

XV J. A. Swieca School and SPSAS Nanophotonics- Campinas July, 2016

High-order nonlinearities in disordered media

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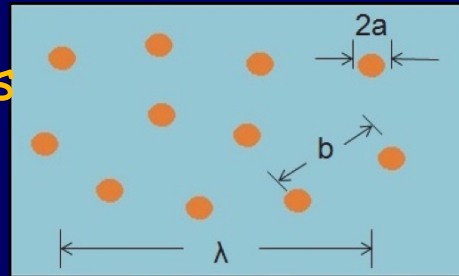
Second lecture

Transverse high-order nonlinear phenomena in
composites

Metal-dielectric nanocomposites

Nanoparticles

Dielectric

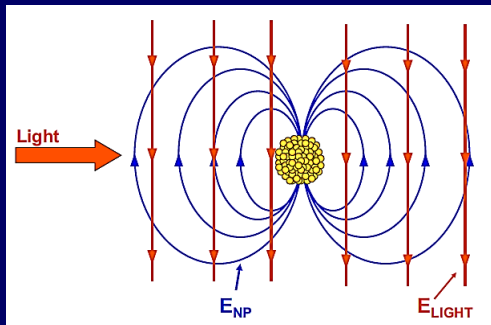
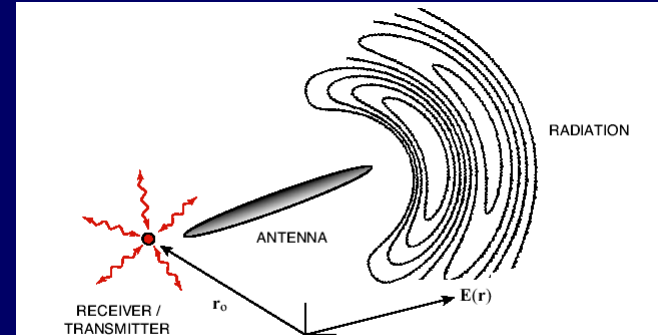


- Glasses (bulk and thin films) with metallic NPs
- Polymers with metallic nanostructures
- Liquid colloids with metallic NPs

Optical response is controlled through the volume fraction of the NPs

Why metal-dielectric nanocomposites?

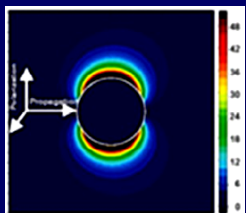
Metallic NPs as optical nanoantennas



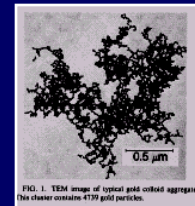
$$E_{local} = \eta E_{light}$$

$$\eta = \frac{3\epsilon_{NP}(\omega)}{\epsilon_{NP}(\omega) + 2\epsilon_h(\omega)}$$

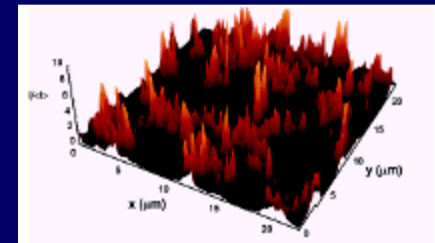
$$\text{Re} [\epsilon(\omega_{sp}) + 2\epsilon_m(\omega_{sp})] = 0$$



Localized
Surface
Plasmons

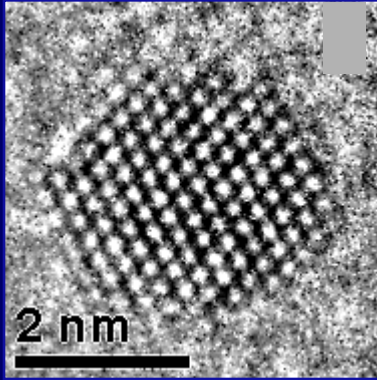


Fractals
and
hot-spots

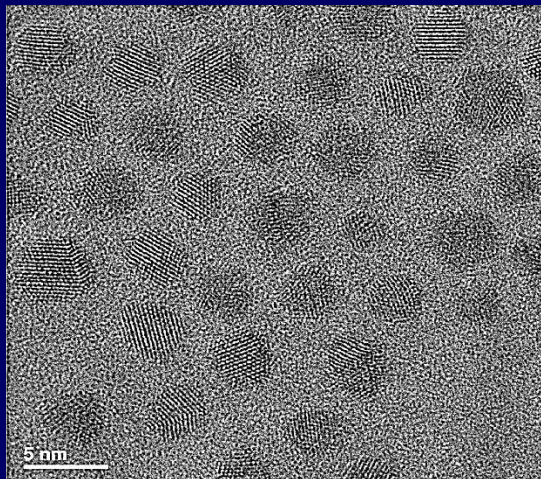
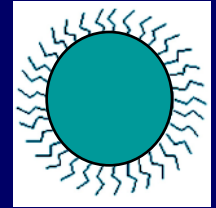


Optical response may be enhanced due to the NPs

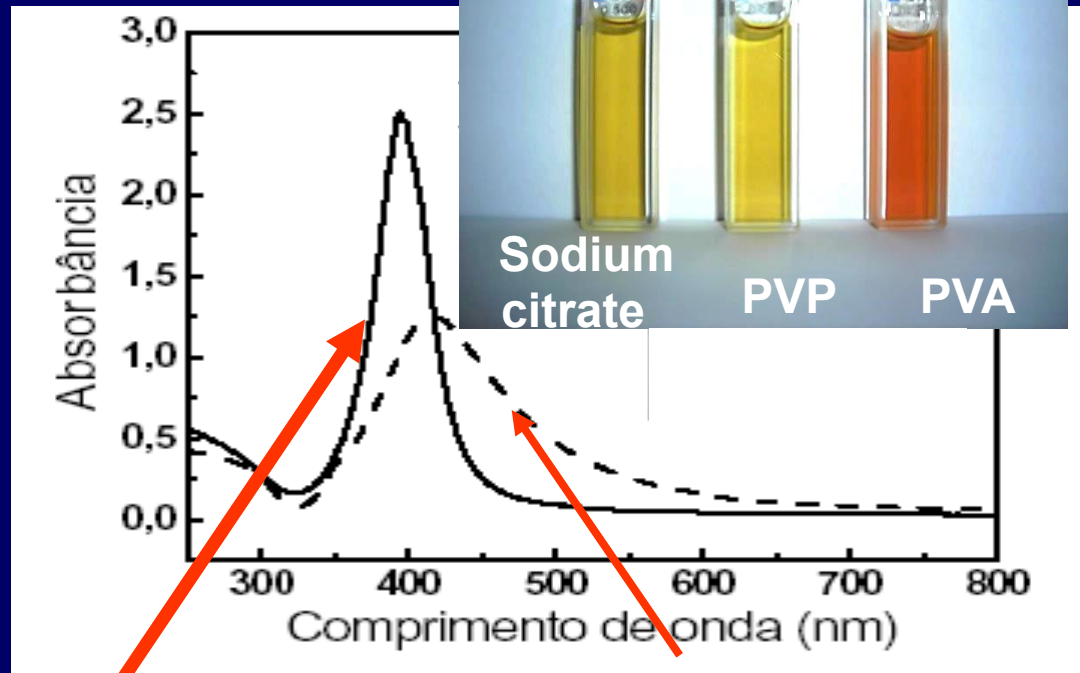
Colloids with Ag spherical NPs



Stabilizing agents to prevent aggregation



diameter: 4 nm
 ≈ 1500 atoms
 $\approx 30\%$ in the surface

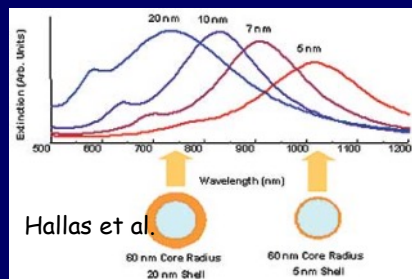


spheres

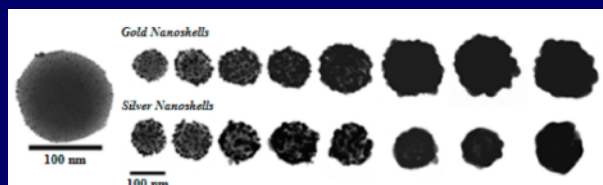
several shapes
and sizes

Metallic nanoshells

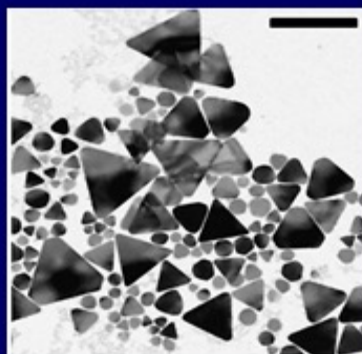
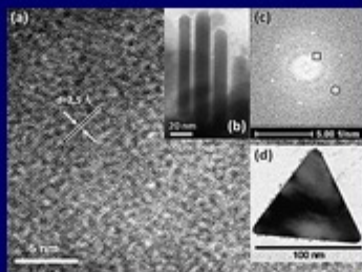
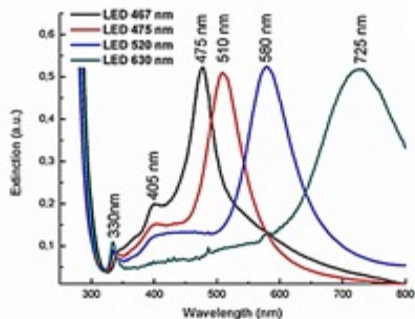
Plasmon frequency depends on the ratio between the shell thickness and the core radius



Langmuir 2013
29, 4366-4372



Silver Nanoprisms



High-order nonlinearity of silica-gold nanoshells in chloroform at 1560 nm

Falcão-Filho et al.
Opt. Express 18 (2010) 21616

Improved synthesis of gold and silver nanoshells

Brito-Silva et al.
Langmuir 29 (2013) 4366

Synthesis of silver nanoprisms:
A photochemical approach
using light emission diodes

