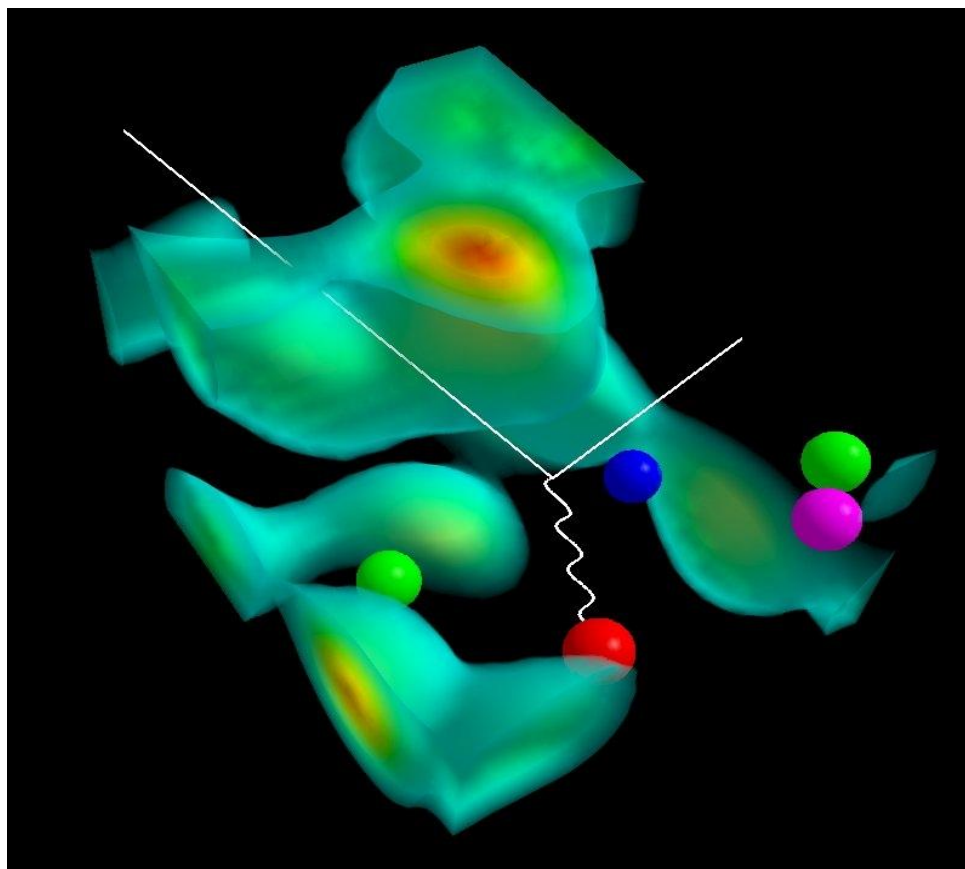


# QCD and a New Paradigm for Nuclear Structure



Australian Government  
Australian Research Council

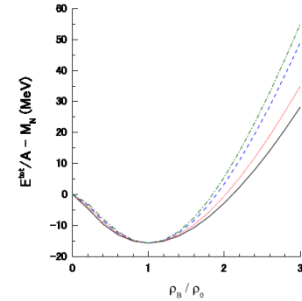
Anthony W. Thomas

QCD-TNT-4

Ilhabela: September 2<sup>nd</sup> 2015



# Relevance of QCD to Nuclear Structure



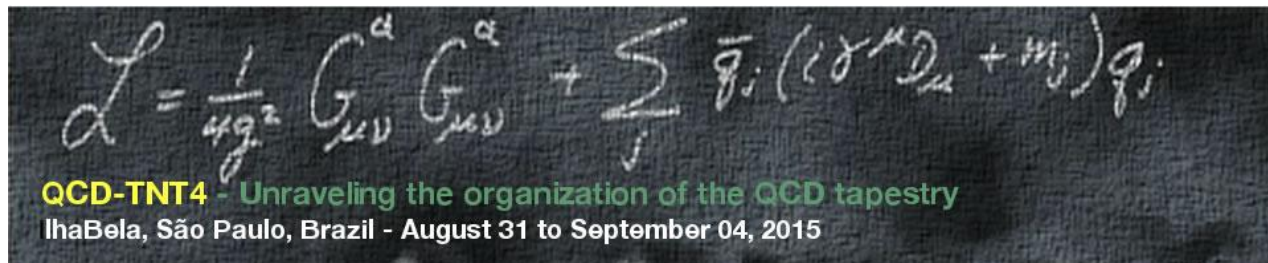
- Insight into origin of saturation?
  - minimum of binding/nucleon vs  $\rho$
- Behaviour at very high density (neutron star)
  - transition from hadronic to quark matter
- EFT *assumes* relevant d.o.f. :  
beware lesson of drunk looking for keys under lamp post
  - EFT has symmetries of QCD but is this enough?  
We need to know the relevant d.o.f. too
- Working at quark level can provide guidance

and now for something really different.....



# Outline

- Start from a QCD-inspired model of *hadron* structure
- Ask how that internal structure is modified in-medium
- This naturally leads to saturation  
+ predictions for all hadrons (e.g. hypernuclei...)
- Derive effective forces (Skyrme type): apply to finite nuclei
- Test predictions for quantities sensitive to internal structure: e.g. DIS structure functions and form factors in-medium

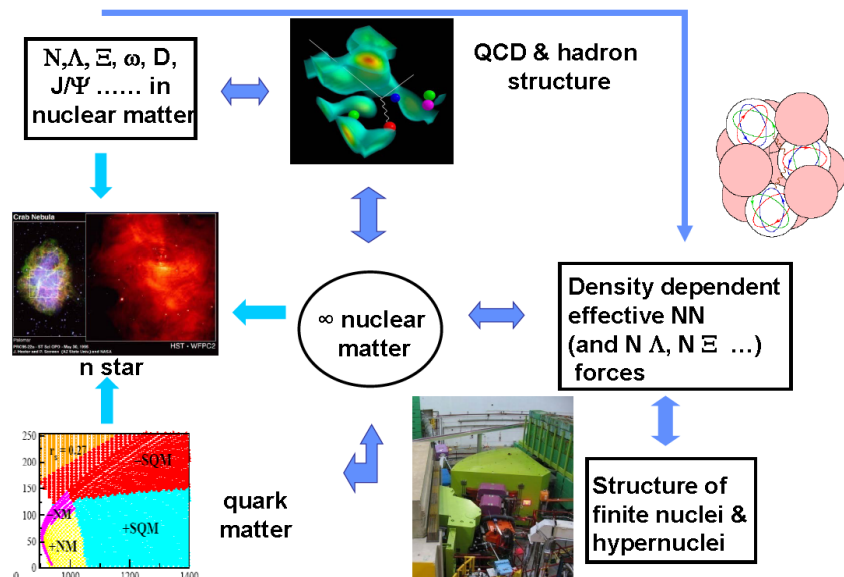


# A different approach : QMC Model

(Guichon, Saito, Tsushima et al., Rodionov et al.

- see Saito et al., Prog. Part. Nucl. Phys. 58 (2007) 1 for a review)

- Start with quark model (MIT bag/NJL...) for all hadrons
- Introduce a relativistic Lagrangian with  $\sigma$ ,  $\omega$  and  $\rho$  mesons coupling to non-strange quarks
- Hence only 3 parameters :  $g^q_{\sigma,\omega,\rho}$ 
  - determine by fitting to saturation properties of nuclear matter ( $\rho_0$ ,  $E/A$  and symmetry energy)
- Must solve self-consistently for the internal structure of baryons in-medium



# Effect of scalar field on quark spinor

- MIT bag model: quark spinor modified in bound nucleon

$$\frac{\mathcal{N}}{4\pi} \begin{pmatrix} j_0(xu'/R_B) \\ i\beta_q \vec{\sigma} \cdot \hat{u}' j_1(xu'/R_B) \end{pmatrix} \chi_m$$

- Lower component enhanced by attractive scalar field

$$\beta_q = \sqrt{\frac{\Omega_0 - m_q^* R_B}{\Omega_0 + m_q^* R_B}}$$

- This leads to a *very small* ( $\sim 1\%$  at  $\rho_0$ ) *increase in bag radius*
- It also *suppresses the scalar coupling to the nucleon as the scalar field increases*

$$g_\sigma = 3g_\sigma^q \int_{\text{Bag}} d\vec{r} \bar{q} q(\vec{r}) \sim \frac{\Omega_0/2 + m_q^* R_B (\Omega_0 - 1)}{\Omega_0 (\Omega_0 - 1) + m_q^* R_B / 2}$$

- This is the “scalar polarizability”: a new saturation mechanism for nuclear matter

# Quark-Meson Coupling Model (QMC): Role of the Scalar Polarizability of the Nucleon

The response of the nucleon internal structure to the scalar field is of great interest... and importance

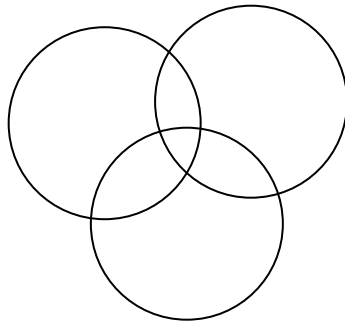
$$M^*(\vec{R}) = M - g_\sigma \sigma(\vec{R}) + \frac{d}{2} (g_\sigma \sigma(\vec{R}))^2$$

Non-linear dependence through the scalar polarizability  
 $d \sim 0.22 R$  in original QMC (MIT bag)

Indeed, in nuclear matter at mean-field level (e.g. QMC), this is the **ONLY** place the response of the internal structure of the nucleon enters.

# Summary : Scalar Polarizability

- Can always rewrite non-linear coupling as linear coupling plus non-linear scalar self-coupling – likely physical origin of some non-linear versions of QHD
- Consequence of polarizability in atomic physics is many-body forces:



$$V = V_{12} + V_{23} + V_{13} + V_{123}$$

– same is true in nuclear physics



# Summary so far .....

- **QMC** looks superficially like QHD but it's **fundamentally different from *all* other approaches**
- **Self-consistent adjustment of hadron structure opposes applied scalar field (“scalar polarizability”)**
- **Naturally leads to saturation of nuclear matter**
  - effectively because of natural 3- and 4-body forces
- **Only 3 parameters:  $\sigma$ ,  $\omega$  and  $\rho$  couplings to light quarks**
- **Fit to nuclear matter properties and then *predict* the interaction of any hadrons in-medium**

# Linking QMC to Familiar Nuclear Theory

Since early 70's tremendous amount of work  
in nuclear theory is based upon effective forces

- Used for everything from nuclear astrophysics to collective excitations of nuclei
- Skyrme Force: Vautherin and Brink

$$\begin{aligned}
 H_{QMC} = & \sum_i \frac{\vec{\nabla}_i \cdot \vec{\nabla}_i}{2M} + \frac{G_\sigma}{2M^2} \sum_{i \neq j} \vec{\nabla}_i \delta(\vec{R}_{ij}) \cdot \vec{\nabla}_i \\
 & + \frac{1}{2} \sum_{i \neq j} \left[ \nabla_i^2 \delta(\vec{R}_{ij}) \right] \left[ \frac{G_\omega}{m_\omega^2} - \frac{G_\sigma}{m_\sigma^2} + \frac{G_\rho}{m_\rho^2} \frac{\vec{\tau}_i \cdot \vec{\tau}_j}{4} \right] \\
 & + \frac{1}{2} \sum_{i \neq j} \delta(\vec{R}_{ij}) \left[ G_\omega - G_\sigma + G_\rho \frac{\vec{\tau}_i \cdot \vec{\tau}_j}{4} \right] \\
 & + \frac{dG_\sigma^2}{2} \sum_{i \neq j \neq k} \delta^2(ijk) - \frac{d^2G_\sigma^3}{2} \sum_{i \neq j \neq k \neq l} \delta^3(ijkl) \\
 & + \frac{i}{4M^2} \sum_{i \neq j} A_{ij} \vec{\nabla}_i \delta(\vec{R}_{ij}) \times \vec{\nabla}_i \cdot \vec{\sigma}_i,
 \end{aligned}$$

