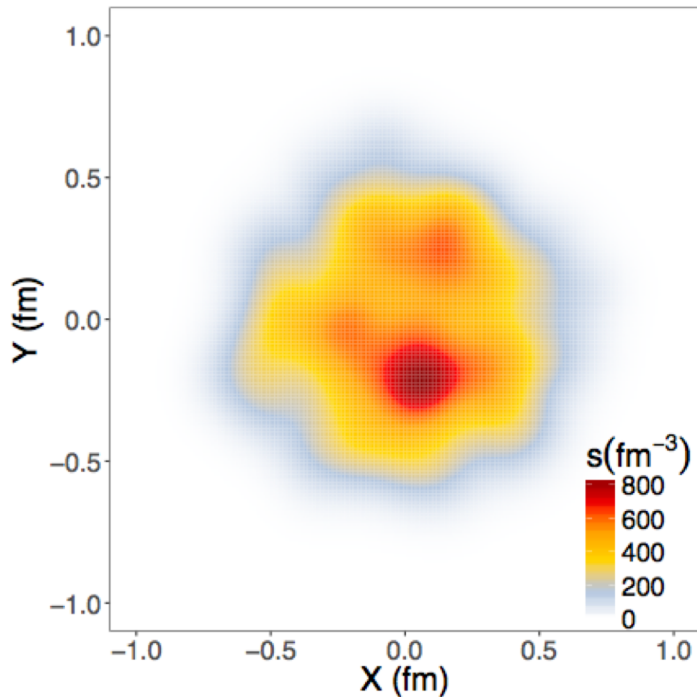
Parameters from Bayesian analysis

(from <https://arxiv.org/abs/1704.07671>)



TRENTo

arXiv:1412.4708v2 [nucl-th]



- A parametric [initial condition generator](#) based on eikonal entropy deposition via a “reduced thickness” function

$$T_{A,B}(x, y) = \int dz \rho_{A,B}^{part}(x, y, z)$$

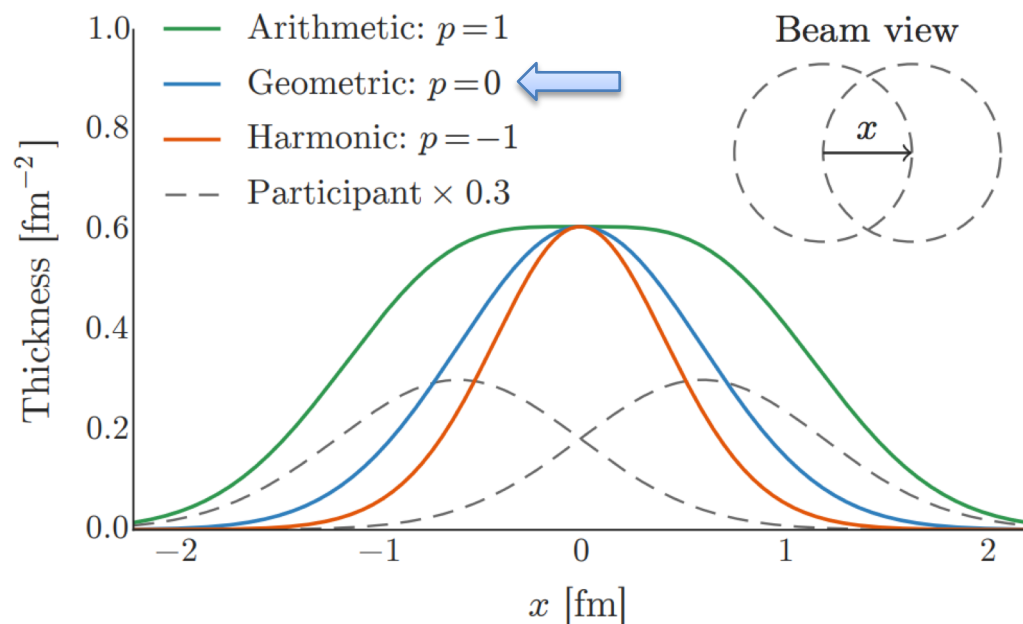
$$\left. \frac{dS}{dy} \right|_{\tau=\tau_0} \propto \left(\frac{T_A^p + T_B^p}{2} \right)^{1/p}$$



TRENT_o

arXiv:1412.4708v2 [nucl-th]

$$T_R = \begin{cases} \max(T_A, T_B) & p \rightarrow +\infty, \\ (T_A + T_B)/2 & p = +1, \text{ (arithmetic)} \\ \sqrt{T_A T_B} & p = 0, \text{ (geometric)} \\ 2T_A T_B / (T_A + T_B) & p = -1, \text{ (harmonic)} \\ \min(T_A, T_B) & p \rightarrow -\infty. \end{cases}$$