Saade, de Araújo
Mater. Chem. Phys. 148 (2014) 1184

Large optical nonlinearity and fast response

Fast response is due to the
induced dipole relaxation

Surface plasmon optical dephasing, T_2

Measured using the "Persistent Hole-Burning Technique"

$$T_2 < 3fs$$

T_2 is influenced by the environment

Nonlinear optics of a nanocomposite

$$P_L + P_{NL} = \epsilon_0 \sum_{N=0}^{\infty} \chi_{eff}^{(2N+1)} E^{(2N+1)}$$

Centro-symmetric media
 $\chi_{eff}^{(\text{even})} = 0$

Effective 3rd. order
susceptibility

$$\chi_{eff}^{(3)} = f L^2 |L|^2 \chi_{np}^{(3)} + \chi_h^{(3)},$$

Local field
factor

$$L = 3\epsilon_h^{(L)} / (\epsilon_{np}^{(L)} + 2\epsilon_h^{(L)})$$

Nonlinear response depends strongly on the laser frequency

$$n_2 \propto \text{Re} \chi_{eff}^{(3)}$$

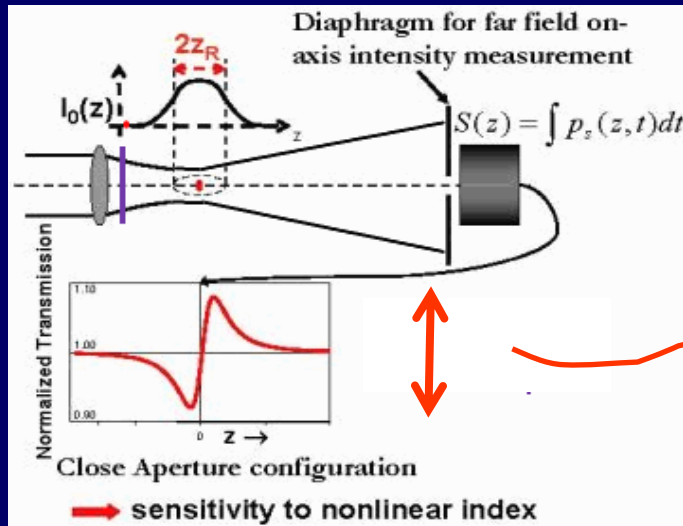
Nonlinear refraction

$$\alpha_2 \propto \text{Im} \chi_{eff}^{(3)}$$

Nonlinear absorption

When high-order nonlinearities are present:

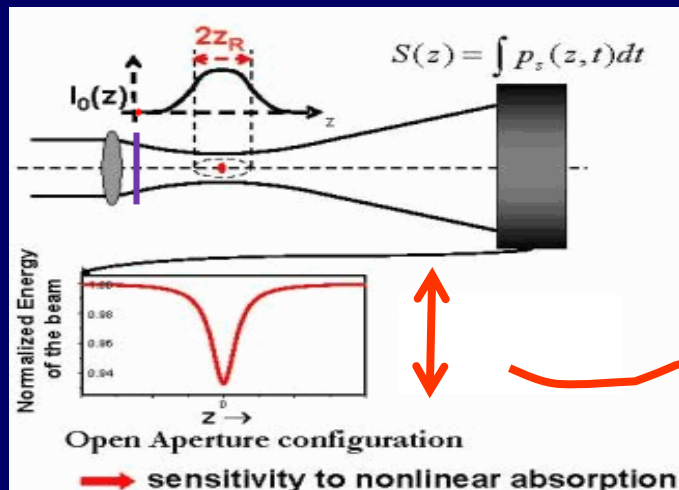
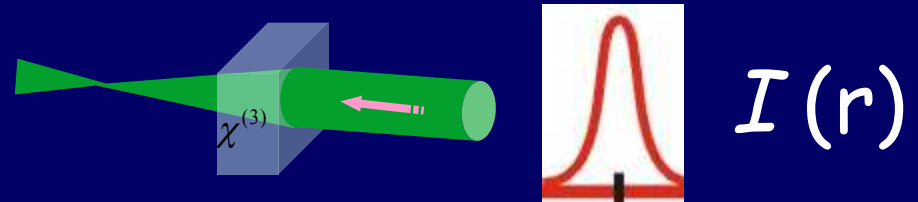
Self - focusing medium



NL refraction

"Closed-aperture" Z scan

$$\Delta T \propto n_2 I + n_4 I^2 + n_6 I^3 + \dots$$

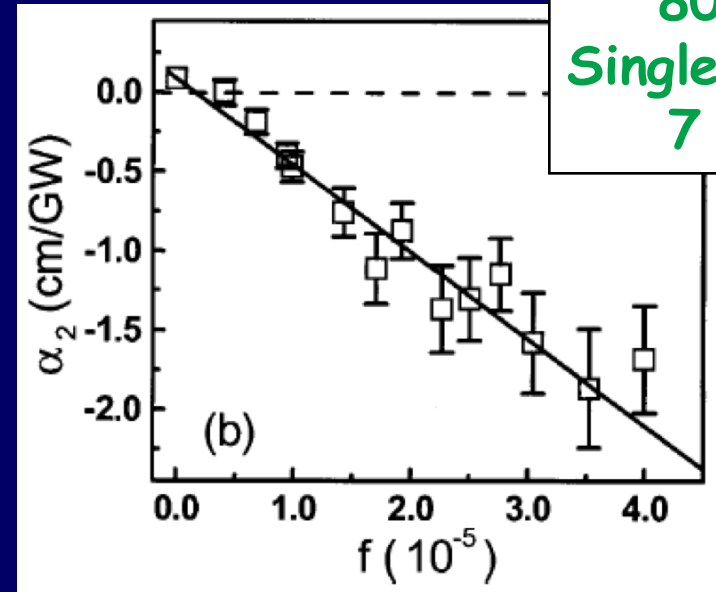
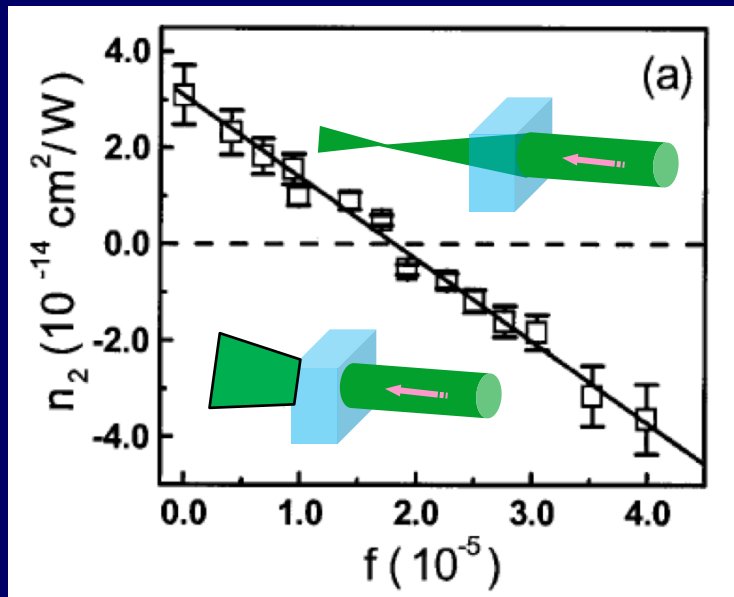


NL absorption

"Open-aperture" Z scan

$$\Delta T \propto \alpha_2 I + \alpha_4 I^2 + \alpha_6 I^3 + \dots$$

Silver NPs in CS₂



532 nm
80 ps
Single pulses
7 Hz

$$\chi_{eff}^{(3)} \approx f(2.3 + i1.0)\chi_{NP}^{(3)} + \chi_{host}^{(3)}$$

$$n_2 \propto \left\{ f(2.3 \operatorname{Re} \chi_{NP}^{(3)} - 1.0 \operatorname{Im} \chi_{NP}^{(3)}) + \operatorname{Re} \chi_{host}^{(3)} \right\}$$

$$\alpha_2 \propto \left\{ f(2.3 \operatorname{Im} \chi_{NP}^{(3)} + 1.0 \operatorname{Re} \chi_{NP}^{(3)}) + \operatorname{Im} \chi_{host}^{(3)} \right\}$$

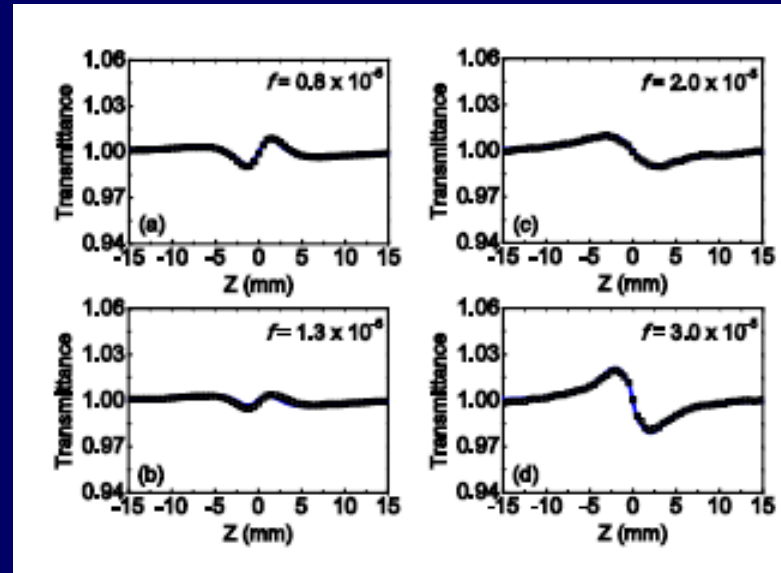
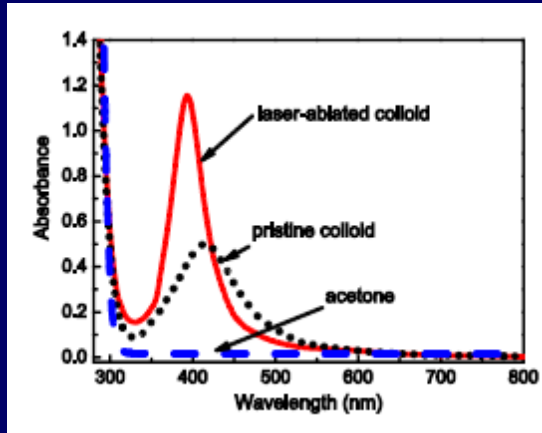
This experiment