Guichon and Thomas, Phys. Rev. Lett. 93, 132502 (2004)

# Derivation of Density Dependent Effective Force

Physical origin of density dependent forces of Skyrme type within the quark meson coupling model

P.A.M. Guichon <sup>a,\*</sup>, H.H. Matevosyan <sup>b,c</sup>, N. Sandulescu <sup>a,d,e</sup>,  
A.W. Thomas <sup>b</sup>

Nuclear Physics A 772 (2006) 1–19

- **Start with classical theory of MIT-bag nucleons with structure modified in medium to give  $M_{\text{eff}}(\sigma)$ :**

$$E = \sum_i \left( \sqrt{P_i^2 + M_{\text{eff}}(\sigma)^2} + g_\omega \omega + V_{\text{so}} \right) + E_{\text{mesons}}$$

**where:**

$$E_{\text{mesons}} = \frac{1}{2} \int d\vec{r} [(\nabla \sigma)^2 + m_\sigma^2 \sigma^2] - \frac{1}{2} \int d\vec{r} [(\nabla \omega)^2 + m_\omega^2 \omega^2]$$

# Derivation of effective Force (cont.)

- Nucleon Effective Mass in-medium is:

$$M_{\text{eff}}(\sigma) = M - g_{\sigma}\sigma + \frac{d}{2}(g_{\sigma}\sigma)^2$$

and the  $\sigma$ N coupling constant in free space is:

$$g_{\sigma} = 3g_{\sigma}^q \int_{\text{Bag}} d\vec{r} \bar{q}q(\vec{r})$$

The classical Hamiltonian is:

$$H(R_i, P_i) = E(R_i, P_i, \sigma \rightarrow \sigma_{\text{sol}}, \omega \rightarrow \omega_{\text{sol}})$$

where  $\frac{\delta E}{\delta \sigma} = \frac{\delta E}{\delta \omega} = 0$  yields  $\sigma_{\text{sol}}, \omega_{\text{sol}}$

- Include fluctuations and expand in  $\delta\sigma$ ; quantise nucleon motion; make non-relativistic expansion...

# Derivation of effective Force (cont.)

- We get the Hamiltonian of the system. We use the Hartree-Fock approximation to evaluate the energy functional (in which case  $\langle \delta \sigma \rangle = 0$  ). The result is:

$$\langle H(\vec{r}) \rangle = \rho M + \frac{\tau}{2M} + \mathcal{H}_0 + \mathcal{H}_3 + \mathcal{H}_{\text{eff}} + \mathcal{H}_{\text{fin}} + \mathcal{H}_{\text{so}}$$

where, if we define ( $m = p, n$ ):

$$\vec{J}_m(\vec{r}) = i \sum_{i \in F} \sum_{\sigma \sigma'} \vec{\sigma}_{\sigma' \sigma} \times [\vec{\nabla} \Phi^i(\vec{r}, \sigma, m)] \Phi^{i*}(\vec{r}, \sigma', m)$$

the pieces are summarised on the next page.

# Derivation of effective Force (cont.)

$$\mathcal{H}_0 + \mathcal{H}_3 = \rho^2 \left[ \frac{-3G_\rho}{32} + \frac{G_\sigma}{8(1 + d\rho G_\sigma)^3} - \frac{G_\sigma}{2(1 + d\rho G_\sigma)} + \frac{3G_\omega}{8} \right] \\ + (\rho_n - \rho_p)^2 \left[ \frac{5G_\rho}{32} + \frac{G_\sigma}{8(1 + d\rho G_\sigma)^3} - \frac{G_\omega}{8} \right],$$

$$\mathcal{H}_{\text{eff}} = \left[ \left( \frac{G_\rho}{8m_\rho^2} - \frac{G_\sigma}{2m_\sigma^2} + \frac{G_\omega}{2m_\omega^2} + \frac{G_\sigma}{4M_N^2} \right) \rho_n + \left( \frac{G_\rho}{4m_\rho^2} + \frac{G_\sigma}{2M_N^2} \right) \rho_p \right] \tau_n \\ + p \leftrightarrow n,$$

$$\mathcal{H}_{\text{fin}} = \left[ \left( \frac{3G_\rho}{32m_\rho^2} - \frac{3G_\sigma}{8m_\sigma^2} + \frac{3G_\omega}{8m_\omega^2} - \frac{G_\sigma}{8M_N^2} \right) \rho_n \right. \\ \left. + \left( \frac{-3G_\rho}{16m_\rho^2} - \frac{G_\sigma}{2m_\sigma^2} + \frac{G_\omega}{2m_\omega^2} - \frac{G_\sigma}{4M_N^2} \right) \rho_p \right] \nabla^2(\rho_n) + p \leftrightarrow n,$$

$$\mathcal{H}_{\text{so}} = \nabla \cdot J_n \left[ \left( \frac{-3G_\sigma}{8M_N^2} - \frac{3G_\omega(-1 + 2\mu_s)}{8M_N^2} - \frac{3G_\rho(-1 + 2\mu_v)}{32M_N^2} \right) \rho_n \right. \\ \left. + \left( \frac{-G_\sigma}{4M_N^2} + \frac{G_\omega(1 - 2\mu_s)}{4M_N^2} \right) \rho_p \right] + p \leftrightarrow n.$$

**Note the totally new, subtle density dependence**

# Global search on Skyrme forces

## The Skyrme Interaction and Nuclear Matter Constraints

M. Dutra, O. Lourenço, J. S. S. Martins, and A. Delfino

*Departamento de Física - Universidade Federal Fluminense,  
Av. Litorânea s/n, 24210-150 Boa Viagem, Niterói RJ, Brazil*

J. R. Stone

*Department of Physics, University of Oxford,  
OX1 3PU Oxford, United Kingdom and*

*Department of Physics and Astronomy,  
University of Tennessee, Knoxville, Tennessee 37996, USA*

C. Providência

*Centro de Física Computacional,*

*Department of Physics,*

*University of Coimbra,*

*P-3004-516 Coimbra, Portugal*

**Phys. Rev. C85 (2012) 035201**

**These authors tested 233  
widely used Skyrme-type forces  
against 12 standard nuclear  
properties: only 17 survived  
including two QMC potentials**

Furthermore, we considered weaker constraints arising from giant resonance experiments on isoscalar and isovector effective nucleon mass in SNM and BEM, Landau parameters and low-mass neutron stars. If these constraints are taken into account, the number of CSkP reduces to to 9, GSkI, GSkII, KDE0v1, LNS, NRAPR, **QMC700, QMC750** and SKRA, the CSkP\* list.

**Truly remarkable – force derived from quark level does  
a better job of fitting nuclear structure constraints than  
phenomenological fits with many times # parameters!**

# Systematic Study of Finite Nuclei



# Systematic approach to finite nuclei

( This work is *in preparation* for publication: collaborators are J.R. Stone, P.A.M. Guichon and P. G. Reinhard)

- Allow 3 basic quark-meson couplings to vary so that nuclear matter properties reproduced within errors

$$-17 < E/A < -15 \text{ MeV}$$

$$0.14 < \rho_0 < 0.18 \text{ fm}^{-3}$$

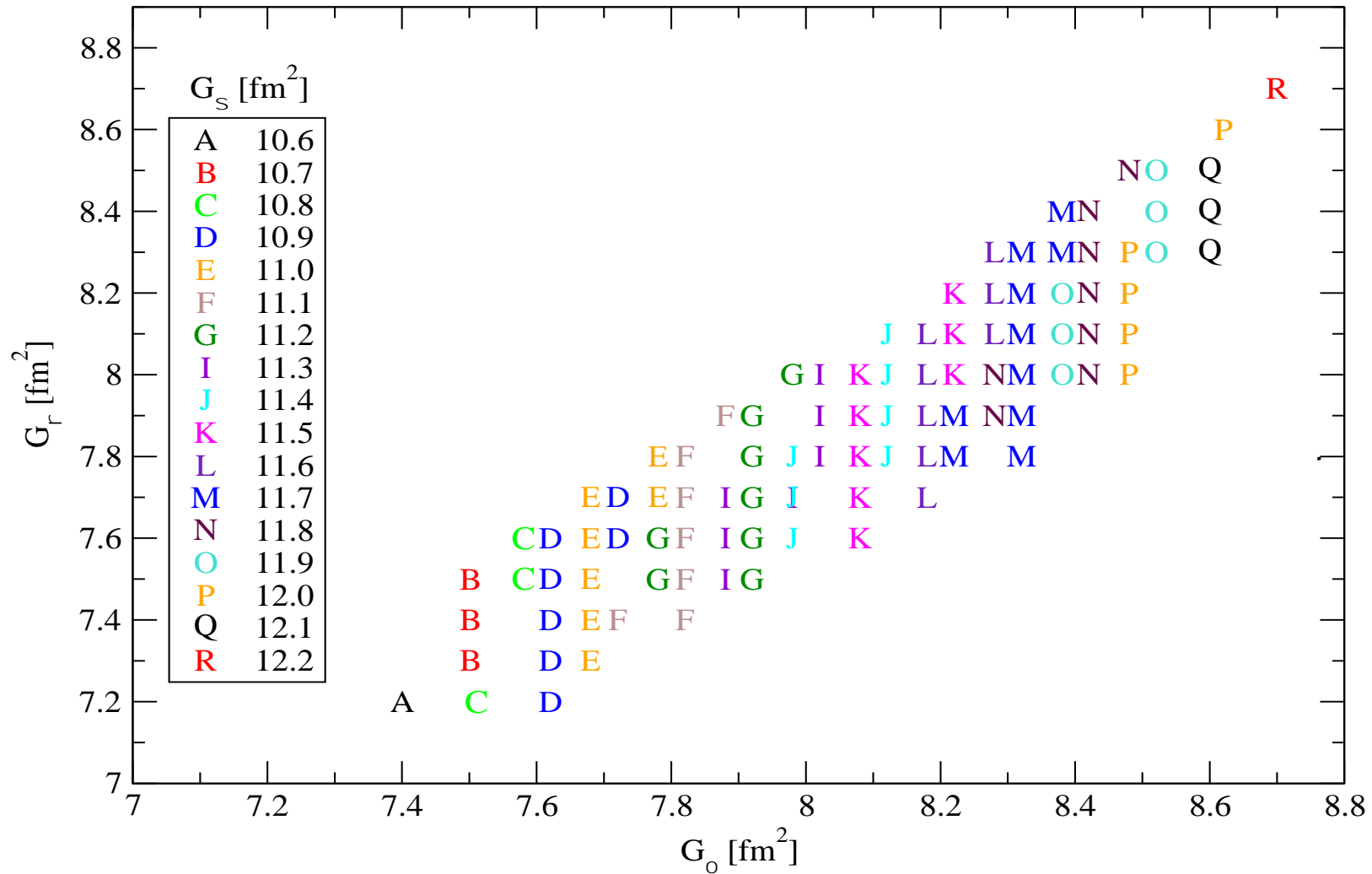
$$28 < S_0 < 34 \text{ MeV}$$

$$L > 20 \text{ MeV}$$

$$250 < K_0 < 350 \text{ MeV}$$

- Fix at overall best description of finite nuclei

# Overview of Allowed Parameters



# Overview of Nuclei Studied – Across Periodic Table

Element	Z	N	Element	Z	N
C	6	6 - 16	Pb	82	116 - 132
O	8	4 - 20	Pu	94	134 - 154
Ca	20	16 - 32	Fm	100	148 - 156
Ni	28	24 - 50	No	102	152 - 154
Sr	38	36 - 64	Rf	104	152 - 154
Zr	40	44 - 64	Sg	106	154 - 156
Sn	50	50 - 86	Hs	108	156 - 158
Sm	62	74 - 98	Ds	110	160
Gd	64	74 - 100			