Hydrodynamics with MUSIC

- Eulerian 3D+1 relativistic second-order viscous hydrodynamics code for event by event (EBE) HIC simulations;
- Evolution is solved through the Kurganov-Tadmor method; (J.Comp.Phys 160, 214 - 2000)
- Code is written in C++ and supports parallelization;
- Code is publicly available (physics.mcgill.ca/music/)

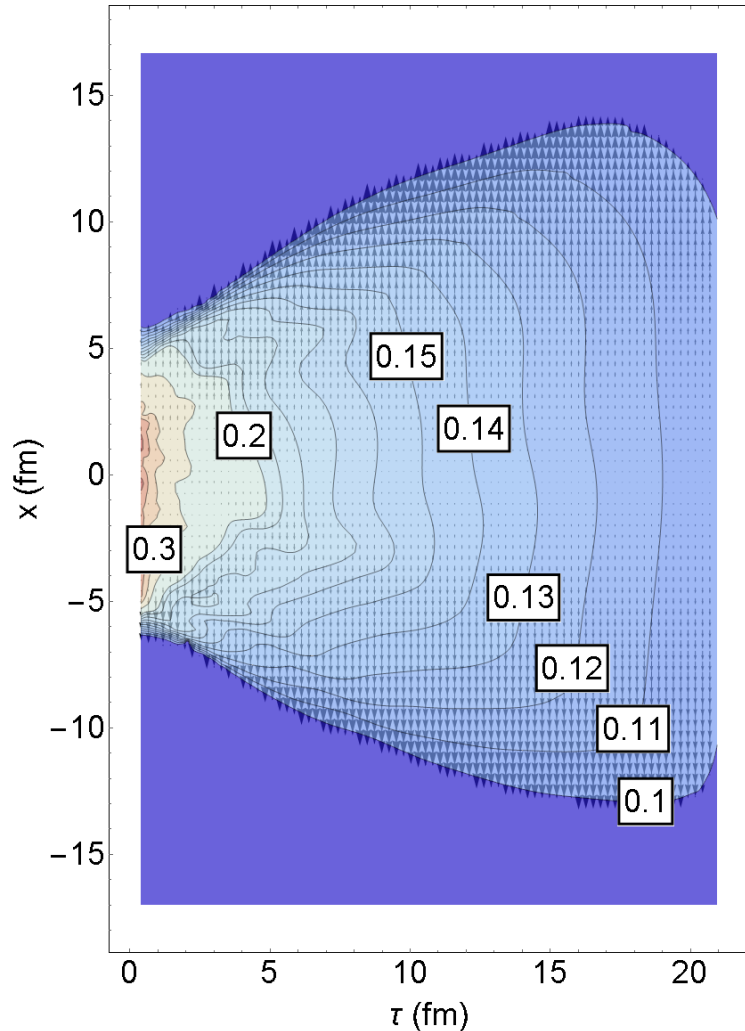
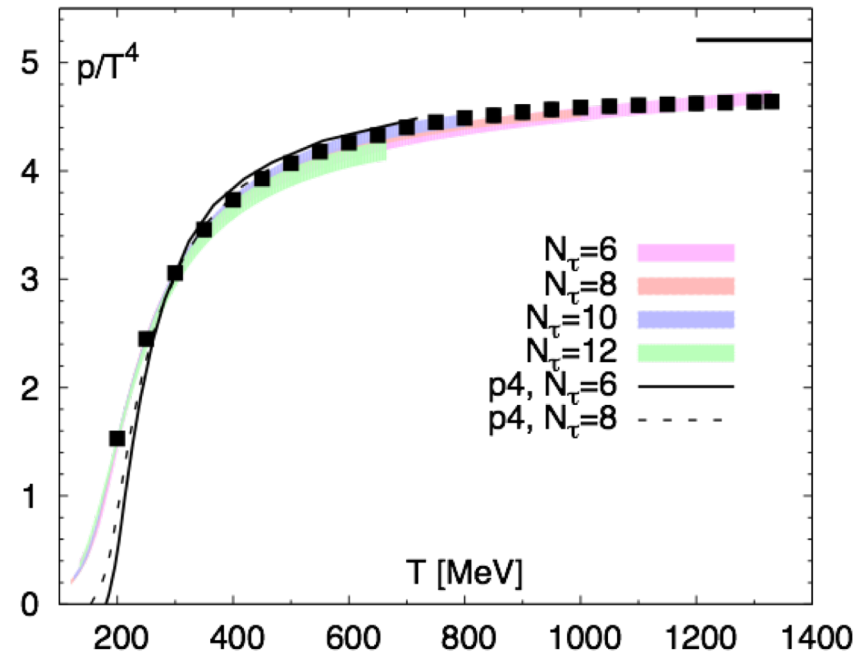


Figure: J-F. Paquet



The equation of state

- External input necessary to close the evolution system of equations;
- Calculated from first principles (e.g. Lattice QCD);
- Details of EOS can influence the extraction of transport coefficients.