$$\chi_{host}^{(3)} = 2.9 \times 10^{-20} + i3.5 \times 10^{-22} (m/V)^2$$

$$\chi_{NP}^{(3)} = -(6.3 - i1.9) \times 10^{-16} (m/V)^2$$

Observation of fifth-order refraction in a metal-colloid

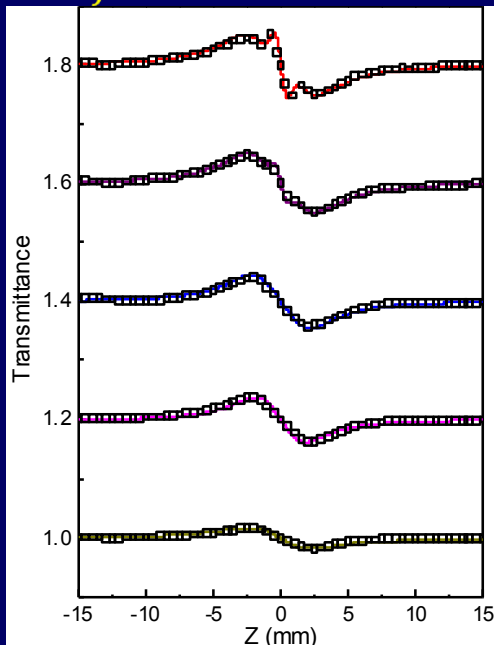
Silver NPs in acetone



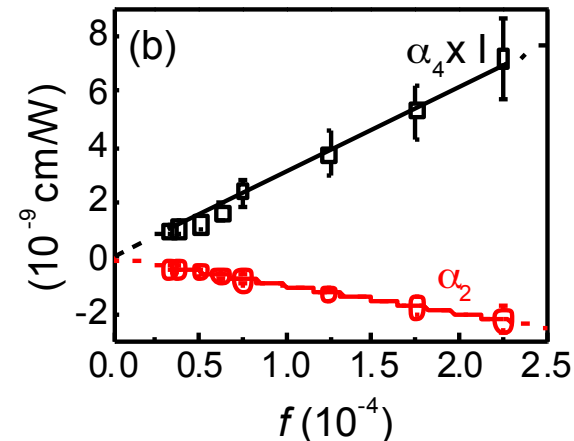
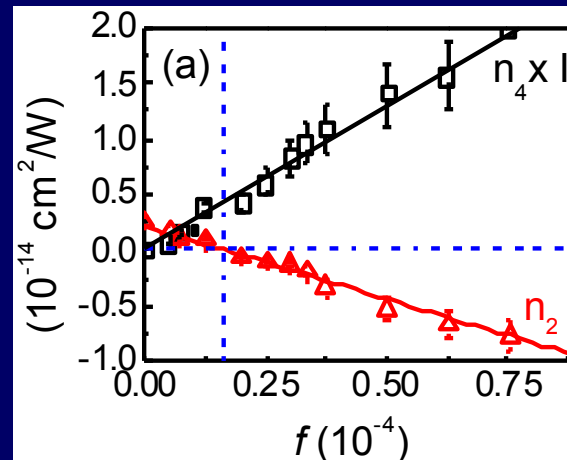
Z-scan

532 nm
Single pulses
5 GW/cm²

$f = 5.0 \times 10^{-5}$

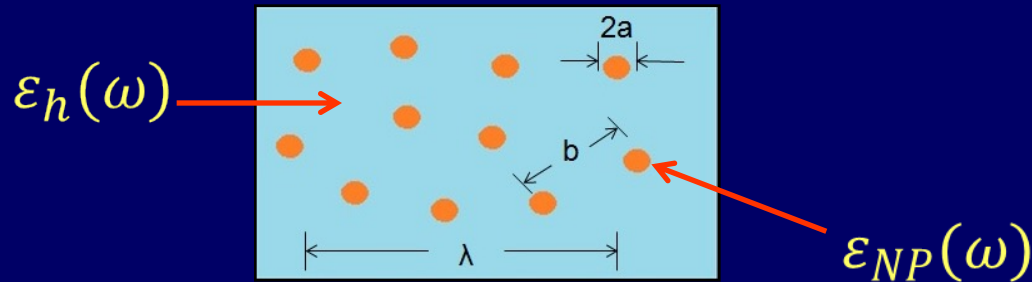


9
8
6
4
2
GW/cm²



9 GW/cm²

Generalized Maxwell-Garnet model



Ag NPs in acetone

$\chi_{host}^{(5)}$ – negligible

$a < b < \lambda$
Maxwell-Garnet model

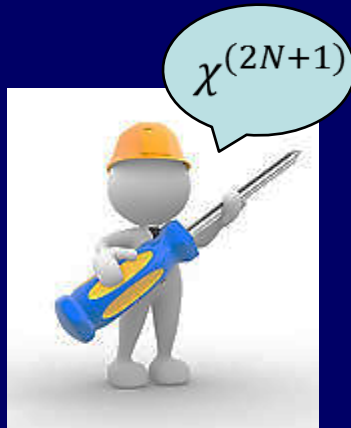
$$\chi_{eff}^{(3)} = f L^2 |L|^2 \chi_{np}^{(3)} + \chi_h^{(3)},$$

$$L = 3\varepsilon_h^{(L)} / (\varepsilon_{np}^{(L)} + 2\varepsilon_h^{(L)})$$

$$\chi_{eff}^{(5)} = f L^2 |L|^4 \chi_{np}^{(5)} - \frac{6}{10} f L^3 |L|^4 (\chi_{np}^{(3)})^2 - \frac{3}{10} f L |L|^6 |\chi_{np}^{(3)}|^2,$$

$$\begin{aligned} \chi_{eff}^{(7)} = & f L^2 |L|^6 \chi_{np}^{(7)} + \frac{12}{35} f L^4 |L|^6 (\chi_{np}^{(3)})^3 + \frac{3}{35} f |L|^8 \left[4L^2 \chi_{np}^{(3)} + |L|^2 (\chi_{np}^{(3)})^* \right] |\chi_{np}^{(3)}|^2 \\ & - \frac{4}{7} f L |L|^6 \left[2L^2 \chi_{np}^{(3)} + |L|^2 (\chi_{np}^{(3)})^* \right] \chi_{np}^{(5)}, \end{aligned}$$

Nonlinearity Management

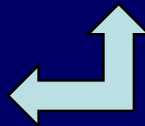


A procedure to obtain exotic metal-dielectric composites

It is possible to suppress one specific order of nonlinearity and enhance another one