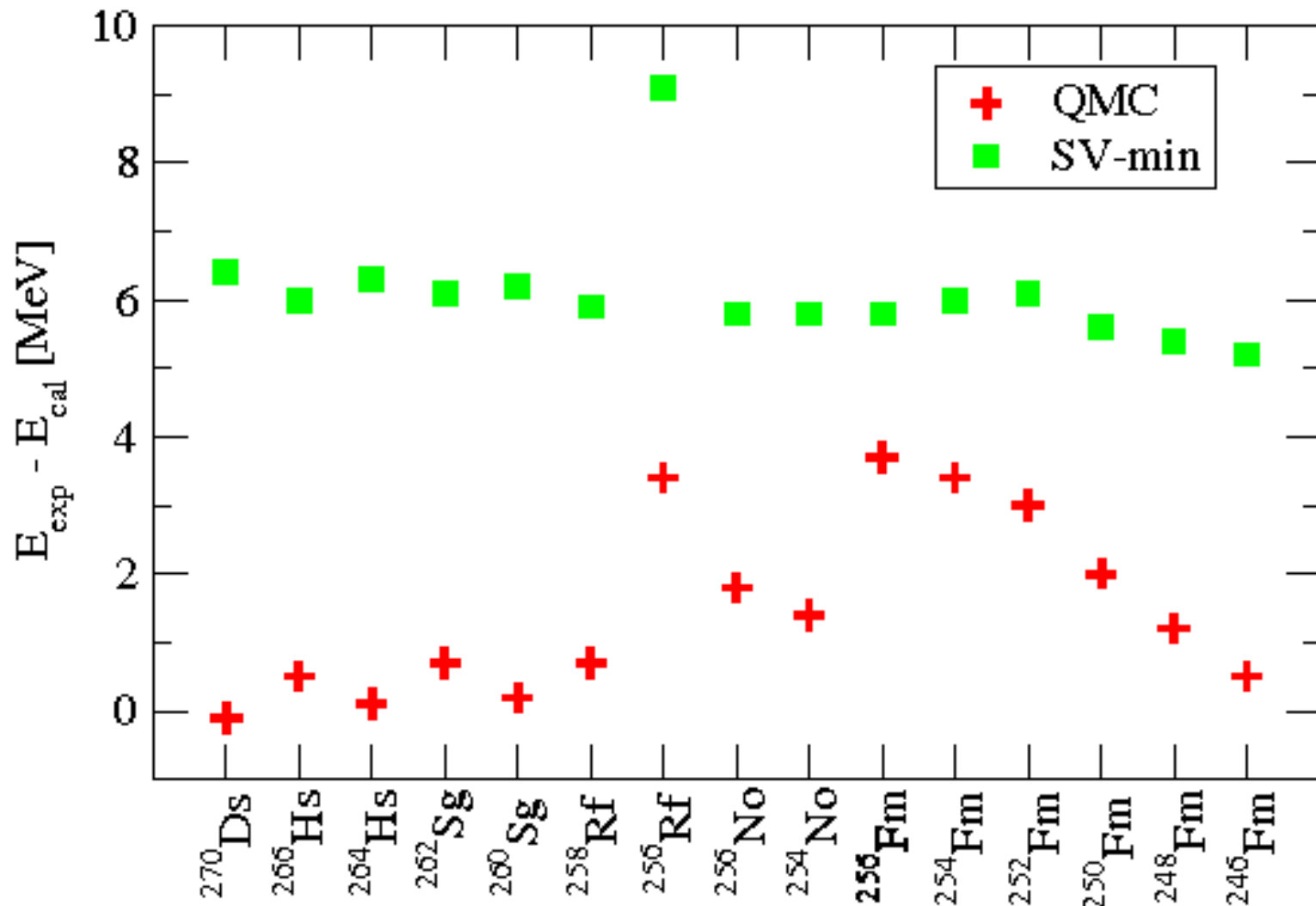
N	Z	N	Z
20	10 - 24	64	36 - 58
28	12 - 32	82	46 - 72
40	22 - 40	126	76 - 92
50	28 - 50		

**i.e. We look at most challenging cases of p- or n-rich nuclei**

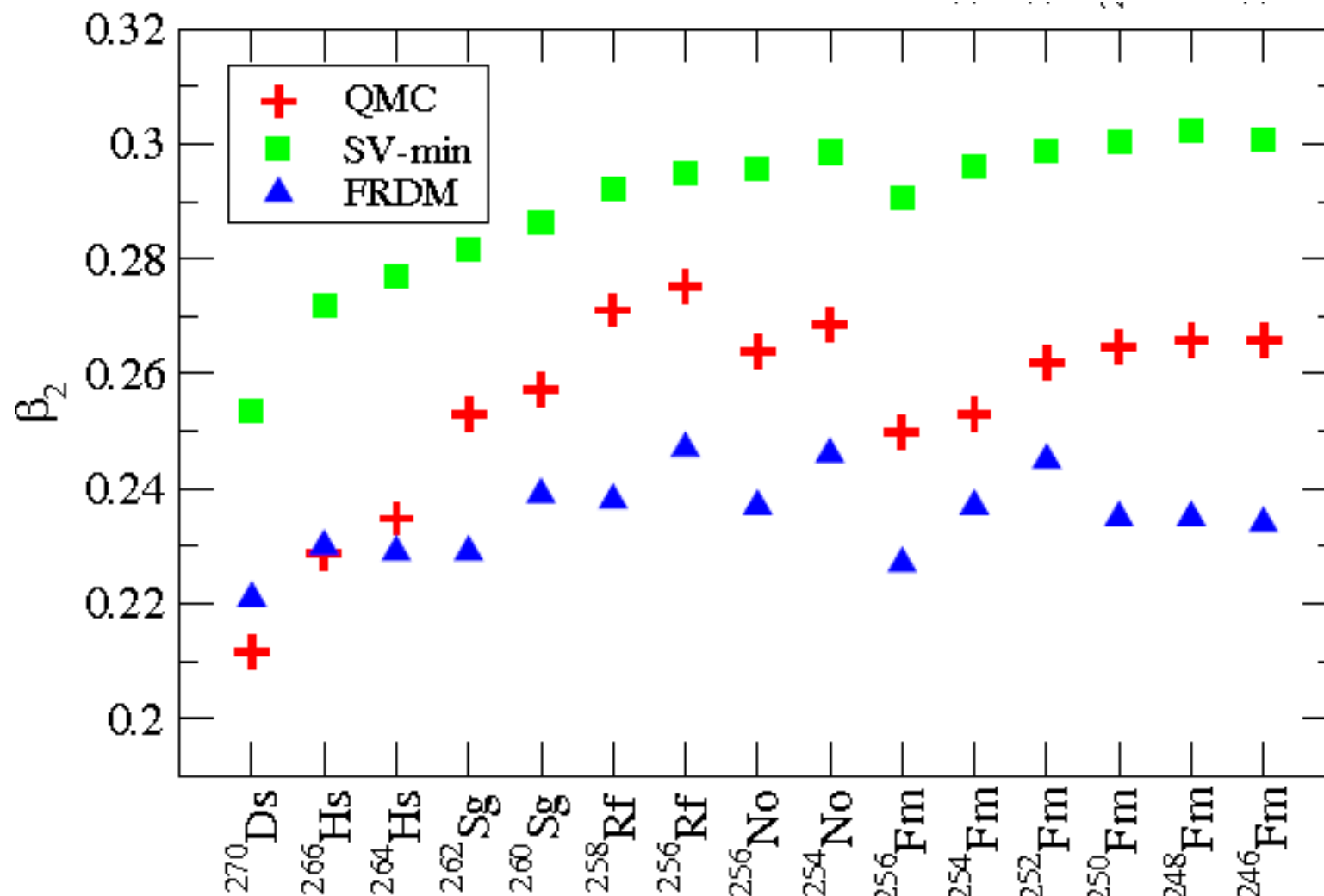
# Overview

data	rms error %	
	QMC	SV-min
fit nuclei:		
binding energies	<u>0.36</u>	0.24
diffraction radii	1.62	0.91
surface thickness	10.9	2.9
rms radii	0.71	0.52
pairing gap (n)	57.6	17.6
pairing gap (p)	25.3	15.5
1s splitting: proton	15.8	18.5
1s splitting: neutron	20.3	16.3
superheavy nuclei:	<u>0.1</u>	0.3
N=Z nuclei	1.17	0.75
mirror nuclei	1.50	1.00
other	0.35	0.26