**A. Bazavov et al.,
Phys. Rev. D 95, 054504 (2017)**



Simulation parameters

TRENT_o

$$p = 0.007, \sigma_{fluc} = 0.918, w = 0.956, d_{min} = 1.27$$

$$n_{2.76} = 286.23, n_{5.02} = 343.48$$

$$x_{2.76} = 6.28, x_{5.02} = 7.0$$

p: Reduced Thickness

w: Nucleon Width

d: Nucleon minimum distance

σ_{fluc} : Standard deviation of nucleon multiplicity fluctuations

n: normalization

x: Inelastic nucleon-nucleon cross-section



Simulation parameters

Hydro

$$T_{fo} = 151 \text{ MeV}, \tau_0 = 0.2 \text{ fm}$$

$$x_{max} = y_{max} = 14 \text{ fm}, N_x = N_y = 280$$

Lattice EOS s95p-v1.2 w/ UrQMD species
(Huovinen and Petrescky, Nucl.Phys.A837:26-53,2010)



Simulation parameters

Hydro: viscosity

Shear viscosity

$$(\eta/s)(T) = (\eta/s)_{min} + (\eta/s)_{slope} \cdot (T - T_c) \cdot (T/T_c)^{(\eta/s)_{crv}}$$

$$(\eta/s)_{min} = 0.081, (\eta/s)_{slope} = 1.11 \text{GeV}^{-1}$$

$$(\eta/s)_{crv} = -0.48, T_c = 154 \text{MeV}$$

Bulk viscosity

$$(\zeta/s)(T) = \frac{(\zeta/s)_{max}}{1 + \frac{T - (\zeta/s)_{T_0}}{(\zeta/s)_{width}}}$$

$$(\zeta/s)_{max} = 0.052, (\zeta/s)_{width} = 0.022 \text{GeV}, T_0 = 183 \text{MeV}$$



Additional technicalities

Ideal hydro

$$T_{ideal}^{\mu\nu} = (\overset{\text{Energy density}}{\epsilon} + \overset{\text{Pressure}}{\mathcal{P}}) \overset{\text{Flow velocity}}{u}^{\mu} u^{\nu} - \mathcal{P} g^{\mu\nu}$$

$$\partial_{\mu} T^{\mu\nu} = 0 \quad + \quad \partial_{\mu} j_i^{\mu} = 0$$

Energy and momentum
conservation

Other conserved
quantities
(B, S, Q)



Additional technicalities

Hydro with viscosity: Israel-Stewart

$$T^{\mu\nu} = T_{ideal}^{\mu\nu} + \overset{\substack{\text{shear viscous} \\ \text{Pressure (tensor)}}}{\pi^{\mu\nu}} - (g^{\mu\nu} - u^\mu u^\nu) \overset{\substack{\text{bulk viscous} \\ \text{Pressure (scalar)}}}{\Pi}$$

$$\partial_\mu T^{\mu\nu} = 0 \qquad \partial_\mu j_i^\mu = 0$$

+ complicated equations of motion for $\pi^{\mu\nu}, \Pi$

Total of 14 non-linear coupled PDEs, with 13 transport coefficients:

$$\eta(T, \mu), \zeta(T, \mu), \tau_\pi(T, \mu), \delta_{\pi\pi}(T, \mu), \dots$$



Additional technicalities

Hydro with viscosity: Israel-Stewart

$$T^{\mu\nu} = T_{ideal}^{\mu\nu} + \pi^{\mu\nu} - (g^{\mu\nu} - u^\mu u^\nu) \Pi$$

$$\partial_\mu T^{\mu\nu} = 0 \quad \partial_\mu j_i^\mu = 0$$

$$\tau_\pi \dot{\pi}^{\langle\mu\nu\rangle} + \pi^{\mu\nu} = 2\eta \sigma^{\mu\nu} + 2\tau_\pi \pi_\alpha^{\langle\mu} \omega^{\nu\rangle\alpha} - \delta_{\pi\pi} \pi^{\mu\nu} \theta + \varphi_7 \pi_\alpha^{\langle\mu} \pi^{\nu\rangle\alpha} - \tau_{\pi\pi} \pi_\alpha^{\langle\mu} \sigma^{\nu\rangle\alpha} + \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu} + \varphi_6 \Pi \pi^{\mu\nu}$$

Shear PDE

$$\tau_\Pi \dot{\Pi} + \Pi = -\zeta \theta - \delta_{\Pi\Pi} \Pi \theta + \varphi_1 \Pi^2 + \lambda_{\Pi\pi} \pi^{\mu\nu} \sigma_{\mu\nu} + \varphi_3 \pi^{\mu\nu} \pi_{\mu\nu}$$

Bulk PDE



A heavy ion collision