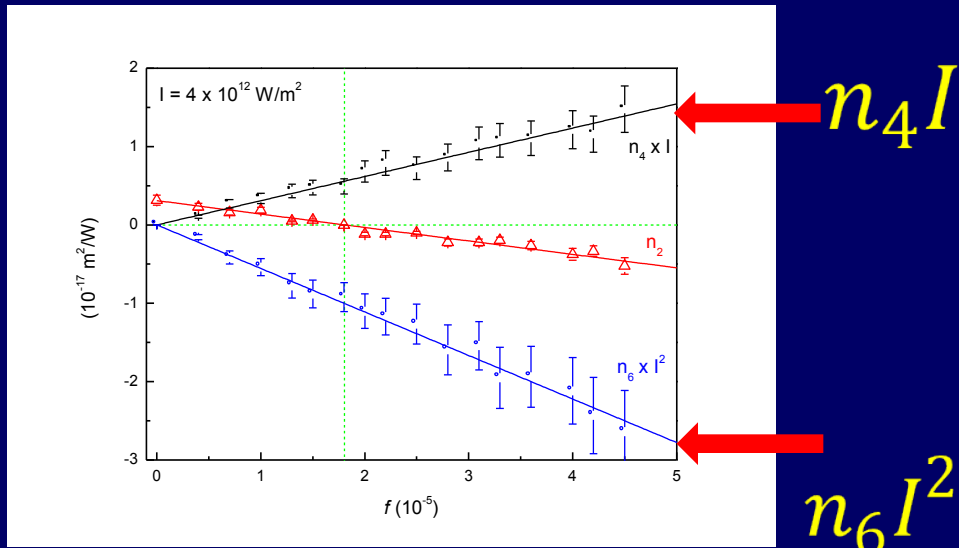
Example: $n_2=0$ and $n_4 \neq 0$

$$n_2 \propto \text{Re}\chi_{eff}^{(3)}$$

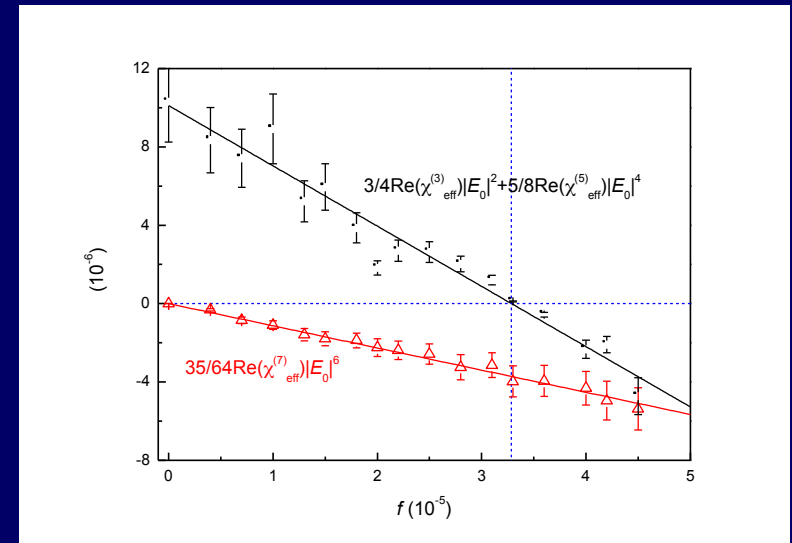


$$n_4 \propto \text{Re}\chi_{eff}^{(5)}$$

Nonlinearity management: Silver NPs + CS₂



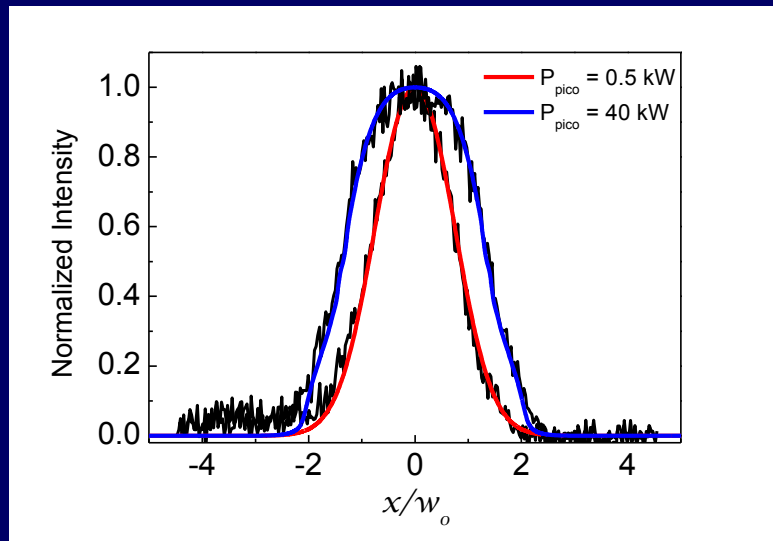
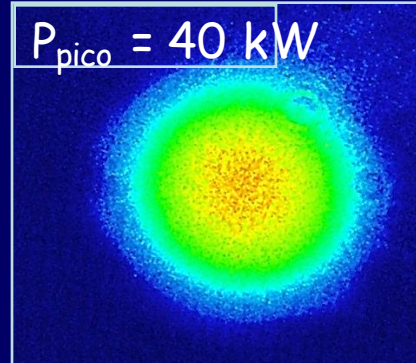
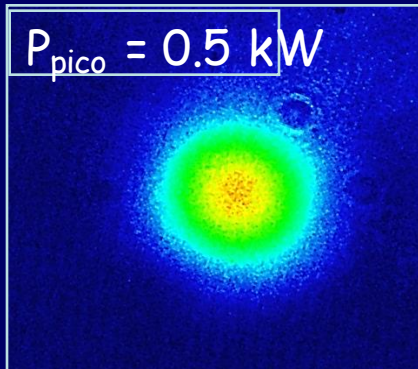
$4 \times 10^8 \text{ W/cm}^2$



$1 \times 10^8 \text{ W/cm}^2$

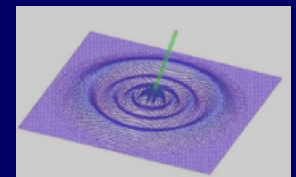
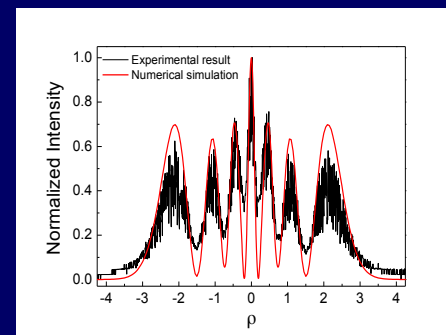
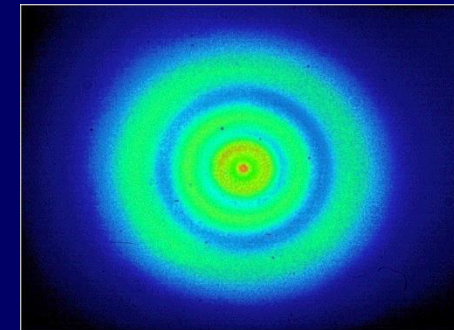
Effective $\chi^{(7)}$

Self-defocusing due to $\chi^{(7)}$ $f = 3.3 \times 10^{-5}$



Input plane out of the lens focus

$$I = 70 \text{ GW/cm}^2$$



Cross-phase modulation with two counter - propagating beams

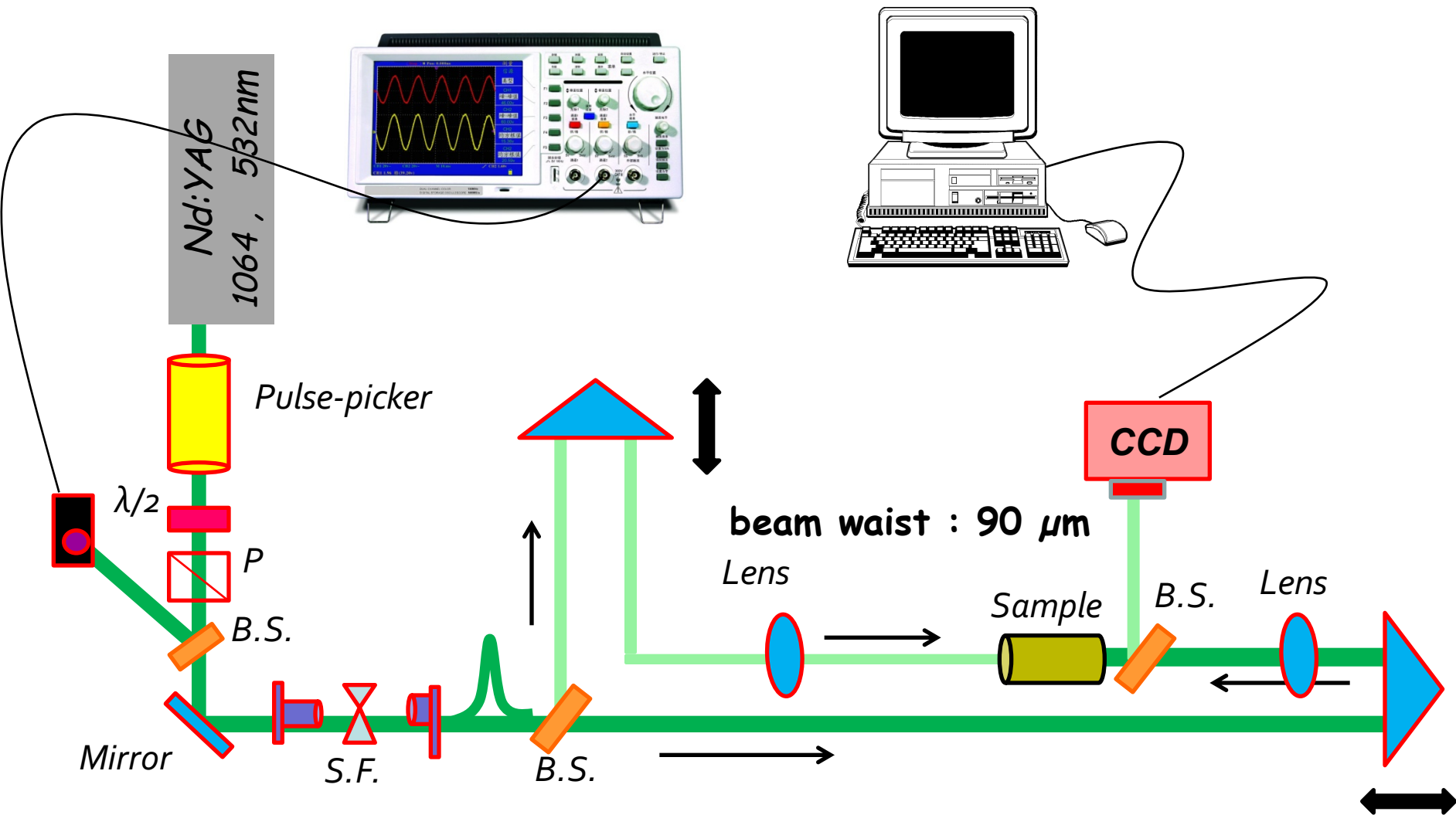
$$-\frac{\partial A_1}{\partial z} - \frac{i}{2k} \left(\frac{\partial^2 A_1}{\partial x^2} + \frac{\partial^2 A_1}{\partial y^2} \right) = \frac{ikn_2}{n_0} \left(|A_1|^2 + 2|A_2|^2 \right) A_1 + \frac{ikn_4}{n_0} \left(|A_1|^4 + 6|A_1|^2 |A_2|^2 + 3|A_2|^4 \right) A_1,$$

$$\frac{\partial A_2}{\partial z} - \frac{i}{2k} \left(\frac{\partial^2 A_2}{\partial x^2} + \frac{\partial^2 A_2}{\partial y^2} \right) = \frac{ikn_2}{n_0} \left(|A_2|^2 + 2|A_1|^2 \right) A_2 + \frac{ikn_4}{n_0} \left(|A_2|^4 + 6|A_1|^2 |A_2|^2 + 3|A_1|^4 \right) A_2,$$

↑
Third-order

↑
Fifth-order

Spatial Cross-Phase Modulation



NPs: 9 nm, $L=5$ cm, $I_{\text{pump}}=2$ GW/cm², $I_{\text{probe}} = 0.1 I_{\text{pump}}$ ⁵⁴