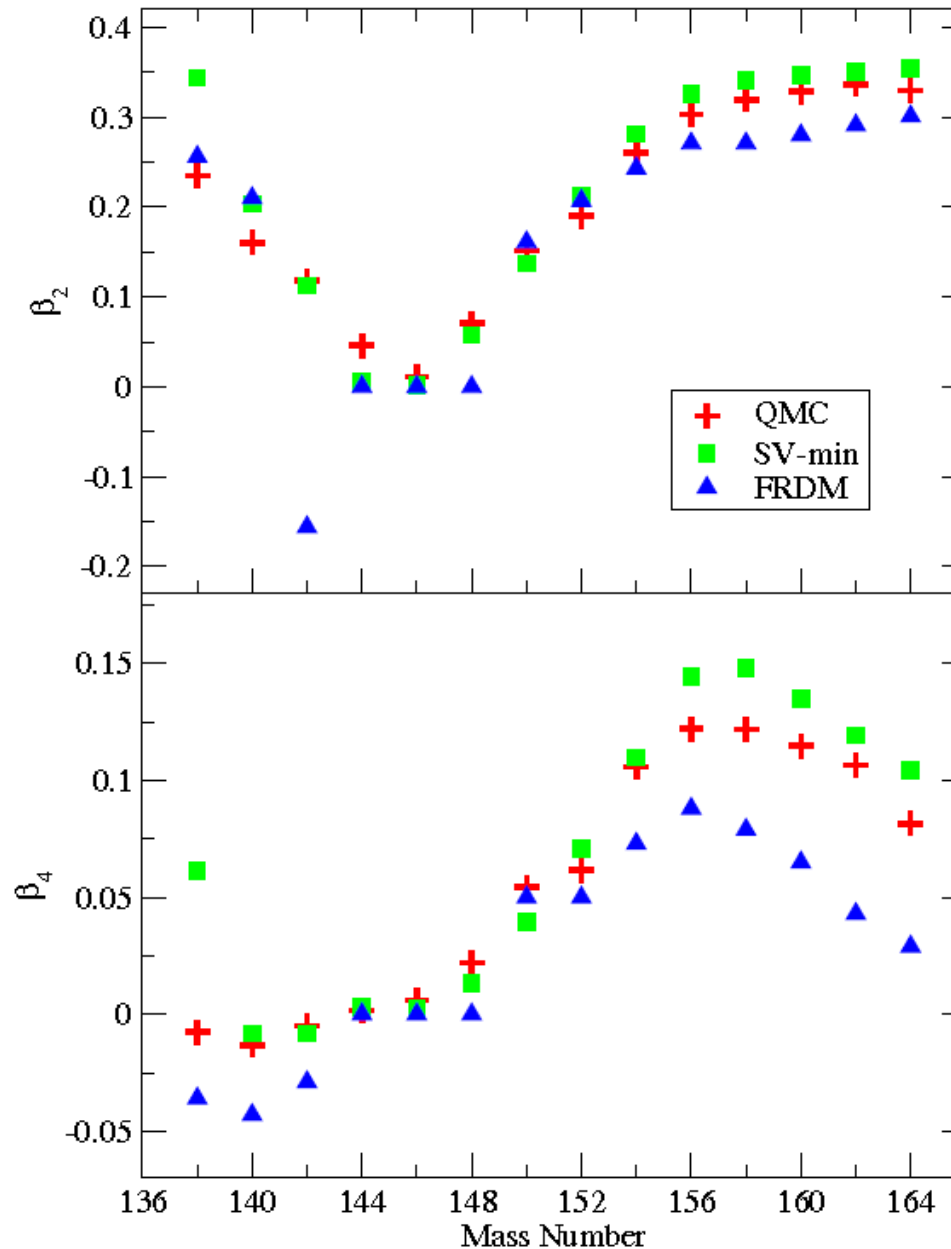
# Superheavies : 0.1% accuracy



# Quadrupole Deformation of Superheavies



# Deformation in Gd (Z=64) Isotopes

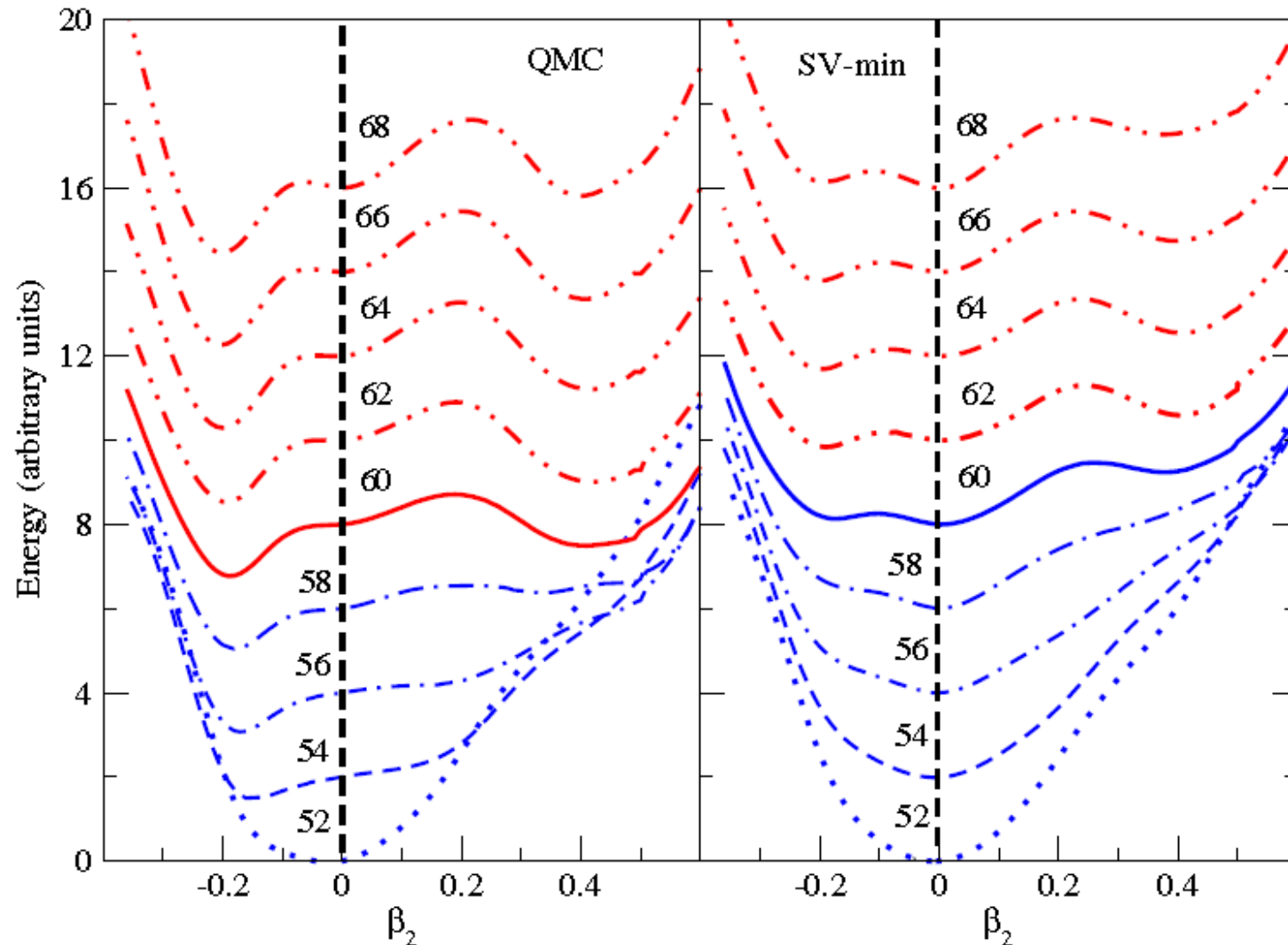


# Spin-orbit splitting

Element		States	Exp [keV]	QMC [keV]	SV-bas [keV]
O16	proton	$1p_{1/2} - 1p_{3/2}$	6.3 (1.3)a)	5.8	5.0
	neutron	$1p_{1/2} - 1p_{3/2}$	6.1 (1.2)a)	5.7	5.1
Ca40	proton	$1d_{3/2} - 1d_{5/2}$	7.2 <sup>b)</sup>	6.3	5.7
	neutron	$1d_{3/2} - 1d_{5/2}$	6.3 <sup>b)</sup>	6.3	5.8
Ca48	proton	$1d_{3/2} - 1d_{5/2}$	4.3 <sup>b)</sup>	6.3	5.2
	neutron	$1d_{3/2} - 1d_{5/2}$		5.3	5.2
Sn132	proton	$2p_{1/2} - 2p_{3/2}$	1.35(27) <sup>a)</sup>	1.32	1.22
	neutron	$2p_{1/2} - 2p_{3/2}$	1.65(13) <sup>a)</sup>	1.47	1.63
	neutron	$2d_{3/2} - 2d_{5/2}$		2.71	2.11
Pb208	proton	$2p_{1/2} - 2p_{3/2}$		0.91	0.93
	neutron	$3p_{1/2} - 3p_{3/2}$	0.90(18) <sup>a)</sup>	1.11	0.89



# Shape evolution of Zr (Z=40) Isotopes



- Shape co-existence sets in at N=60
- Usually difficult to describe – e.g. Mei et al., PRC85, 034321 (2012)

# Summary: Finite Nuclei

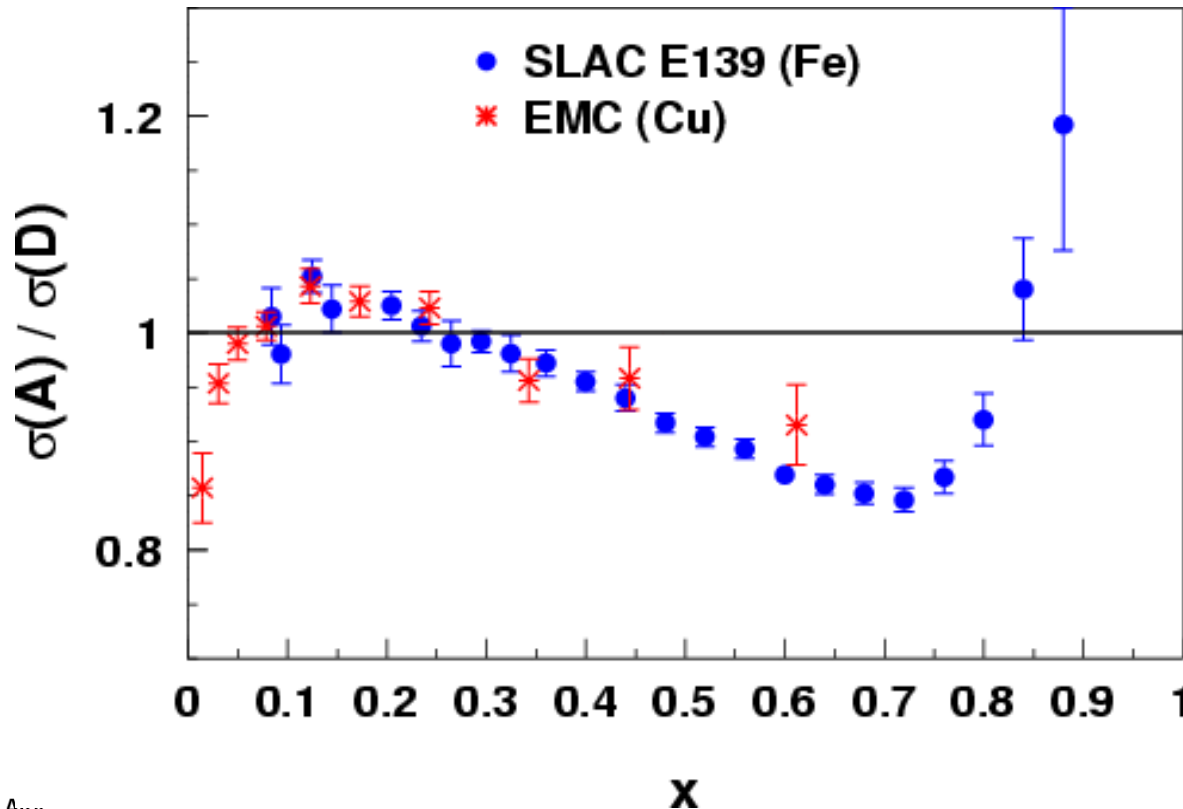
- The effective force was *derived* at the quark level *based upon changing structure of bound nucleon*
- Has many less parameters but reproduces nuclear properties at a level comparable with the best phenomenological Skyrme forces
- Looks like standard nuclear force
- BUT underlying theory also predicts modified internal structure and hence modified
  - DIS structure functions
  - elastic form factors.....

# Nuclear DIS Structure Functions

**To address questions like this one MUST start with a theory that quantitatively describes nuclear structure – very, very few examples.....**

# The EMC Effect: Nuclear PDFs

- Observation stunned and electrified the HEP and Nuclear communities 30 years ago
- Nearly 1,000 papers have been generated.....
- What is it that alters the quark momentum in the nucleus?