Counter-propagating beams

First observation of Spatial Modulational Instability due to $\chi_{eff}^{(5)}$

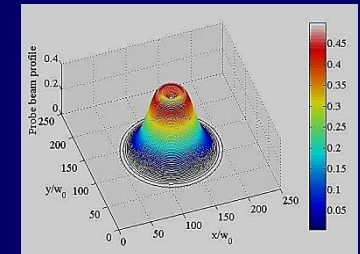
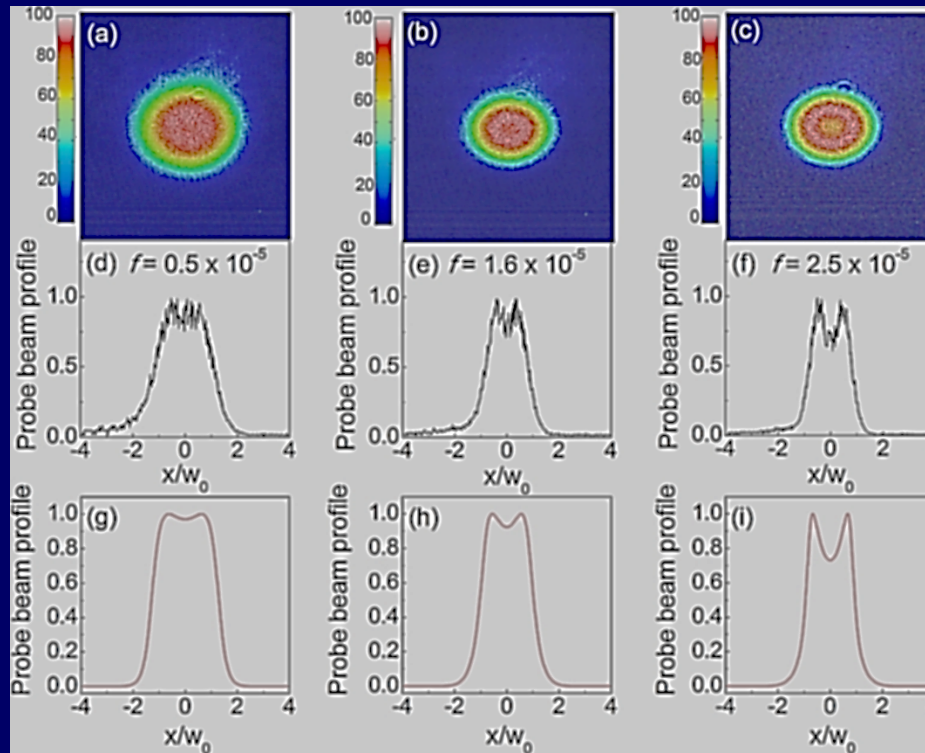
Probe beam profile



Profiles from the images



Theory



$$\text{Re } \chi^{(3)} = 0$$

$$\text{Re } \chi^{(5)} > 0$$

Ag NPs + acetone

$$n_2 = 0$$

$$n_4 = +3.2 \times 10^{-25} \text{ cm}^4 / W^2$$

Cross-phase modulation

Co-propagating beams

$$\begin{aligned}
 -2ik \frac{\partial E_1}{\partial z} + \Delta E_1 = & -\frac{\omega^2}{c^2} \left[3\chi_{\text{eff}}^{(3)} (|E_1|^2 + 2|E_2|^2) E_1 \right. \\
 & + 10\chi_{\text{eff}}^{(5)} (|E_1|^4 + 6|E_1|^2 |E_2|^2 + 3|E_2|^4) E_1 \\
 & \left. + 35\chi_{\text{eff}}^{(7)} (|E_1|^6 + 18|E_1|^2 |E_2|^4 + 12|E_1|^4 |E_2|^2 + 4|E_2|^6) E_1 \right]
 \end{aligned}$$

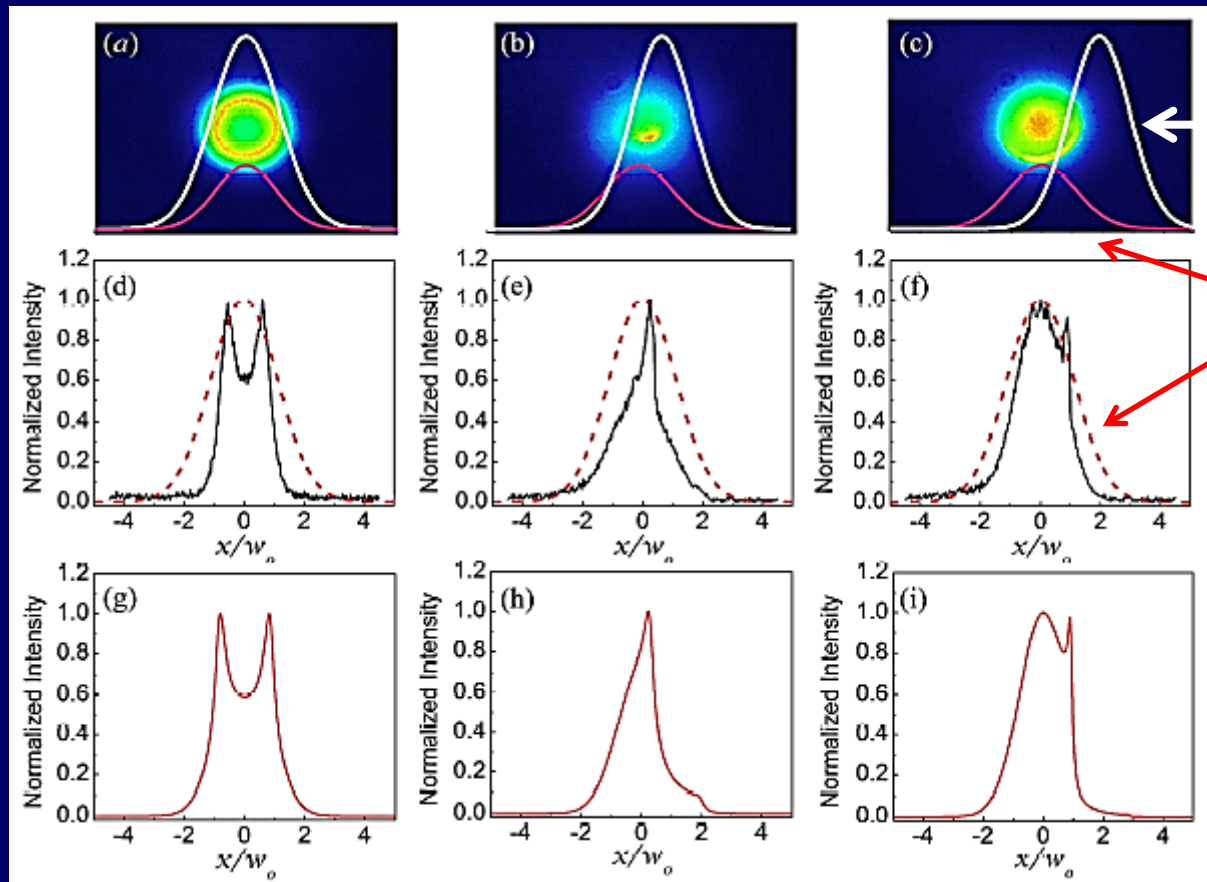
$$\begin{aligned}
 2ik \frac{\partial E_2}{\partial z} + \Delta E_2 = & -\frac{\omega^2}{c^2} \left[3\chi_{\text{eff}}^{(3)} (2|E_1|^2 + |E_2|^2) E_2 \right. \\
 & + 10\chi_{\text{eff}}^{(5)} (3|E_1|^4 + 6|E_1|^2 |E_2|^2 + |E_2|^4) E_2 \\
 & \left. + 35\chi_{\text{eff}}^{(7)} (4|E_1|^6 + 12|E_1|^2 |E_2|^4 + 18|E_1|^4 |E_2|^2 + |E_2|^6) E_2 \right].
 \end{aligned}$$

Induced focusing due to the seventh-order susceptibility

Experiment

Experiment

Theory

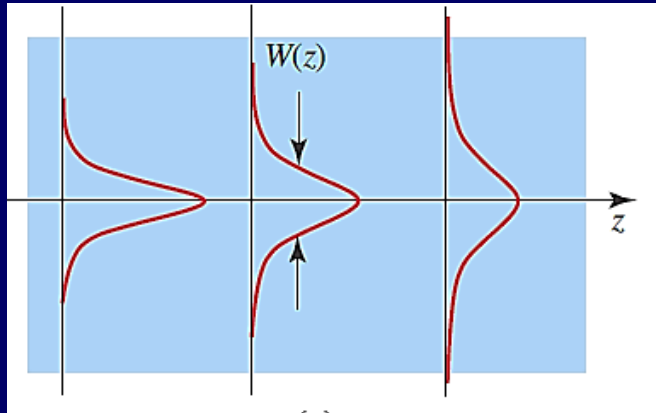


Pump
beam profile

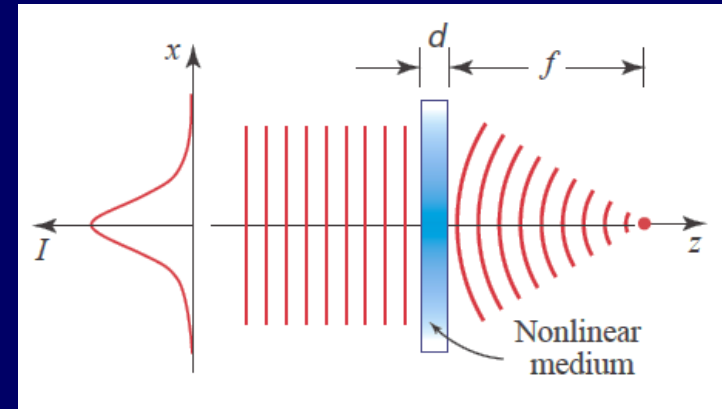
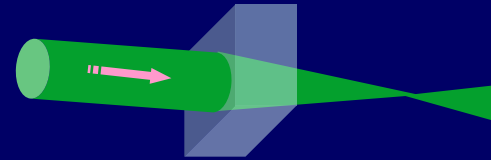
Input
probe
beam
profile

$$n_2 = 0; \quad n_4 = 0; \quad n_6 < 0$$

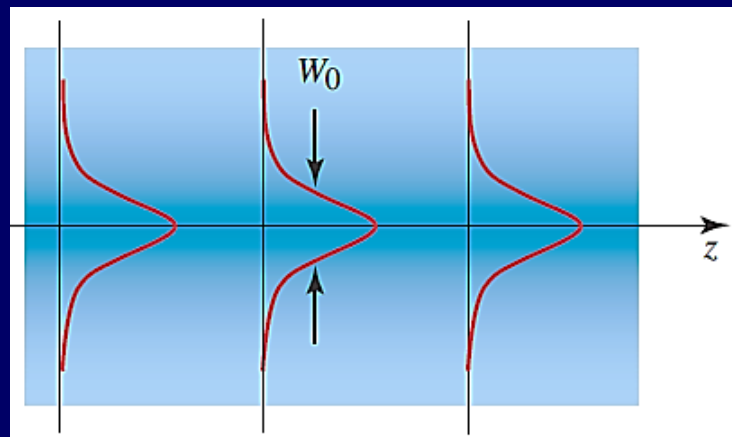
Diffraction



Self-focusing

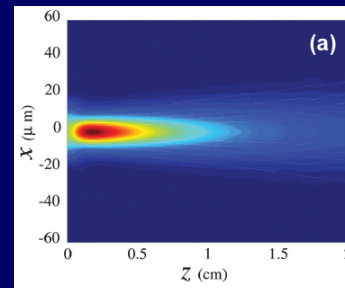
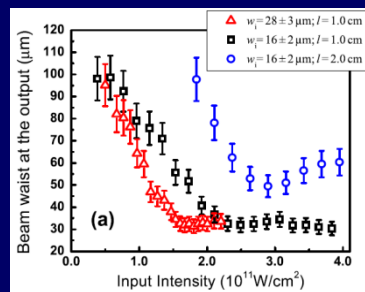
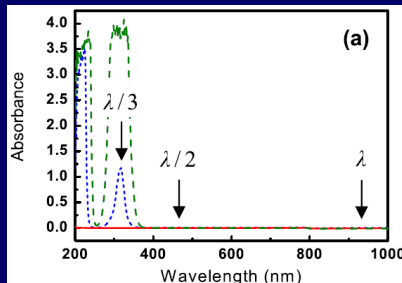


Bright Spatial Soliton

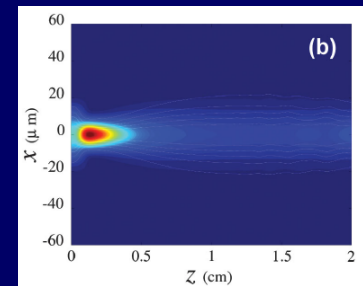


First demonstration of (2+1)D soliton propagating in a homogeneous medium with local nonlinearity

Falcão-Filho, de Araújo, Boudebs, Leblond, Skarka
Robust two-dimensional spatial solitons in liquid carbon disulfide
Phys. Rev. Lett. 110 (2013) 013901.



Low intensity



soliton

Very important: contributions of third and fifth order of opposite signs

CS_2 : stable (2+1)D soliton

$$Re \chi^{(3)} > 0$$

$$Re \chi^{(5)} < 0$$

Is it possible to observe a stable (2+1)D soliton
in a system with:

$$Re \chi^{(3)} = 0 \quad , \quad Re \chi^{(5)} > 0 \quad , \quad Re \chi^{(7)} < 0 \quad ?$$

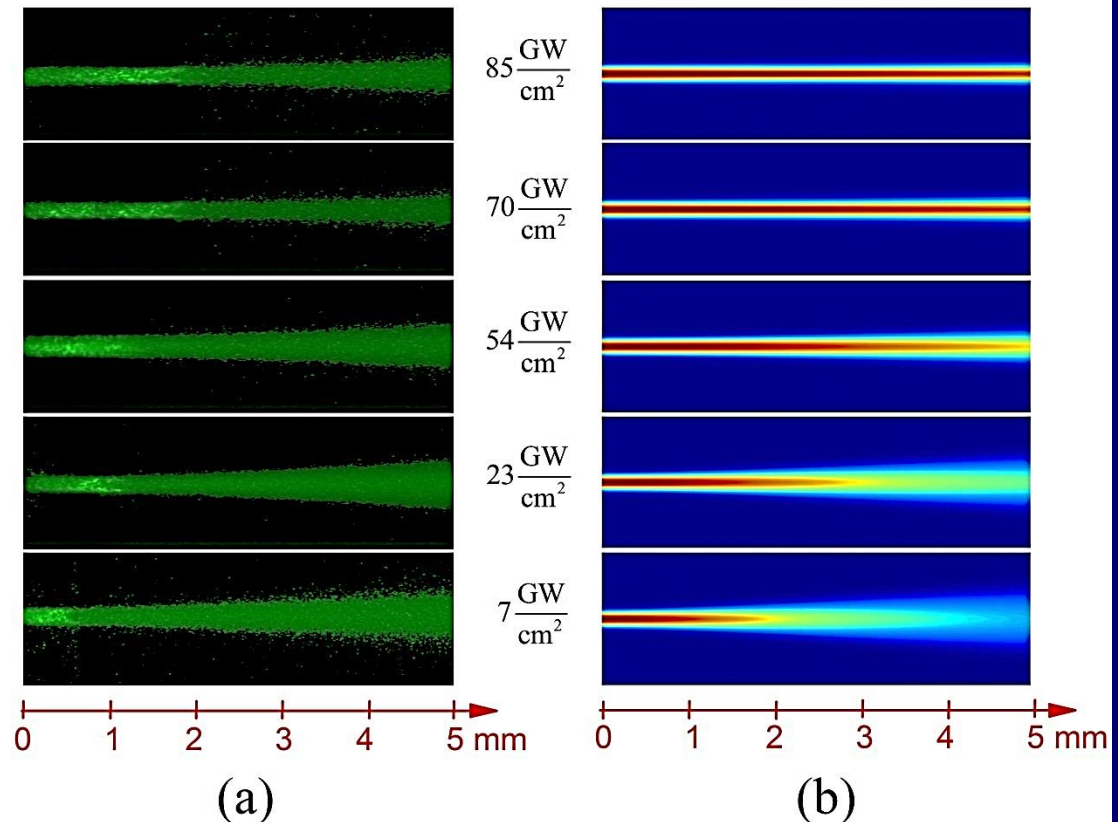
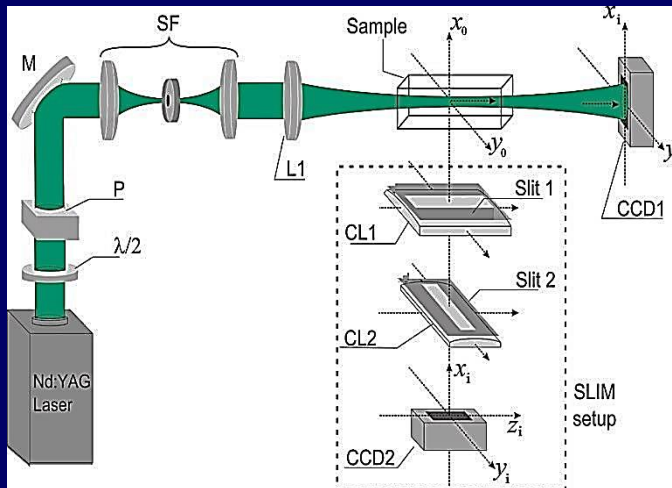
$$2ik \frac{\partial E}{\partial z} + \Delta E = -\frac{\omega^2}{c^2} \left[3\chi_{eff}^{(3)} |E|^2 E + 10\chi_{eff}^{(5)} |E|^4 E + 35\chi_{eff}^{(7)} |E|^6 E \right]$$