J. Ashman *et al.*, Z. Phys. C57, 211 (1993)

J. Gomez *et al.*, Phys. Rev. D49, 4348 (1994)

# Theoretical Understanding

- Still numerous proposals but few consistent theories
- Initial studies used MIT bag<sup>1</sup> to estimate effect of self-consistent change of structure in-medium  
– but better to use a covariant theory
- For that Bentz and Thomas<sup>2</sup> re-derived change of nucleon structure in-medium in the NJL model
- This set the framework for sophisticated studies by Cloët and collaborators over the last decade

<sup>1</sup> Thomas, Michels, Schreiber and Guichon, Phys. Lett. B233 (1989) 43

<sup>2</sup> Bentz and Thomas, Nucl. Phys. A696 (2001) 138

# Calculations for Finite Nuclei

(Spin dependent EMC effect TWICE as large as unpolarized)

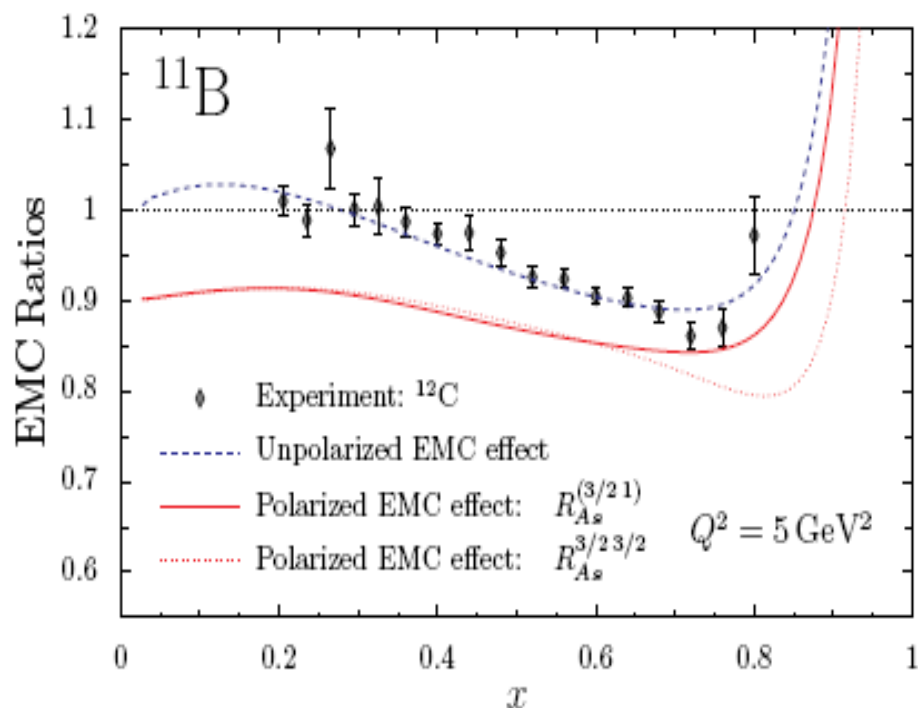


FIG. 7: The EMC and polarized EMC effect in  $^{11}\text{B}$ . The empirical data is from Ref. [31].

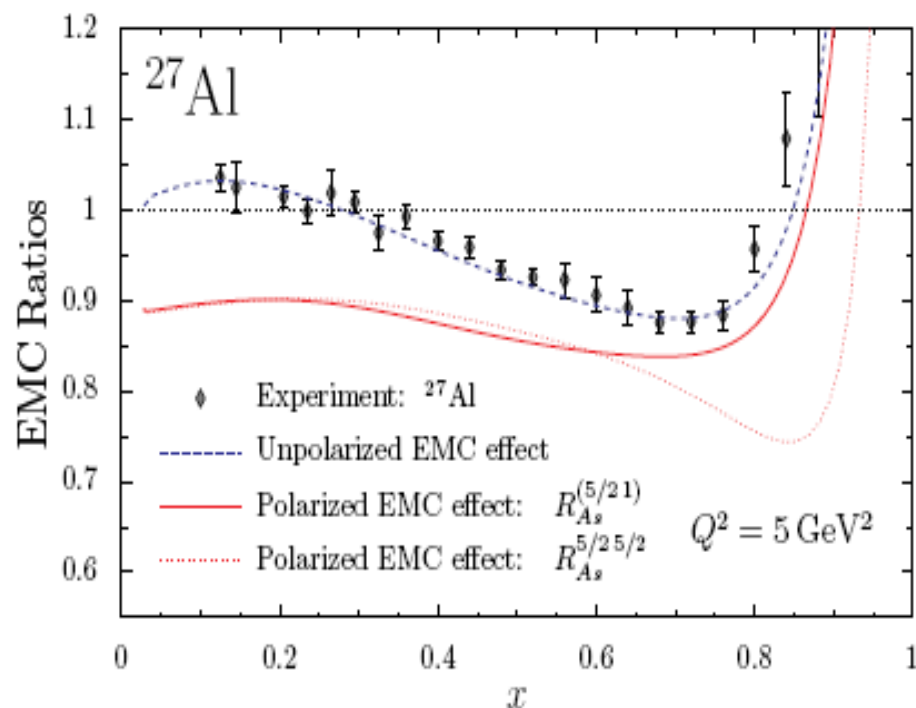
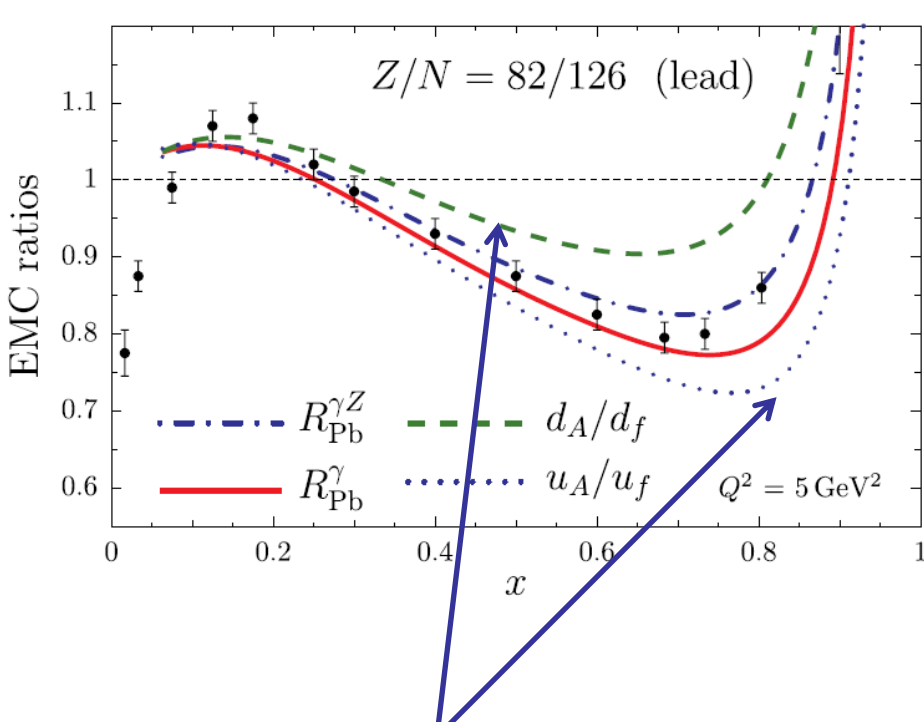


FIG. 9: The EMC and polarized EMC effect in  $^{27}\text{Al}$ . The empirical data is from Ref. [31].

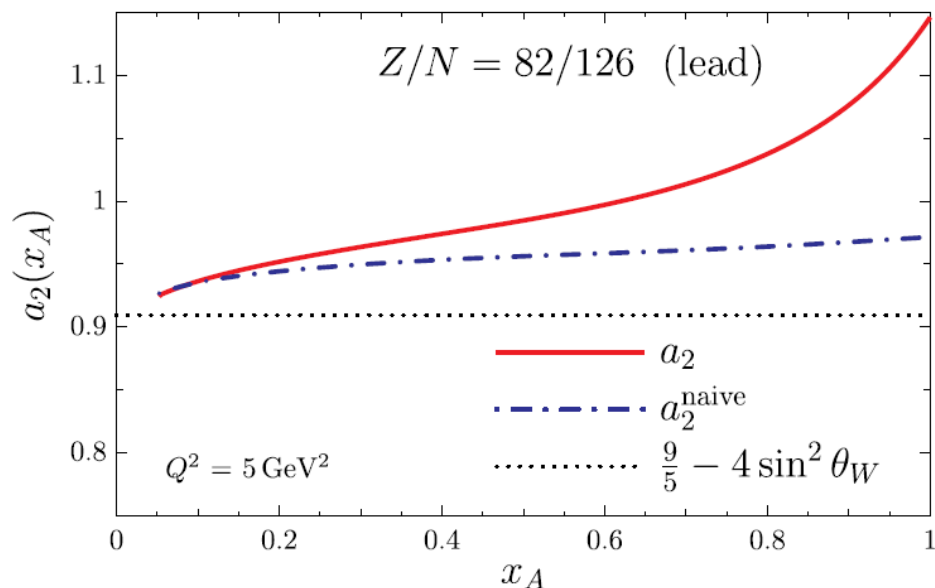
Cloët, Bentz & Thomas, Phys. Lett. B642 (2006) 210 (nucl-th/0605061)

# Parity-Violating Deep Inelastic Scattering and the Flavor Dependence of the EMC Effect

I. C. Cloët,<sup>1</sup> W. Bentz,<sup>2</sup> and A. W. Thomas<sup>1</sup>



$$A_{\text{PV}} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha_{\text{em}}} \left[ a_2(x_A) + \frac{1 - (1 - y)^2}{1 + (1 - y)^2} a_3(x_A) \right]$$



**Ideally tested at EIC with CC reactions**

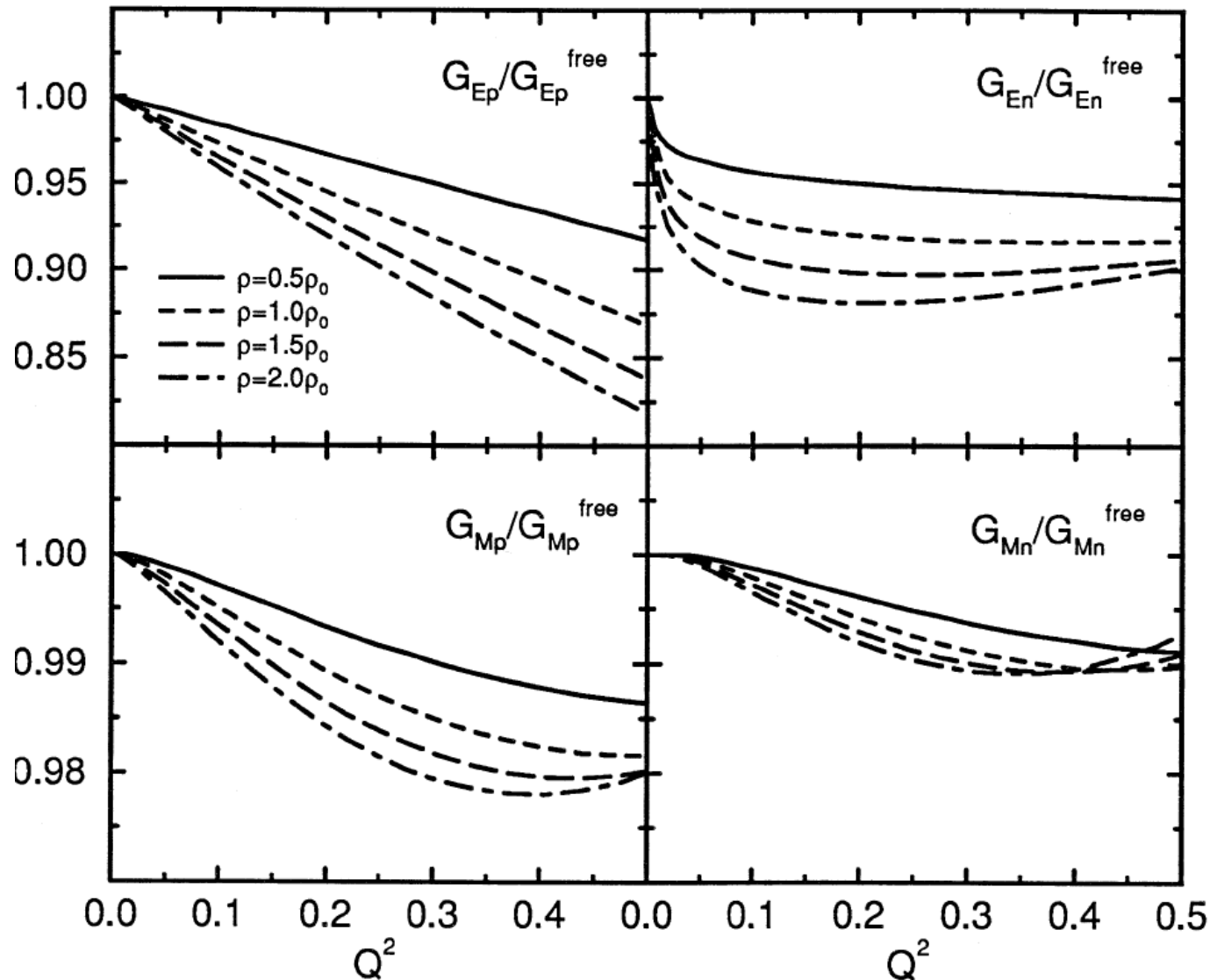
**Parity violating EMC will be tested at JLab 12 GeV**

# Modified Electromagnetic Form Factors In-Medium



# In-medium electron-nucleon scattering

D.H. Lu <sup>a</sup>, A.W. Thomas <sup>a</sup>, K. Tsushima <sup>a</sup>, A.G. Williams <sup>a</sup>, K. Saito

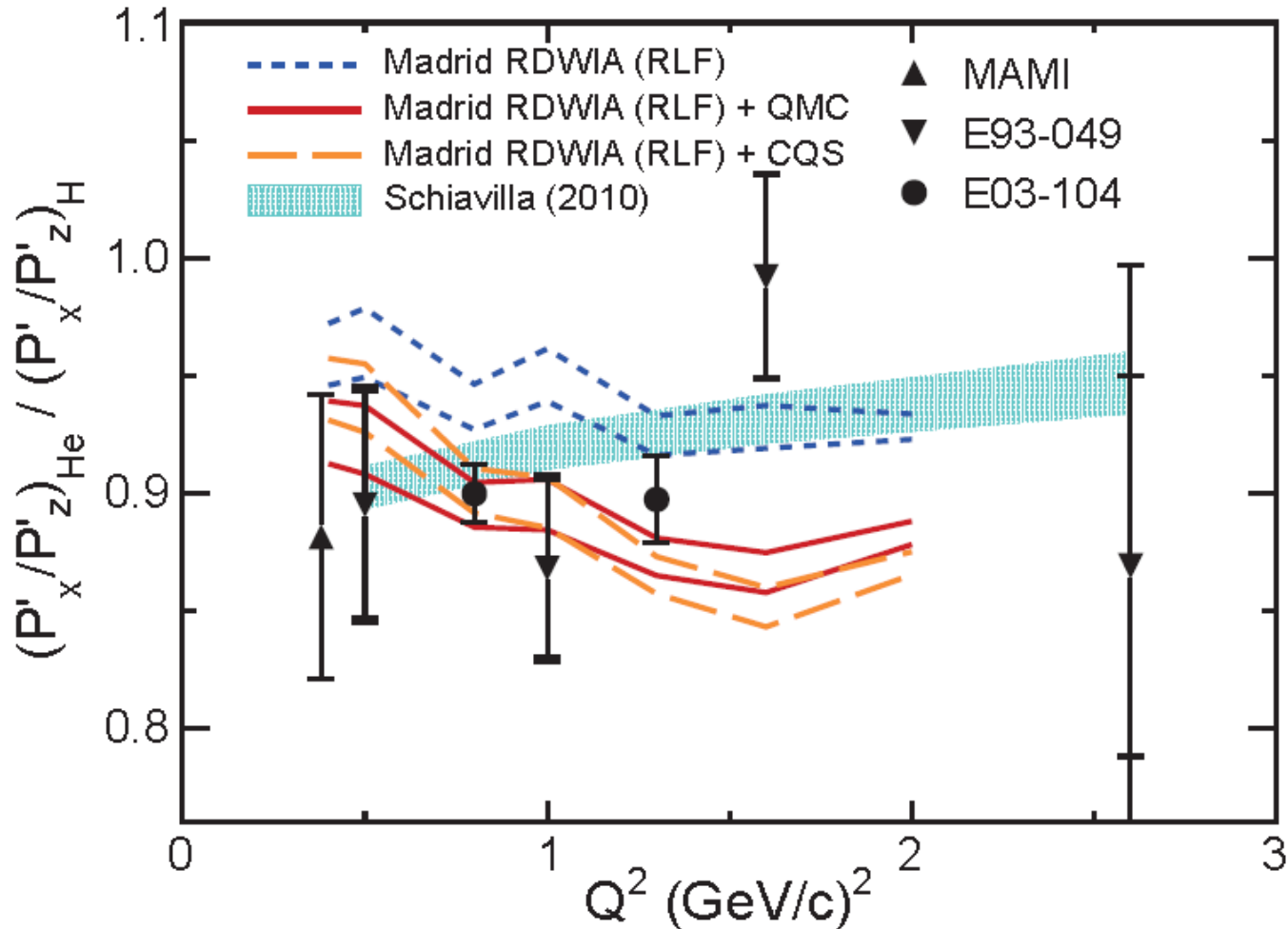


QMC

# Jefferson Lab & Mainz

Strauch et al., EPJ Web of Conf. 36 (2012) 00016

Polarized  
 $^4\text{He}(\vec{e}, e' \vec{p})$   
 measuring  
 recoil p  
 polarization  
 (T/L :  $G_E/G_M$ )

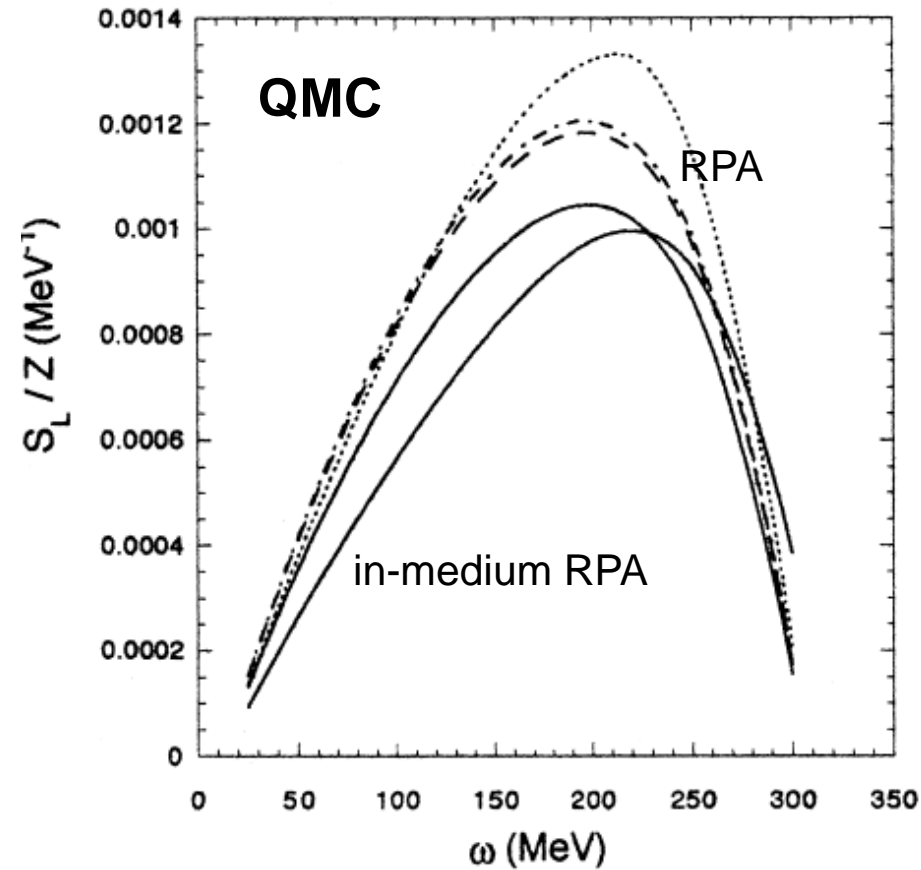
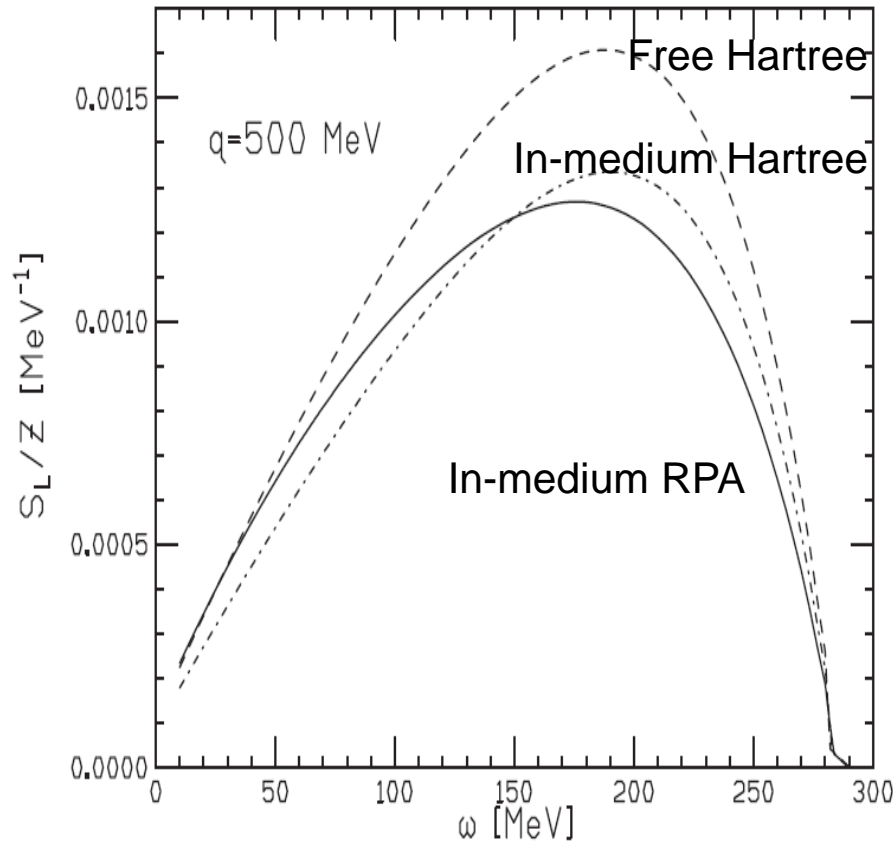


**QMC medium effect predicted more than  
 a decade years before the experiment  
 (D.H. Lu et al., Phys. Lett. B 417 (1998) 217)**

# Longitudinal response function

– revisited in expectation of new results from JLab, Meziani et al.