First observation of 2D Spatial-Solitons in a quintic-septimal medium

Silver NPs
in acetone

$$n_2 = 0; \quad n_4 > 0; \quad n_6 < 0$$

$$\chi^{(2N+1)}$$



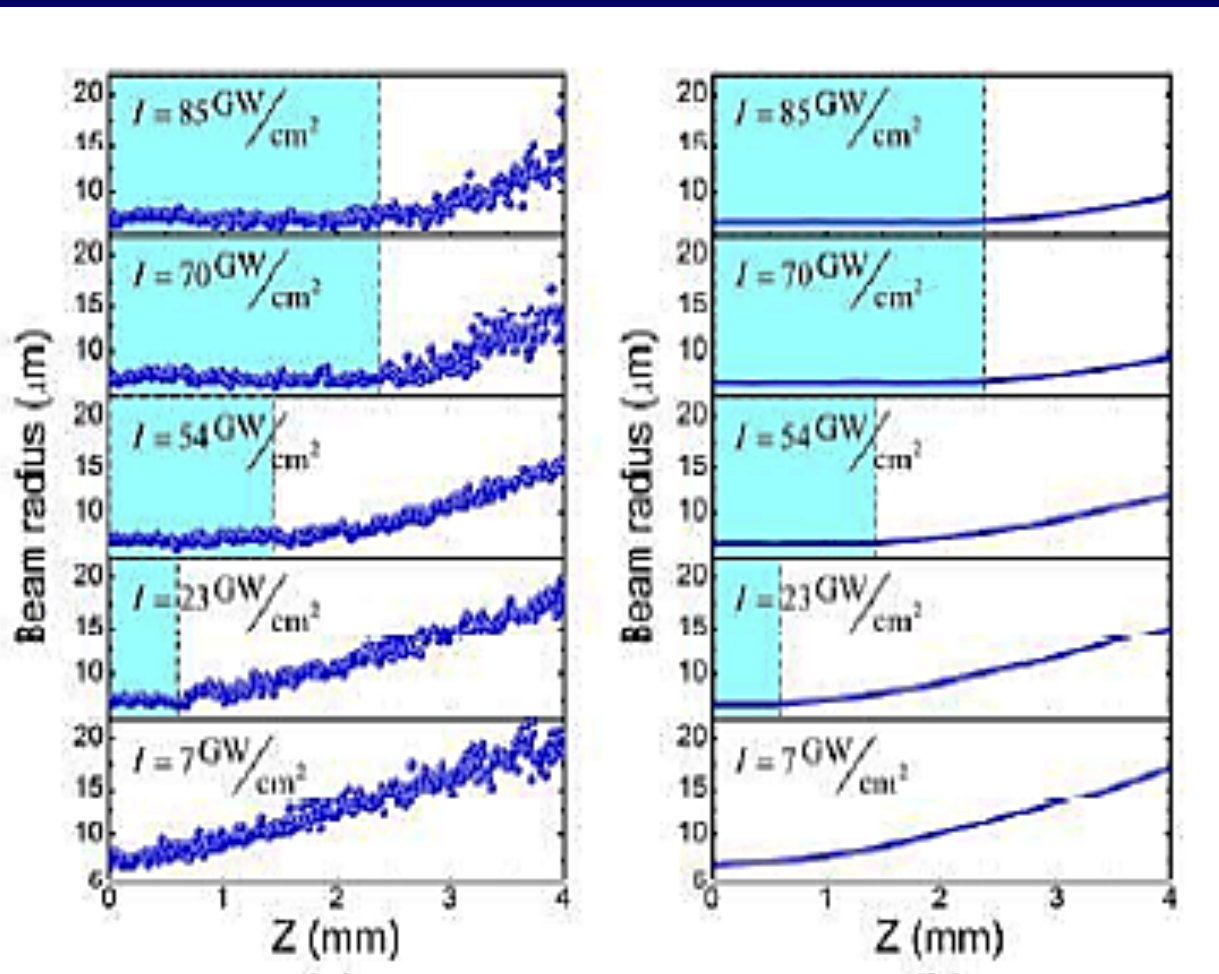
experiment

theory

Reyna, Jorge, de Araújo,
de Araújo et al. ,

Phys. Rev. A 90 (2014) 063835
J. Lumin. 169 (2016) 492-496

$$2ik \frac{\partial E}{\partial z} + \Delta E = -\frac{\omega^2}{c^2} \left[3\chi_{\text{eff}}^{(3)} |E|^2 E + 10\chi_{\text{eff}}^{(5)} |E|^4 E + 35\chi_{\text{eff}}^{(7)} |E|^6 E \right]$$

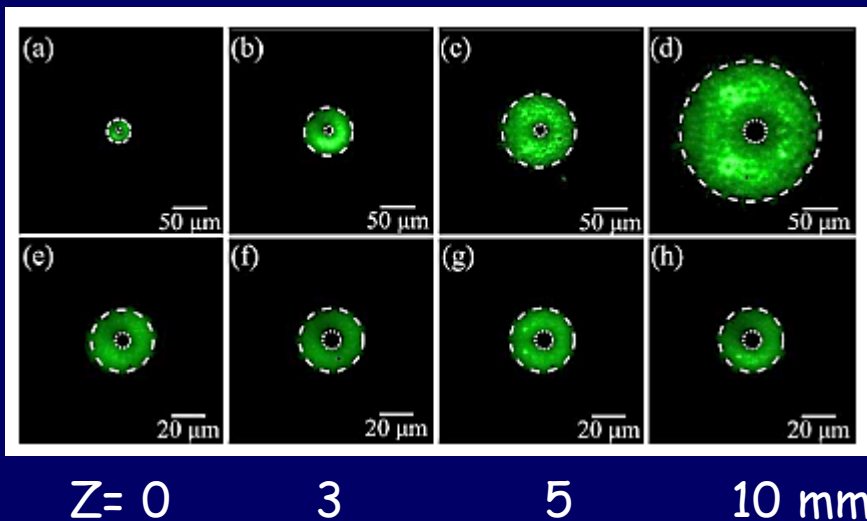
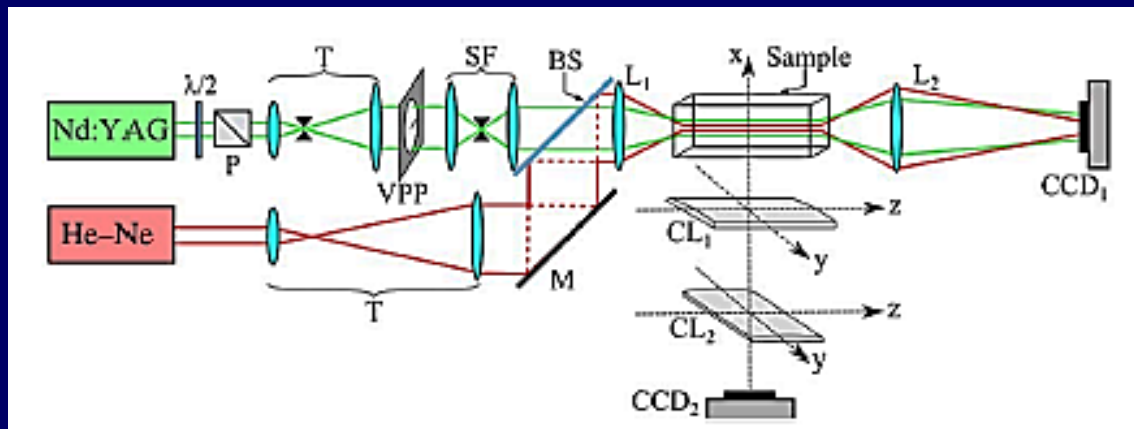


experiment

theory

Guiding and confinement of light induced by optical vortex solitons in a cubic-quintic medium