*K. Saito et al. / Physics Letters B 465 (1999) 27–35*



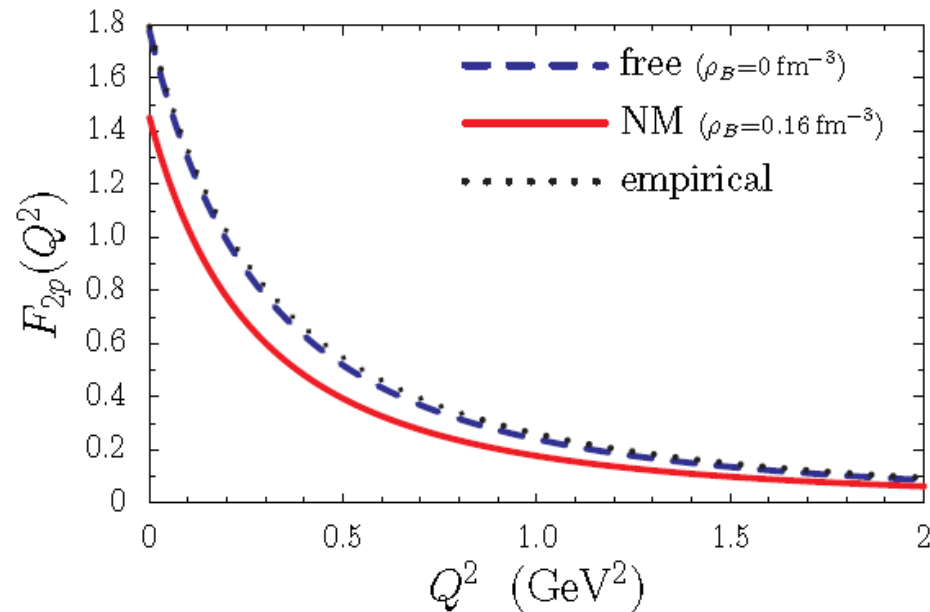
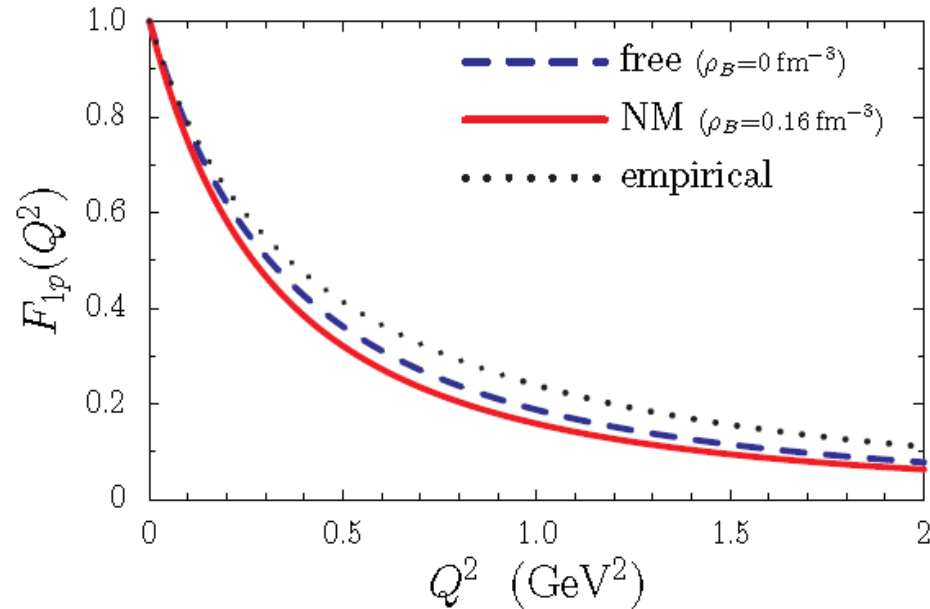
Horikawa and Bentz, nucl-th/0506021

# Recent Calculations Motivated by:

**E01-015, PR-04-015 – Chen, Choi & Meziani**

- Using NJL model with nucleon structure self-consistently solved in-medium
- Same model describing free nucleon form factors, structure functions and EMC effect

# Modification of Proton Form Factors



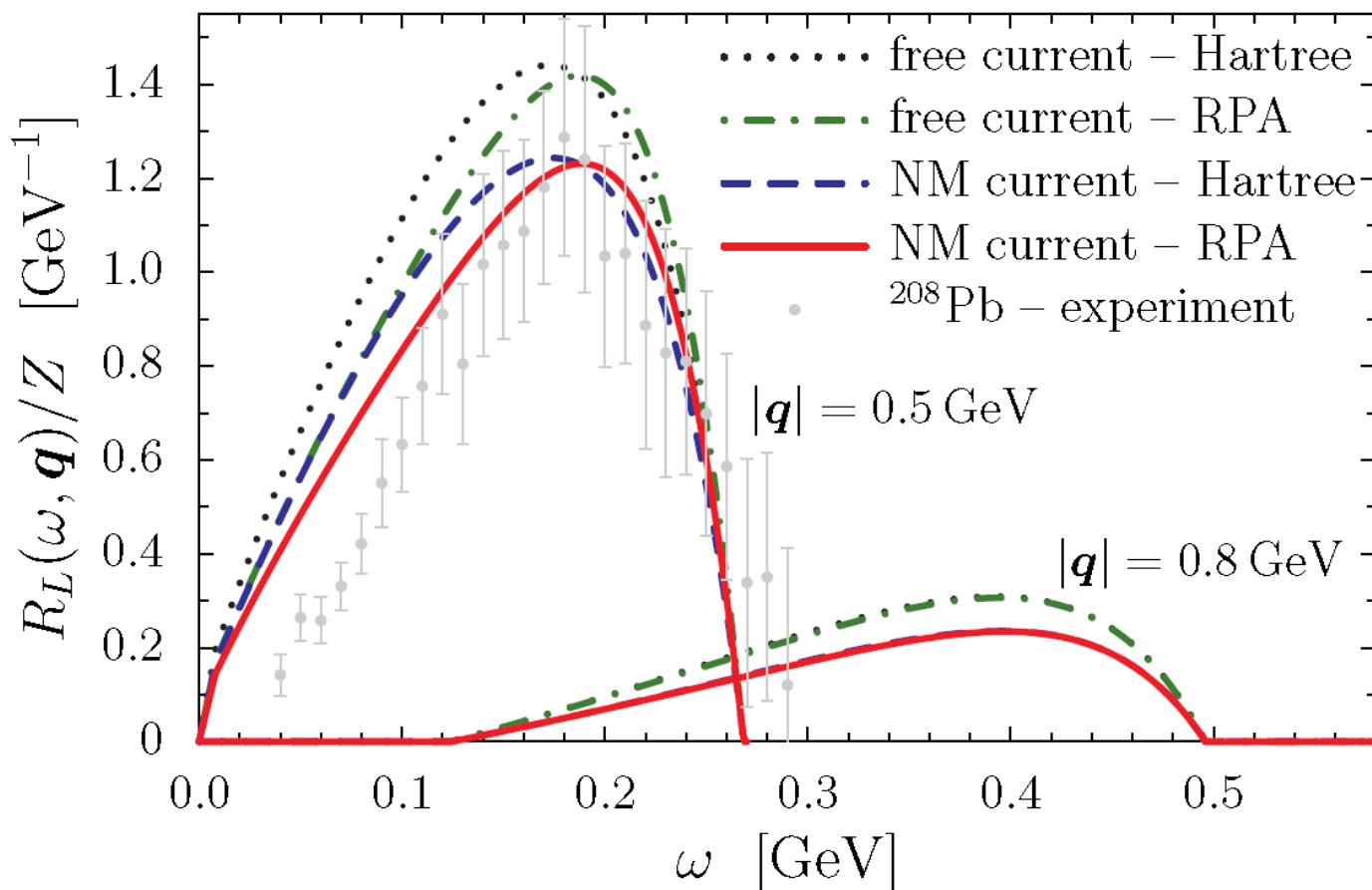
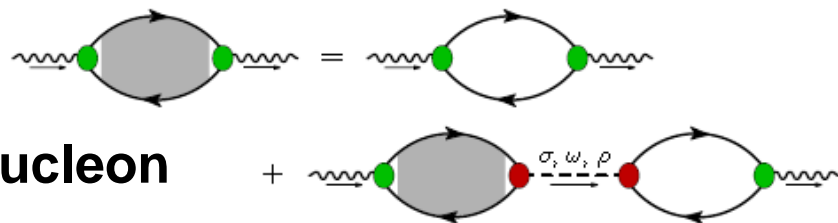
**Free nucleon  
form factors  
Bentz *et al.*  
Phys Rec C90,  
045202 (2014)**

**Cloët *et al.*, arXiv:1405.5542**

# Response Function

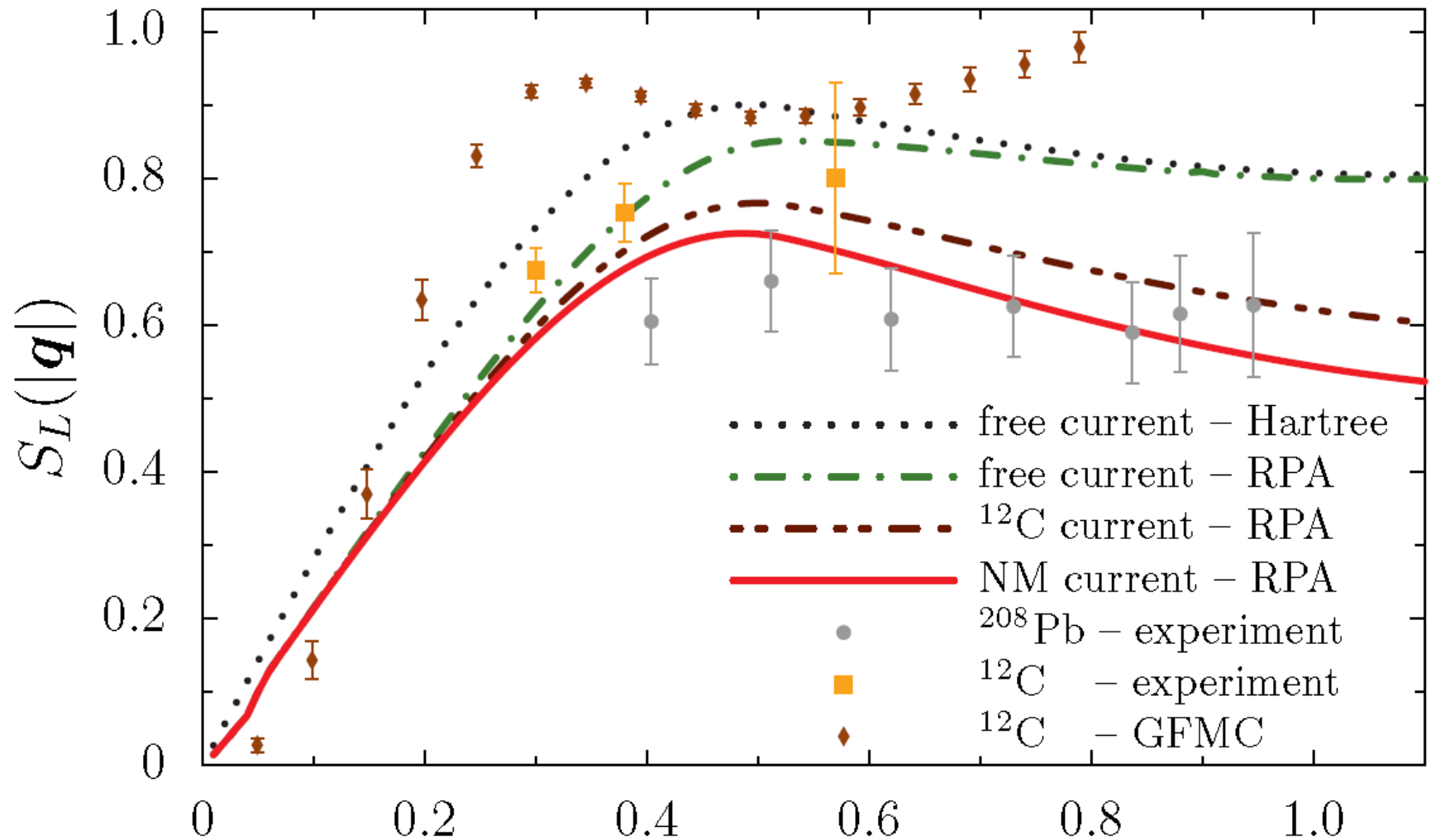
**RPA correlations repulsive**  
**Significant reduction in Response**  
**Function from modification of bound-nucleon**

$$\frac{d^2\sigma}{d\Omega d\omega} = \sigma_{\text{Mott}} \left[ \frac{q^4}{|q|^4} R_L(\omega, |q|) + \left( \frac{q^2}{2|q|^2} + \tan^2 \frac{\theta}{2} \right) R_T(\omega, |q|) \right]$$