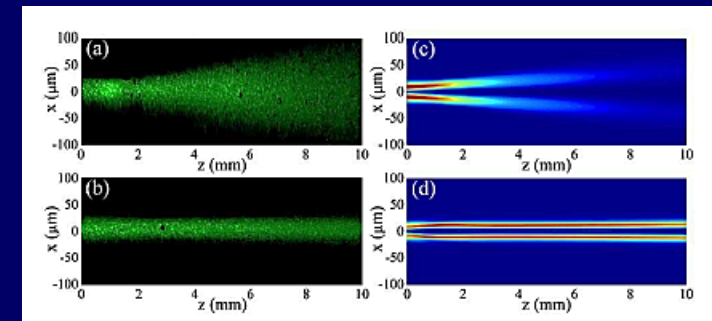
ALBERT S. REYNA* AND CID B. DE ARAÚJO



0.1

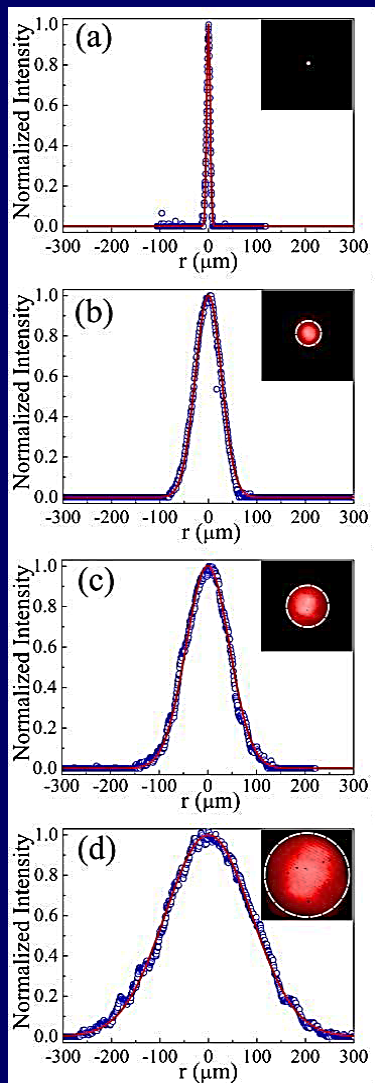
3.0

GW/cm^2

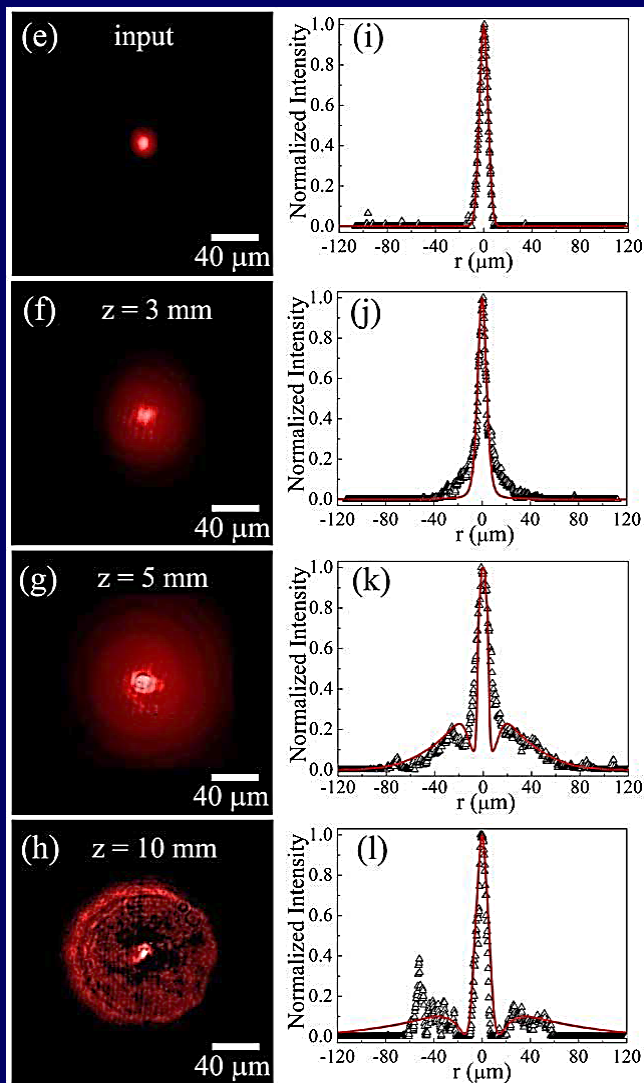


10 mm - 25 Z_R

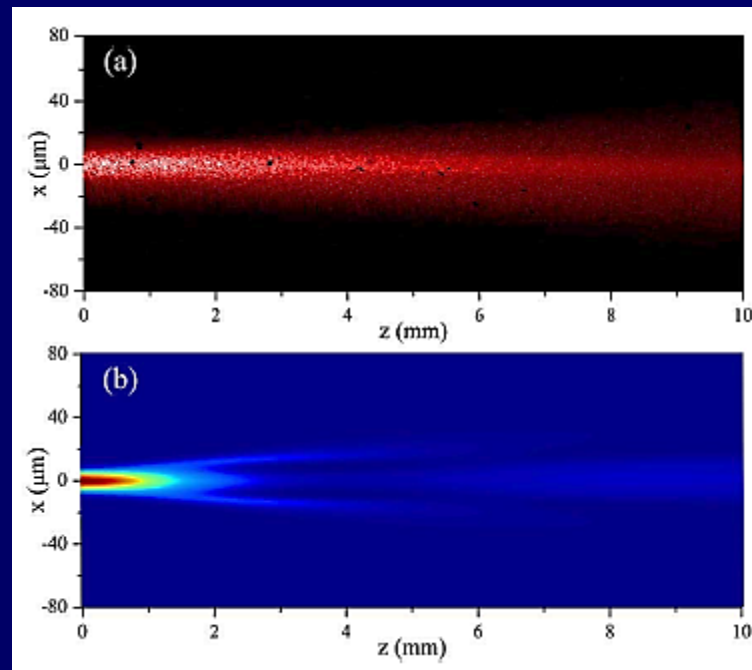
63



HeNe



Guided HeNe



$$I_{\text{OVS}} = 3.0 \text{ GW/cm}^2$$

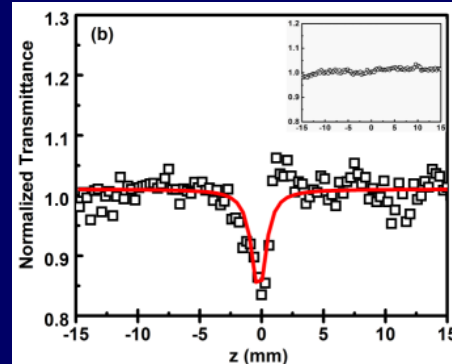
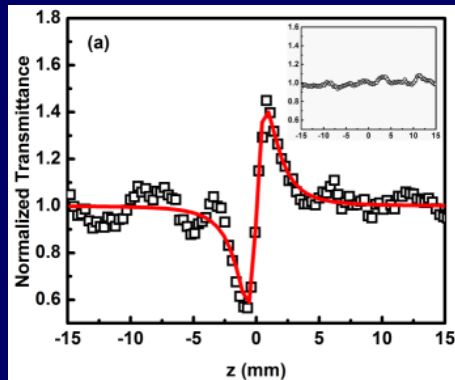
$$I_{\text{HeNe}} = 0.1 \text{ GW/cm}^2$$

How to address the long standing problem of discovering a very good material for all-optical switching?

We need a material with large NL refraction and low NL absorption

In general large NL refraction presents large NL absorption

PbO-GeO₂ films with gold NPs for all-optical switching



RF sputtering

800 nm

150 fs

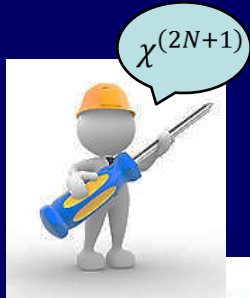
Figure-of-merit
enhanced by two
orders of magnitude

Germanate film	$n_2/\lambda\alpha_2$
As grown	8.3×10^{-4}
With Au NPs	$>2.1 \times 10^{-1}$

Optimization procedure for the design of all-optical switches based on metal-dielectric nanocomposites

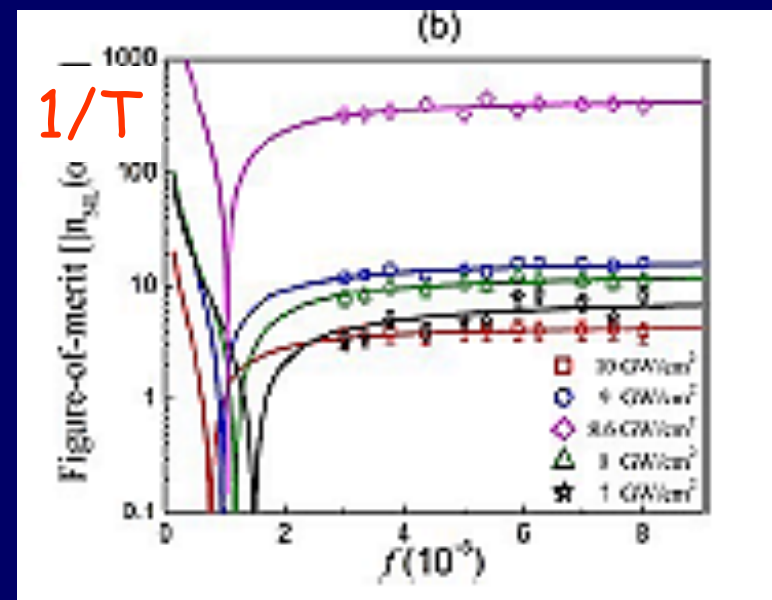
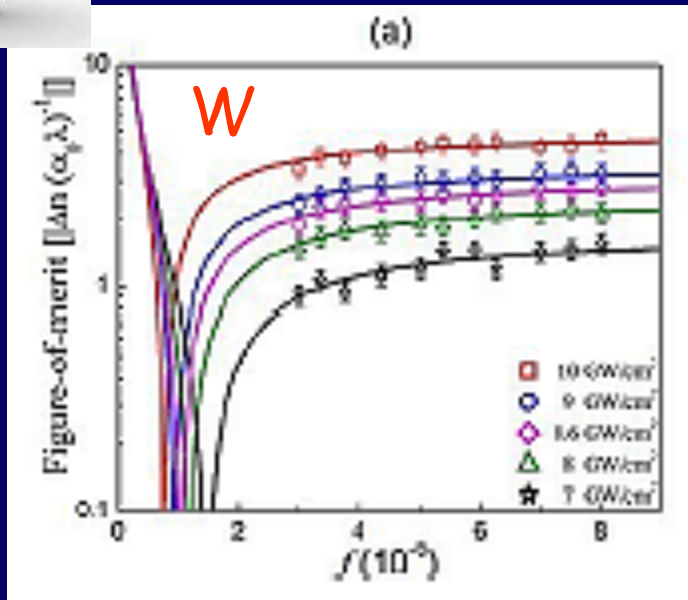
$$\Delta n = n_2 I + n_4 I^2 + n_6 I^3 + \dots = n_{NL} I$$

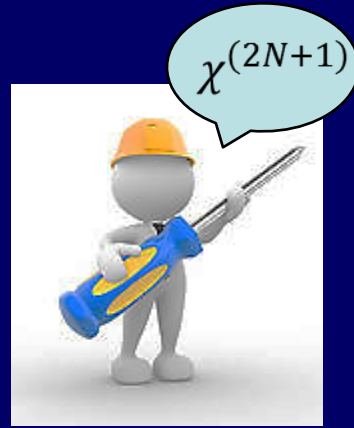
$$\alpha_{NL} = \alpha_2 + \alpha_4 I + \alpha_6 I^2 + \dots$$



$$W = \frac{\Delta n}{\lambda \alpha_0} > 1$$

$$T = \frac{\lambda \alpha_{NL}}{n_{NL}} < 1$$





These results show that it is possible to have an efficient all-optical switch if a nanocomposite is made according to the nonlinearity management procedure presented

Challenge for
materials scientists

Summary

Metal composites present large NL susceptibility which depends on the shape and volume fraction of NPs

Metallic NPs can be nucleated inside different media allowing enhancement of:

- luminescence properties (Stokes and anti-Stokes)
- optical gain/amplification in waveguides
- random lasers, DFB lasers
- all-optical switching, etc.

Nonlinearity Management



The control of NPs volume fraction allows suppression and/or enhancement of nonlinear optical contributions

Robust two-dimensional spatial solitons in liquid carbon disulfide
Phys. Rev. Lett. 110 (2013) 013901.

Two-dimensional solitons in a quintic-septimal medium.
Phys. Rev. A 90 (2014) 063835.

Nonlinearity management of photonic composites and observation of spatial-modulation instability due to quintic nonlinearity.
Phys. Rev. A 89 (2014) 063803.

Spatial phase modulation due to quintic and septimal nonlinearities in metal colloids. *Opt. Express* 22 (2014) 22456.

An optimization procedure for the design of all-optical switches based on metal-dielectric nanocomposites. *Opt. Express* 23 (2015) 7659 .

Robust self-trapping of optical vortex beams in a saturable optical medium. *Phys. Rev. A* 93 (2016) 013840.

Taming the emerging beams after the split of optical vortex solitons in a saturable. *Phys. Rev. A* 93 (2016) 013843.

Guiding and confinement of light induced by optical vortex solitons in a cubic-quintic medium. *Opt. Lett.* 41 (2016) 191.

Thank you for your attention

Our work has been supported by the Brazilian agencies