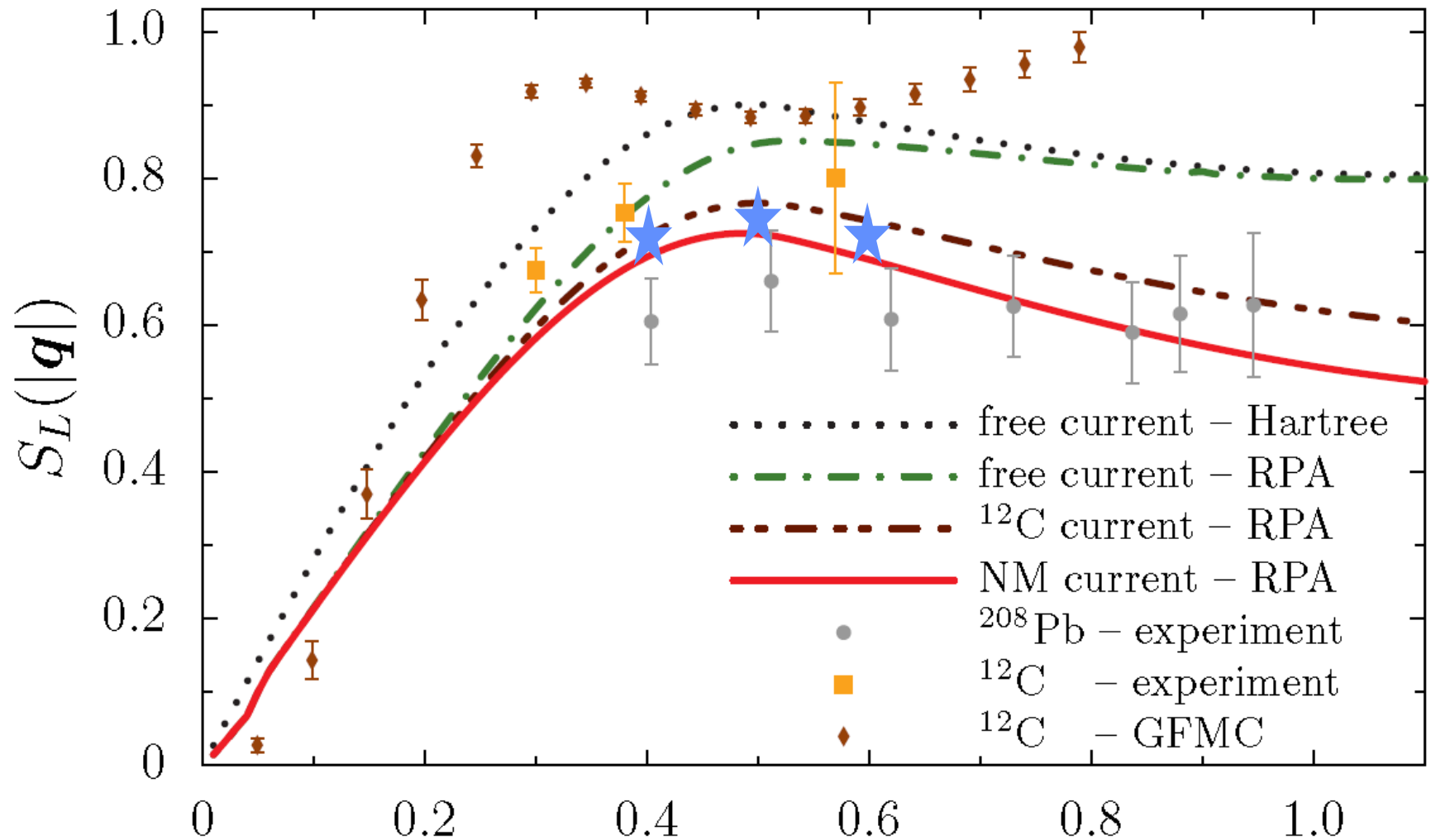
**Cloët, Bentz & Thomas ( arXiv:1506.05875)**

# Comparison with Unmodified Nucleon & Data



$$S_L(|q|) = \int_{\omega+}^{|q|} d\omega \frac{R_L(\omega, |q|)}{Z G_{Ep}^2(Q^2) + N G_{En}^2(Q^2)} |q| \text{ [GeV]}$$

# and these predictions are stable!



$$S_L(|q|) = \int_{\omega+}^{|q|} d\omega \frac{R_L(\omega, |q|)}{Z G_{Ep}^2(Q^2) + N G_{En}^2(Q^2)} \quad |q| \text{ [GeV]}$$

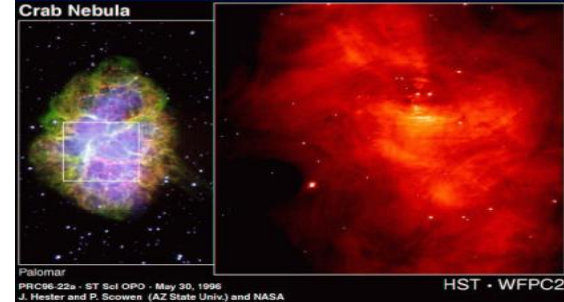
★ Saito et al., QMC 1999  
(op cit)

Data: Morgenstern & Meziani

Calculations: Cloët, Bentz & Thomas (arXiv:1506.05875)



# Summary



- Intermediate range NN attraction **STRONG** Lorentz scalar
- This modifies the intrinsic structure of the bound nucleon
  - profound change in shell model :  
what occupies shell model states are **NOT** free nucleons
- Scalar polarizability is a natural source of three-body force/ density dependence of effective forces
  - clear physical interpretation
- Derived, density-dependent effective force gives results better than most phenomenological Skyrme forces

# Summary

- **Initial systematic study of finite nuclei very promising**
  - Binding energies typically within 0.5% or better across periodic table
- **Super-heavies ( $Z > 100$ ) especially good (typically better than 0.25%)!**
- **Deformation, spin-orbit splitting and charge distributions all look good (NOT fit – only binding)**
- **BUT need empirical confirmation:**
  - Response Functions & Coulomb sum rule (soon)
  - Isovector EMC effect; spin EMC etc....
- Lattice QCD etc. : any clever ideas?

# Special Mentions.....



**Guichon**



**Tsushima**



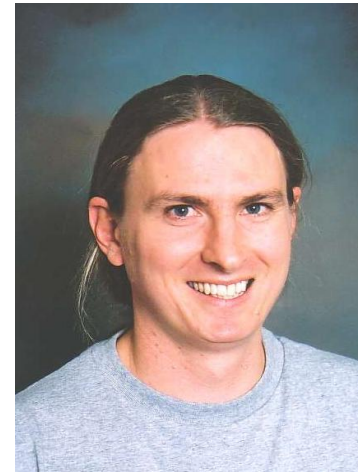
**Saito**



**Stone**



**Bentz**

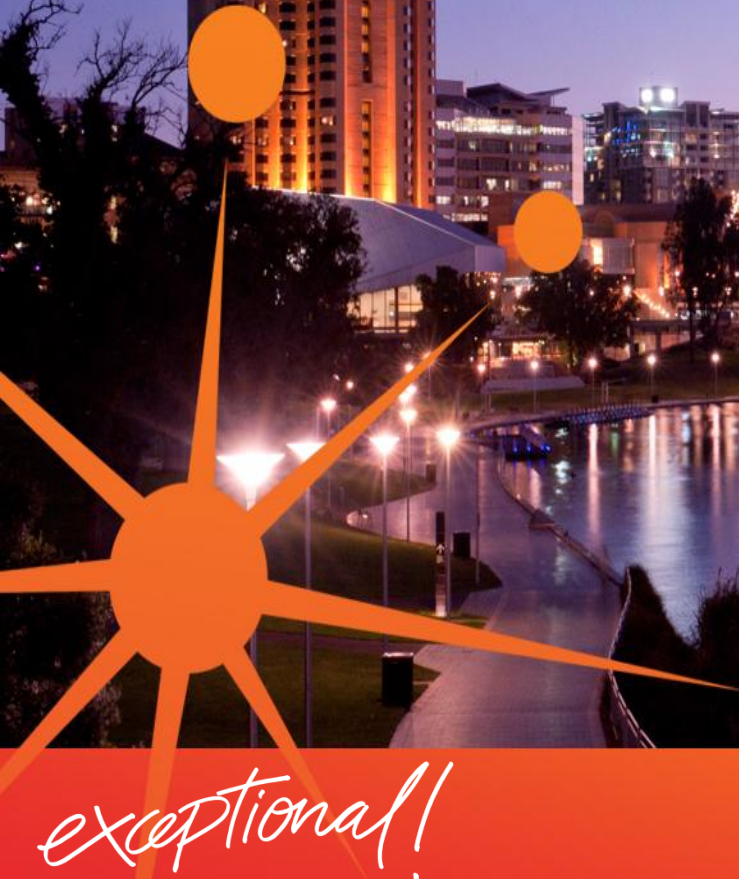


**Cloët**



We look forward to welcoming delegates to  
Adelaide, Australia for INPC 2016

September 11-16 2016



*exceptional!*



# Key papers on QMC

- **Two major, recent papers:**

1. Guichon, Matevosyan, Sandulescu, Thomas, Nucl. Phys. A772 (2006) 1.
2. Guichon and Thomas, Phys. Rev. Lett. 93 (2004) 132502

- **Built on earlier work on QMC: e.g.**

3. Guichon, Phys. Lett. B200 (1988) 235
4. Guichon, Saito, Rodionov, Thomas, Nucl. Phys. A601 (1996) 349

- **Major review of applications of QMC to many nuclear systems:**

5. Saito, Tsushima, Thomas, Prog. Part. Nucl. Phys. 58 (2007) 1-167 (hep-ph/0506314)

# References to: Covariant Version of QMC

- **Basic Model: (Covariant, chiral, confining version of NJL)**
- **Bentz & Thomas, Nucl. Phys. A696 (2001) 138**
- **Bentz, Horikawa, Ishii, Thomas, Nucl. Phys. A720 (2003) 95**
- **Applications to DIS:**
- **Cloet, Bentz, Thomas, Phys. Rev. Lett. 95 (2005) 052302**
- **Cloet, Bentz, Thomas, Phys. Lett. B642 (2006) 210**
- **Applications to neutron stars – including SQM:**
- **Lawley, Bentz, Thomas, Phys. Lett. B632 (2006) 495**
- **Lawley, Bentz, Thomas, J. Phys. G32 (2006) 667**

# Can we Measure Scalar Polarizability in Lattice QCD ?

- IF we can, then in a real sense we would be linking nuclear structure to QCD itself, because scalar polarizability is sufficient in simplest, relativistic mean field theory to produce saturation
- Initial ideas on this published :  
the trick is to apply a chiral invariant scalar field  
– do indeed find polarizability opposing applied  $\sigma$  field

**18<sup>th</sup> Nishinomiya Symposium: nucl-th/0411014**  
– published in Prog. Theor. Phys.

# Most recent nuclear structure results

- **Results obtained using SKYAX code of P. G. Reinhard**
- **2 BCS pairing parameters (density dependent, contact pairing force) fitted from pairing gaps in Sn isotopes**



